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Citation: AIP Advances 7, 105104 (2017); doi: 10.1063/1.5005017
View online: http://dx.doi.org/10.1063/1.5005017
View Table of Contents: http://aip.scitation.org/toc/adv/7/10
Published by the American Institute of Physics
2D PIV measurement on the interaction zone between two parallel planar jets in a crossflow

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(Received 26 May 2017; accepted 26 September 2017; published online 6 October 2017)

This paper reports an experimental investigation on the zone between two parallel planar jets in a crossflow, termed as the interaction zone. The experiment was conducted using 2D PIV measurement, which involves a test matrix designed for a parametric study. Based on both mean and instantaneous results, effects of different parameters, i.e. front jet velocity, space between the two jets, and crossflow flow velocity, on the interaction zone were analysed. The two coupled recirculation structures, size, velocity field, and turbulence characteristics of the interaction zone are discussed. In addition, the large-scale vortices inside the interaction zone were recognised using $\Gamma$ value. How these different parameters affect the evolution of these vortices was also studied. © 2017 Author(s). All article content, except where otherwise noted, is licensed under a Creative Commons Attribution (CC BY) license (http://creativecommons.org/licenses/by/4.0/). https://doi.org/10.1063/1.5005017

I. INTRODUCTION

Tandem jets in a crossflow (TJCF) can be found in a number of engineering applications, e.g. lift jets of V/STOL aircraft, turbine blade cooling, and flow-induced noise reduction.¹⁻³ As a generic flow regime, extensive studies, especially in experiment⁴⁻¹⁵ have been performed for both research and engineering interest. The performance of the jets has a great impact on the entire flow field. Therefore, the characterisation of the jets has become the main research area in TJCF.

Previous observations from the experiment⁵,⁷,¹¹,¹³ showed that when tandem jets, for example, dual jets are ejected into a crossflow, both of them will be deflected downstream. However, due to the shielding from the front jet, the crossflow momentum around the rear jet will be substantially reduced and therefore it will deflect less than the front jet. As a consequence, the two jets will gradually merge and finally combine into one. In addition to the deflection, the shielding from the front jet has been found to have more impact on the rear jet, in terms of decay rate of the mean centerline velocity,¹² jet spreading,¹² entrainment,¹⁴ vortices,¹⁴ etc.

When it comes to vortex dynamics, two groups of vortices¹⁶ have been identified in the traverse jet in a crossflow. One group refer to those structures that are induced by the interaction among the jet, crossflow, and the wall, including Counter-Rotating Vortex Pair (CRVP), Horseshoe Vortices (HSV), Wall Vortices (WV) and Upright Vortices (UV). The other group consist of those structures that exist in the free jet as well, but whose evolution and destabilisation are influenced by the crossflow, e.g. Ring-Like Vortices (RLV).

One more characteristic that is worth mentioning is the recirculation zone below the rear jet. Discussions on the recirculation zone can be found in some studies on the single jet in the crossflow (SJCF).¹⁷⁻¹⁹ In particular, due to the shielding from the jet, the ambient fluid in the trailing side of the jet loses its crossflow momentum and is entrained into the jet. The strong entrainment quickly transports fluid that is close to the trailing edge of the jet, inducing pressure gradient. This gradient has

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to be offset by the fluid in the wall proximity. As such, a strong recirculation zone appears downstream to the jet.

To date, the vast majority of investigations of both TJCF and SJCF focus on the circular jet. This is mainly because the circular jet has more common engineering significance. However, to date experimental work on the planar jet in SJCF\textsuperscript{17,19–22} has found that the planar jets possess some distinct characteristics. Therefore, it necessitates more investigations on the tandem planar jets in a crossflow. In addition, previous work of TJCF mainly concentrates on the jets themselves. To obtain a better understanding of the entire flow field, more discussion on other areas is worth conducting.

The present study investigates an interesting region between two planar jets in the crossflow ambient. Since the development of this region is highly dependent on the interaction of the two jets, this region is termed as the interaction zone (IZ). Based on the 2D-PIV measurement, a parametric analysis was conducted to compare the effects on the IZ. Both mean and instantaneous results are reported in this paper, encompassing two coupled recirculation structures, velocity field, turbulence characteristics and large-scale vortices.

II. EXPERIMENTAL APPARATUS

Experiments were carried out in a subsonic open-jet wind tunnel. All measurements were made using a low-speed 2D-PIV system.

A. Wind tunnel system

The wind tunnel system used in this study consists of a subsonic open-jet wind tunnel, a test platform, and a planar jet generator, described in Fig. 1. The entire system was supported by aluminium extrusion frame.

The subsonic open-jet wind tunnel was used to create a crossflow up to 70 m/s, powered by a 5.5kW centrifugal blower. The nozzle of the tunnel, as illustrated in Fig. 1(a), was connected to a cubic plenum upstream, with a size of 800mm × 800mm × 800mm. The plenum can uncouple flow from the blower, pressurise the air, and suppress the turbulence level through two layers of mesh plate inside. The nozzle, with an outlet size of 75mm × 75mm, was made to be flush with a horizontal end-plate, shown in Fig. 1(b). On the endplate, two planar jet slots were installed, the configuration of which can be found in Fig. 1(c).

The crossflow ejected from the nozzle of the wind tunnel has been characterised using the hot-wire anemometry. The probe was a single-wire Dantec 55P15.\textsuperscript{23} As schematically shown in Fig. 2(a), a few sampling points were planned outside the nozzle of the crossflow, on which the measurement of the velocity was conducted. More specifically, the black shade illustrates the nozzle exit in scale. The bottom row of the sampling points are 2mm higher than the end-plate, and the distance between each row is 12.5mm. Based on the interpolation of the measurement results, the velocity profile of the crossflow nozzle can be achieved. In Fig. 2(b), the profile is reported as the contour superimposed on the nozzle exit, normalised by the maximum velocity in the profile. In this case, $U_\infty = 30.199$ m/s. Note that the crossflow and the jet velocities reported in this paper, i.e. $U_\infty$, $U_1$, and $U_2$, are the

![FIG. 1. Wind tunnel system: (a) crossflow nozzle; (b) endplate; (c) test section; (d) planar jet generator; (e) front jet nozzle junction; (f) examples of the front jet mesh.](image-url)
maximum velocity in the profile. Since the measurement was conducted in the centre-plane of the
crossflow, the velocity profile is also reported in Fig. 3. It is observed that there are three shear layers
on the top, right and left sides of the crossflow, respectively. The shear layers on the right and left sides
on the jet in the PIV measurement window can be ignored since the measurement was conducted
in the centre-plane. This will be further described in Section II B. As for the upper shear layer, the
entire crossflow as well as the upper shear layer will be defected by the jet. Therefore, it will not
interact with the planar jet. The turbulence intensity of the streamwise component below the upper
shear layer of the crossflow is within 1%.

The planar jet generator comprises a 2.2kW centrifugal blower, a cubic plenum and the two jet
slots. A hose was linked from the blower outlet to the bottom of the plenum. As described in Fig. 1(d),
the plenum was situated below the endplate and had a height of 540mm. The horizontal cross-section
of the plenum is 424mm × 424mm. Likewise, to reduce the turbulence level of the jets, one layer
of honeycomb with a hexagonal grid (6mm edge length) was mounted in the middle of the plenum.
Additionally, baffles were added to suppress recirculation. The two parallel jet slots were connected on the top of the plenum, the width \( w \) of which was 10mm and the spanwise length of the jet was 100mm. Note that \( P \), i.e. centre-to-centre space between the two jets, can be altered as required. The value will be reported later in Section II C. Considering the plenum was shared by the two jets, a special mechanism was adopted to manipulate the jet speeds independently. More specifically, in the junction between the font jet and the plenum, one thin mesh plate was installed, as schematically described in Fig. 1(e). The alloy mesh plate was designed with a variety of porosity. By changing the mesh plate and adjusting the actual power of the blower, the required speeds can be acquired for the two jets. Examples of the alloy mesh plate are given in Fig. 1(f). In the test program, only three jet velocities were used, i.e. 37m/s, 25m/s and 13m/s. The velocity profiles in the centre-plane of the jet has also been characterised by the hot-wire, reported in Fig. 4.

B. PIV arrangement

A 2-D low-speed PIV system was used to carry out all flow measurements, which allow a quantitative analysis of the flow regime. To visualise the flow field, both the jets and the crossflow were seeded with Pea Soup® Oil Based Smoke Generator PS31. The size of the particle was in the order of 1.5\( \mu \)m. The measurement plane was made to align with the centre-plane of the test section, which is also the farthest section to the corner. This contributes to the 2D representation of the flow field. Particles in the plane were illuminated using a sharp laser sheet. The source of the sheet was a New Wave Solo-II PIV double pulsed Nd:YAG laser (532 nm, 30 mJ/pulse), mounted on the top of the aluminium frame. One lens set was used to diverge the point source to a line source. In addition, in order to highlight the illuminated plane, one black PVC board was fixed behind the laser sheet as a dark background. Note that the board was outside the crossflow and accordingly had no interference.
with the flow. A LaVision® FlowMaster CCD camera was situated beside the test section, taking image pairs of the flow field of interest. A 532 nm narrowband pass optical filter was installed to the camera lens in the measurement. 3D CAD sketch of the PIV arrangement is shown in Fig. 5. The image pairs were captured at 4 frames per second, and the time delay between two images in one pair was 15 µs. The resolution of the CCD camera is 1280 pixels by 1024 pixels. In the set-up described above, the image size was 106 mm × 84.6 mm (X × Y). This allows the image to have a resolution of 12 pixels × 12 pixels per mm². Those image pairs were processed using cross-correlation in DaVis® software with decreasing multi-pass interrogation window sizes, 32 × 32 and 16 × 16, respectively. There were two passes and 50% overlap in each window size. The post-processing was performed with an open access Matlab toolbox-PIVMat.

C. Test programme

The test programme in this study was designed to study the effects of different parameters on the IZ. Fig. 6 is a schematic of the dual-jet configuration, along with a 2-D Cartesian coordinate system utilised throughout this paper. In this system, the origin of the system aligns with the centre of the rear jet outlet, with the X axis along the streamwise direction and Y normal to end-plate. Note that in all test cases, the rear jet position, with the reference to the crossflow nozzle, was fixed, i.e. l = 195 mm. By contrast, the front jet was installed with different distances P from the rear jet.

Parameters of each case in the test programme are tabulated in Table I. The velocity of the jet and crossflow was measured using an FCO510 Micromanometer equipped with a Pitot tube. Herein, the blowing ratio (k₁ and k₂) is introduced. In the study of SJIC, the blowing ratio is usually defined

<table>
<thead>
<tr>
<th>Run No.</th>
<th>Group No.</th>
<th>( U_\infty ) (m/s)</th>
<th>( U_1 ) (m/s)</th>
<th>( U_2 ) (m/s)</th>
<th>( P ) (mm)</th>
<th>( Re_1 )</th>
<th>( Re_2 )</th>
<th>( P/w )</th>
<th>( k_1 )</th>
<th>( k_2 )</th>
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<td>I,II,III</td>
<td>30.005</td>
<td>37.097</td>
<td>37.105</td>
<td>70</td>
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<td>26,000</td>
<td>7</td>
<td>1.24</td>
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<tr>
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<td>I</td>
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<td>25.649</td>
<td>37.209</td>
<td>70</td>
<td>18,000</td>
<td>26,000</td>
<td>7</td>
<td>0.85</td>
<td>1.24</td>
</tr>
<tr>
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<td>I</td>
<td>30.092</td>
<td>13.525</td>
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<td>26,000</td>
<td>7</td>
<td>1.06</td>
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</table>
as the ratio of the jet velocity to the local crossflow velocity. However, due to the shielding from the front jet, the local crossflow velocity of the rear jet is no longer $U_\infty$. In this paper, $k_2$ is still defined as $U_2/U_\infty$, which is the nominal blowing ratio of the rear jet. It is certain that the real blowing ratio of the rear jet is much greater than $k_2$.

As shown in Table I, each test case has been identified by a Run Number. These cases can be divided into three parametric groups, in which N1 is the baseline case. In Group I, N1, N2 and N3 have different $U_1$ (and $Re_1$ and $k_1$), they are compared to study the effects on the IZ from the front jet velocity. In Group II, N1, N4 and N5 were installed with different $P$ (and $P/w$), used to analyse the effects from the space between the jets. Group III have N1, N6 and N7. In this group, the two jets were ejected into different crossflow velocities, which can investigate the effects from different $U_\infty$.

In order to reach convergence of the mean properties, 1,500 image pairs were acquired for each case in the test matrix. In the mean flow field of all cases, the maximum uncertainty was found to be $\pm 0.017$ m/s.

Due to the shear layer on the sides of the crossflow, and the low aspect-ratio of the planar jet outlet, it is necessary to validate the 2D performance of the flow in the measurement range. Here we introduce a simple approach based on hot-wire measurement. This approach used similar sampling method in the crossflow velocity characterisation, shown in Fig. 2(a). However, due to the symmetry regarding the centre-plane, the data sampling was only conducted on the one side of the centre-plan. What is more, the sampling section is close to the downstream limit of the PIV window, instead of the the crossflow nozzle. This is because the flow spread more in the downstream than the upstream. Therefore, if the 2D performance is guaranteed downstream, the upstream flow will be also 2D. Here $h$ is used to term the height of the sampling point row, the sampling was taken at $h/w = 1$, $h/w = 3$, $h/w = 5$, and $h/w = 7$, respectively. In each row, there are 9 sampling point with different distance to the centre-plane. The velocity profiles are reported in Fig. 7, normalised by the centre-plane velocity. It is found that the velocity almost keeps the magnitude within a distance of 10mm. As such, it is sensible to say that the flow within the measurement plane, i.e. the centre-plane is two dimensional and we can proceed to the following discussion.

### III. RESULTS AND DISCUSSION

The mean velocity contour and streamlines of the IZ have been zoomed-in shown in Fig. 8. Due to the poor performance of the velocity magnitude calculation in the end-plate proximity, the lower side of the contour has been blocked in Fig. 8(a). Nonetheless, it is found that the streamline calculation, which is more related to the velocity direction, is less affected by the proximity effects. As such, the block is not added in Fig. 8(b). From the velocity contour it is observed that between the two jets, there exists an obvious low-speed area with a triangle-like shape, i.e. the IZ. This zone is isolated from the main crossflow stream by the two jets. Within the IZ, one relative high-speed area can be found in the middle, which is a noteworthy characteristic. As such, the velocity field of the IZ will be discussed in detail in Section III C, along with the turbulence properties. The streamline field is an informative approach to depicting the mean flow field. For example, it is clearly illustrated in Fig. 8(b) that the crossflow is subsequently deflected by the front jet and the rear jet. More importantly, two obvious recirculation structures can be observed inside the interaction zone. In order to distinguish these two structures, hereinafter the large one upstream is termed as $R1$, and the small one downstream is termed...
as $R_2$. In this section, study on $R_1$ and $R_2$ is reported. Also, the large-scale vortices inside the IZ are discussed.

A. Coupled recirculation structures

$R_1$ and $R_2$ are two full recirculation structures that can be detected in the mean streamline field of the IZ. It is worth mentioning that research work by Gutmark et al.\textsuperscript{12} also observed the streamlines of two circular jets in a crossflow. However, despite the existence of recirculation, no such full structure was found due to the 3D configuration. As such, $R_1$ and $R_2$ can be recognised as a unique characteristic of the planar TJIC.

1. Formation of $R_1$ and $R_2$

The formation of $R_1$ and $R_2$ is highly correlated to the jet entrainment of the ambient fluid. Fig. 9 shows the vector field of the IZ, it is clearly shown that the rotation direction of $R_1$ and $R_2$ is clockwise and counter-clockwise, respectively. For $R_1$, when the front jet is discharged, the crossflow momentum inside the IZ will be shielded. As a consequence, the relatively quiescent fluid in the trailing proximity of the front jet will be continuously entrained into the jet, inducing a pressure gradient. Due to the 2-D characters of the planar jet, this gradient has to be offset by the fluid downstream, which in turn will also lead to new pressure gradient herein and drag down the fluid from the upper side of the IZ. Therefore, $R_1$ is established with a clockwise rotation. As mentioned in Section I, in SJIC a large recirculation zone can be also observed downstream to the jet.\textsuperscript{17–19} As such, $R_1$ corresponds to the same recirculation structure of the front jet, but confined inside the IZ by the rear jet.

The formation of $R_2$ is more related to the vortex dynamics of the rear jet. Experimental studies on the circular jet to date\textsuperscript{16,25,26} found from instantaneous results that, when the jet is ejected into a crossflow ambient, horseshoe vortices (HSV) can develop in the leading side of the jet orifice and roll up. Then it will wrap around the jet orifice, evolve to the downstream field, and become coherent vortices.
In the 2D field, the roll-up of the HSV will be substantially enhanced. Due to the time-dependent periodicity, a recirculation zone in the mean flow field will establish in the leading side of the jet slot, with a contour-clockwise rotation. In the IZ of TJIC, the upstream recirculation zone of the rear jet extends due to the reduced crossflow momentum. As such, it develops to $R_2$ in the mean flow field. This also explains why the recirculation structures can be also observed upstream to the front jet. For example, in Fig. 10(e), the recirculation structure can be also observed upstream to the front jet, but with a much smaller size. This is because the downward portion of $R_1$ and the upward velocity of the rear jet contributes to a continuous pressure gradient around $R_2$. This gradient enhances $R_2$ and makes it much larger.

One more important aspect of $R_1$ and $R_2$ that is related to their formation is the coupling. To be more specific, the pressure gradient that drags down the fluid from the upper side of the IZ, couples $R_1$ and $R_2$. On one hand, the downward flow plays a role as the boundary to confine the relative position of the two structures. As a result, $R_1$ and $R_2$ have to be situated on each side of the IZ respectively. On the other hand, the downward flow is the edge shared by $R_1$ and $R_2$. Therefore, $R_1$ and $R_2$ are highly coupled with mutual effects.
2. Critical points and area of R1 and R2

Fig. 10 reports the mean streamline field in the IZ from all test cases. Overall, it appears that R1 is dominant over R2 in terms of the size. Besides, the area and the position of R1 and R2 vary with the parameters of the flow field. As such, in order to characterise the two coupled recirculation structures, R1 and R2 are quantitatively investigated from a topological point of view: the critical points and the size of the structures are compared, as a parametric analysis.

In the mean flow field, a critical point is a position where the velocity vanishes. For example, Fig. 11 shows three typical critical points inside 2D flow streamlines: centre point, saddle point, and reattachment point. To be more specific, the centre point is the pivot around which streamlines revolve; the stagnation point is where streamlines from different directions converge and then leave in other directions; the reattachment point is the stagnation point on the wall. In the streamline field, the location of the critical point can be determined using Taylor serious and the standard theory for Hamiltonian systems.28–30

The coordinates of the critical points are calculated and illustrated in Fig. 10. One centre point is found within each recirculation structures, and CP1 and CP2 are used to denote them respectively. One stagnation point, termed as SP, can be detected in the region where the front jet, the rear jet, R1, and R2 converge. On the end-plate, there exists one reattachment point between R1 and R2, denoted as RP. Because CP1 and CP2 are the centre point of the two recirculation structures, they can be used to assess the locus of R1 and R2’s motion. The stagnation point is where the streamlines of the jets and the recirculation structures converge, SP can be treated as the combining point of the two jets, viz. the upper limit of the IZ. As for RP, it is used to separate R1 and R2 and accordingly applied for the area calculation, introduced later in this same section.

In order to characterise the recirculation structures, the area is an important characteristic, which needs to be first addressed. Obviously, RP is the lower limit. Regarding the edge, they are recognised in this paper based on the velocity magnitude profile along the horizontal direction. More specifically,
FIG. 13. Velocity magnitude profiles of N1 acquired along the horizontal direction at (a) $y/w = 2.4$; (b) $y/w = 1.8$; (c) $y/w = 1.4$; (d) $y/w = 1$; (e) $y/w = 0.8$; (f) $y/w = 0.2$. Note that $U_{\text{max}}$ is the maximum velocity magnitude in each profile.

Fig. 12 is the schematic of the two jets, with a magnification view of the IZ. A number of horizontal lines between SP and the end-plate are made to extract velocity magnitude profiles from the IZ. In Fig. 13, examples of the velocity profiles from N1 at different $y/w$ are shown. It is observed that two peaks coexist in each profile (highlighted with the empty circle ◦), which can be reasonably attributed to the centreline of the jet, and the IZ is between them. Considering the width and spreading of the jet, the locus of the half magnitude point of each peak in the sampling profile is used to be the boundary between the jet and the IZ (highlighted with the solid circle •). Obviously, when $y/w = 0$, i.e. on the end-plate, the boundary begins at the trailing edge of the front slot and the

FIG. 14. Boundary defined for $R1$ and $R2$. 
leading edge of the rear slot, where $x/w = -6.5$ and $x/w = -0.5$, respectively. Both ends at SP. When it comes to the separation between $R_1$ and $R_2$, these two recirculation structures co-flow in the middle, increasing the velocity magnitude (further discussed in Section III C). As such, a minor peak can be observed in the middle of those profiles that are neither in the endplate proximity nor close to the SP. For example, those points marked with $\Delta$ in the profiles of Fig. 13(b)–(e). In fact, they are the location of the maximum downward velocity between $R_1$ and $R_2$. They are used for defining the shared edge of $R_1$ and $R_2$, along with SP and RP. Fig. 14 shows the boundaries defined using the approach described above, superimposed on the streamlines. It is shown that the edges between the IZ agree well with the outside streamlines of the recirculation zone. The shared edge between $R_1$ and $R_2$ also separates $R_1$ and $R_2$. Therefore, this definition can be used in the following analysis.

![Graphs showing coordinates of key points](image)

FIG. 15. Coordinates of the key points (CP1, CP2 and SP). (a) Group I(N1, N2 and N3): decreasing the strength of the front jet velocity; (b) Group II(N1, N4 and N5): decreasing the spacing between the two jets; (c) Group III(N6, N1 and N7): increasing the strength of the crossflow velocity.
As a parametric study, it is observed from Fig. 10 that the position of CP1, CP2 and SP is dependent on the flow conditions, so is the area of $R_1$ and $R_2$. To analyse the dependence, the coordinates of these three critical points are reported in the diagram in Fig. 15; the area of $R_1$, $R_2$, and $IZ$ (discussed in Section III B), calculated using numerical integration, is reported in the bar chart in Fig. 16.

Fig. 15(a) illustrates the variation of the key points with the front jet velocity $U_1$. It is found that when $U_1$ becomes smaller, all three key points descend and in the meanwhile, move downstream. Regarding the area, Fig. 16(a) shows that both areas of $R_1$ and $R_2$ become smaller. This trend can be further confirmed from the streamlines in Fig. 10(a)–(c). Therefore, it is concluded that with the decrease of $U_1$, both $R_1$ and $R_2$ will shrink and approach the rear jet slot proximity. In addition, the two jets will combine at a lower and more downstream location. All of the variations can be simply explained by the reduced shielding from the front jet. When the front jet has less momentum, the shielding it provides to the rear jet will be less, therefore the rear jet will deflect more. Thus, SP becomes not just lower but also more downstream. Also, $R_1$ and $R_2$ have to cut down their size and move downstream due to a compressed $IZ$. For example, both $R_1$ and $R_2$ become extremely small in N3 in Fig. 10(c), which has the lowest $U_1$.

Fig. 15(b) and Fig. 16(b) describe the effects from the jet space $P$. It is observed that when $P$ shortens, all of CP1, CP2 and SP gradually decrease. This is due to the reduction in the size of $R_1$ and $R_2$. As shown in Fig. 10(a),(d) and (e), when $P/w$ changes from 7 to 5, SP gets lower. $R_1$ and $R_2$
have to reduce their size because they are confined within a smaller IZ. In the meantime, a shorter size of \( P/w \) pushes \( R1 \) towards the rear jet, which means CP1 is also approaching the rear jet when its area reduces. However, SP and CP2 do not display a same consistent trend in the horizontal direction. More specifically, N2, which possesses the medium \( P/w \) among the three cases, is the closest one to the rear jet in terms of both SP and CP2. One more interesting thing is the upstream recirculation zone of the front jet, observed from the front jet in Fig. 10(d) and (e). Particularly, when \( P/w \approx 5 \) in Fig. 10(e), there is a full structure upstream of the front jet. It is worth noting that in other cases, there must be a similar structure existing upstream to the front jet. However, due to the limit of the PIV image range, it is not shown in other figures. As mentioned in Section III A 1, this one is a variation of the horseshoe vortices in the mean flow field, which corresponds to \( R2 \) within the IZ. Therefore, it is assumed that this recirculation structure exists in all front jets outside the image.

Fig. 15(c) and Fig. 16(c) illustrate the change of the key points and the recirculation areas with the crossflow velocity \( U_\infty \). Obviously, a lower \( U_\infty \) influences the size of \( R1 \) and \( R2 \), and the height of the centres. Also, the combination location of the two jets, SP will ascend to a higher position with a lower \( U_\infty \). However, similar to the effects from \( P \), the horizontal position of these key points do not move with a uniform trend as the crossflow velocity reduces.

**B. Size of the interaction zone**

The size of the interaction zone is an important characteristic that is worth considering. As depicted in Fig. 10, it is correlated with the investigating parameter. Here, the area of IZ was calculated as the sum of \( R1 \) and \( R2 \).

As Fig. 16 shows, the total area of the IZ is dependent on to \( U_1 \), \( P \) and \( U_\infty \), which agrees with Fig. 10. Within the range being tested, it is obvious that the area of the IZ is positively corrected with \( U_1 \) and \( P \), but negatively with \( U_\infty \). Furthermore, there are some extreme conditions that can be discussed without the test. For example, \( U_1 \to 0, P \to 0, U_\infty \to 0 \), respectively.

When \( U_1 \to 0 \), the scenario is similar to SJIC. Therefore, \( R1 \to 0 \), but \( R2 \) will restore to be the upstream recirculation of SJIC. Then the area of the IZ is equal to the upstream recirculation, termed as \( \Omega \) here in after. Note that for a particular \( P \), when \( U_1 \) increases but is still small, the front jet may directly merge with the crossflow ambient. This means that the front jet has little impact on the rear jet and the size of the IZ remains to be as same as \( \Omega \). But the size will be greater than \( \Omega \) when the front jet velocity is sufficiently high and it starts to interact wit the rear jet. When \( U_1 \to \infty \), this extreme condition will extend the potential core of the front jet to an infinity long distance, and the shear layer in both trailing and leading sides become so thin that can be ignored. Therefore, little spreading will happen to the front jet. More importantly, such powerful front jet will completely block the crossflow. Moreover, the entrainment of the fluid from the IZ plays a crucial role, inducing pressure gradient to drag the rear jet close to the front jet. It is reasonable to infer that this drag is overwhelmingly strong and can directly deflect the rear jet, which means the size of the IZ will go to zero. As such, it is expected that when \( U_1 \) increases from 0 to \( \infty \), there exists a peak value for the size of the IZ. The size will firstly remain to be equal to \( \Omega \), and then start to increase until it reaches the peak. Subsequently, it declines and gradually approaches zero.

When \( P \to 0 \), obviously the IZ will disappear with no area. As \( P \) increases, the size of the IZ will at first increase, shown Fig. 16(b). However, it is expected that when \( P \to \infty \), the front jet will have merged with the crossflow before making an influence on the rear jet, making the rear jet behave like the SJIC. The limit is \( \Omega \) as well. Therefore, it is concluded that a peak also exists when \( P \) moves from 0 to \( \infty \). Firstly, the area of the IZ remains to be \( \Omega \) until the front jet begins to interact with the rear jet. Then it will ascend to the peak and likewise, start to descend till zero.

When \( U_\infty \to 0 \), the dual jets will be ejected into a quiescent ambient. Previous studies\textsuperscript{31–33} on the dual moderately-spaced jets in a quiescent ambient reported that after ejection, two jets will merge and combine into one due to the mutual entrainment of each other. More importantly, a recirculation zone will show up between them. This can be the upper limit of the IZ size when \( U_\infty \to 0 \). Furthermore, it is easy to obtain the lower limit of the IZ regarding the crossflow velocity, i.e. the area of the IZ when \( U_\infty \to \infty \). Obviously, when such extreme condition happens, both jets will deflect immediately after ejection, which means the area goes to zero. As such, unlike \( U_1 \) and \( P \), it is expected that area of the IZ is negatively correlated with the crossflow velocity.
C. Velocity field and turbulence properties

As shown earlier in Fig. 8(a), there exists interesting characteristics in the velocity contour of the IZ, which are discussed in detail in this section. For ease of comparison, the contour with lines of the velocity field is illustrated in Fig. 17, along with CP1, CP2 and SP. Because $U_2$ is constant in all cases, the contour has been normalised by the rear jet velocity. It is observed that the magnitude around the three key points is the lowest within the IZ ($U/U_2 < 0.1$), which agrees with the definition in Section III A 2. The low-speed region around CP1, denoted as LSR$_{CP1}$, extends from the front jet trailing proximity to the middle of the IZ. It is obvious that this region is the core area of $R_1$. Likewise, the low-speed region around CP2, denoted as LSR$_{CP2}$ is the core area of $R_2$, close to the front jet. Another low-speed region, which has the maximum height, is situated around the stagnation point SP, denoted as LSR$_{SP}$. This is because the velocities from different directions cancel out here, making SP surrounded with slow velocity magnitude. Note that in LSR$_{CP1}$ and LSR$_{SP}$, the velocity magnitude is less that $0.1U_2$. This allows the boundary to align with the contour line so that the analysis can proceed.

In the middle of LSR$_{CP1}$, LSR$_{CP2}$ and LSR$_{SP}$, there exists an elliptic high-speed region, where $0.2 < U/U_2 < 0.3$. If compared with the streamlines in Fig. 10, the high-speed region is attributed to the shared edge of $R_1$ and $R_2$. More specifically, the two recirculation structures co-flow here, which accordingly raises the velocity magnitude. This high-speed region also separates LSR$_{CP1}$ from LSR$_{CP2}$ and LSR$_{SP}$. The area of this high-speed region is also dependent on the flow initial conditions. As for the separation between LSR$_{CP2}$ and LSR$_{SP}$, it is found to be the upper portion of $R_2$. However, this separation is ambiguous. As shown in Fig. 17(a)–(c), when $U_1$ reduces, LSR$_{CP2}$ and LSR$_{SP}$ tend to merge into one. From Fig. 17(a), (f) and (g), it is found that when $U_\infty$ becomes the lowest among the three cases, LSR$_{CP2}$ and LSR$_{SP}$ also merge. However, the comparison among Fig. 17(a), (d) and (e) shows that $P$ has less effect on the separation between LSR$_{CP2}$ and LSR$_{SP}$. Therefore, it suggests that the recirculation speed of $R_2$ is dependent on $U_1$ and $U_\infty$, but less dependent on $P$.

The mean characteristics of the turbulence are also analysed through the turbulence kinetic energy (TKE). In Fig. 18, the contour of TKE, normalised by the power of the rear jet velocity ($TKE/U_2^2$) is illustrated, along with SP, CP1 and CP2. Also, TKE at $y/w = 1$ and $y/w = 2$ are reported in Fig. 19 for information. In the proximity of the front jet outlet, high TKE can be found on both sides of the jet potential core, which are the shear layers. More importantly, the difference between...
these two shear layers is evident. It can be observed in Fig. 18, especially (d) and (e), that the leading shear layer is more turbulent than the trailing one when close to the end-plate. However, the trailing one, which is more related to the interaction zone, can develop farther and blend into the peak region. This is because the leading shear layer is directly exposed to the crossflow. As a result, when the crossflow momentum is stronger than the jet, the vortices with different scale sizes in the upstream shear layer, which contributes to the growth of the TKE, will be suppressed. At last, the shear layer merges with the deflected crossflow with low TKE. By contrast, the trailing shear layer close to the IZ is shielded, which benefits a farther spread. This conclusion can be confirmed by Fig. 18(b) and (c), when the front jet velocity is low, hardly can the high TKE region in the leading shear layer be observed. On the development of the vortices in the upstream shear layer of the front jet, more detail will be discussed in Section III D. It is worth noting that in Fig. 18(d) and (e), some high TKE can be found even ahead of the leading shear layer of the front jet. As mentioned earlier in Section III A 1, here is where the HSV develop. In terms of the mean field, there exists an upstream recirculation zone due to the front jet. As such, fluid here is more turbulent so that TKE increases.

D. Large-scale vortices

When a jet is discharged into a crossflow, formation and roll-up of the large eddies occur due to the Kelvin-Helmholtz instability. These coherent structures were found to have a significant impact on
the development of the jet, e.g. dispersion and mixing of the fluids, noise production, combustion.\textsuperscript{34–36} As previously mentioned in Section I, those large-scale vortices include, in reference to a circular jet, CRVP, HSV, WV, UV, and RLV.\textsuperscript{16} Due to the approximately 2-D character, the main flow feature of a planar jet is the RLV. However, since the shape does not resemble a ring, it is termed as a Shear Layer Vortices (SLV) in the planar jet.\textsuperscript{21} In this section, the large-scale vortices within the interaction zone is discussed, i.e SLV.

1. Recognition of the large-scale vortices

In order to recognise large-scale vortices from PIV instantaneous data, the $\Gamma_1$ criterion based on the topology of velocity field is used, proposed by Graftieaux et al.\textsuperscript{37} $\Gamma_1$ function can be used to locate the centre of large-scale vortices. Let $A$ denote a random point in the vector domain, surrounded by a
two-dimensional area $S$. $M$ is a different point within $S$. Therefore, the $\Gamma_1$ function of $A$ is expressed as:

$$\Gamma_1(A) = \frac{1}{S} \int_{M \in S} \frac{\mathbf{AM} \times \mathbf{U}_M \cdot \mathbf{z}}{|\mathbf{AM}| \cdot |\mathbf{U}_M|} \, dS$$

$$= \frac{1}{S} \int_S \sin \theta_M \, dS,$$

(1)

where $\mathbf{AM}$ is the radius vector, pointing from $A$ to $M$, $\mathbf{U}_M$ is the local velocity at $M$, $\theta_m$ is the angle between $\mathbf{AM}$ and $\mathbf{U}_M$, and $\mathbf{z}$ is the normal unit vector to the plane. If applied for PIV measurements, the $\Gamma_1$ value in the discrete vector field can be calculated as:

$$\Gamma_1(A) = \frac{1}{N} \sum_S \frac{\mathbf{AM} \times \mathbf{U}_M \cdot \mathbf{z}}{|\mathbf{AM}| \cdot |\mathbf{U}_M|}$$

$$= \frac{1}{S} \sum_S \sin \theta_M,$$

(2)

where $N$ is the number of point $M$ within $S$. According to Graftieaux et al., $N$ plays the role of a spatial filter, which can be adjusted to locate large-scale vortices. However, $N$ almost does not affect $\Gamma_1$ value of a vortex centre. After a few attempts $N$ was used as 15 in this study. For all points $\Gamma_1$ drops within the range between -1 and 1. Typically, $|\Gamma_1| > 2/\pi (\approx 0.637)$ corresponds to a presence of large-scale vortex, and whether $\Gamma_1$ is positive or negative corresponds to the clockwise or counter-clockwise rotation.

In Fig. 20, examples of the instantaneous velocity field from N1 at different time are shown, along with the $\Gamma_1$ contour superimposed. As a large-scale vortex detector, $|\Gamma_1| > 2/\pi$ well locates those vortices in each field. It is observed from all 1,500 results that the large-scale vortices only develop along the trailing edge of the front jet within the IZ, leading edge of the rear jet within the IZ, and trailing edge of the rear jet. However, no such structures exist on the leading edge of the front jet. As mentioned in Section III C, this can be attributed to the crossflow momentum. More specifically, when two jets are discharged, the front jet is directly exposed to the crossflow with a much larger momentum. Therefore, even though those eddies initially occur due to the shear layer instability in the leading edge of the front jet, the high-velocity gradient will quickly tear them up and transform them into small eddies. By contrast, with the shielding from the front jet, the crossflow momentum can be significantly reduced inside the IZ. This allows the large eddies to evolve before the two jets combine. Likewise, these large-scale eddies can also be found in the trailing edge of the rear jet, due to the shielding from both jets. In terms of the rotation direction, also found from the local vector field around the areas of $|\Gamma_1| > 2/\pi$ that those vortices in all trailing edges mentioned above are clockwise, and those in the leading edges, are counter-clockwise.

2. **Evolution of the large-scale vortices**

The $\Gamma_1$ value also makes it possible to evaluate the size of the large-scale vortices, which is defined as the total area around a core, where $|\Gamma_1| > 2/\pi$ in an instantaneous flow field. In this paper, the counter-clockwise vortices from the leading edge of the rear jet are calculated as an example. However, the evolution of an eddy includes formation, growth and finally fracture into more eddies with smaller sizes, which means the size of an eddy rapidly varies. Due to the limitation of the PIV sampling frequency, it is impossible to capture the entire process of an eddy’s evolution. Therefore, in order to obtain a parametric analysis on the size of counter-clockwise vortices, the probability of the size in statistics from all instantaneous results is adopted. As mentioned earlier, a positive or negative value of $\Gamma_1$ corresponds to a different rotation direction of an eddy, respectively. Here the negative one is considered to reckon the counter-clockwise vortices in the leading edge of the rear jet. First of all, those areas with $|\Gamma_1| > 2/\pi$ were recognised in from all 1,500 results. Among these 1,500 images, within 1% of them did not capture any counter-clockwise eddies. These results were eliminated from the total samples. Secondly, the size of the eddies based on $-1 < \Gamma_1 < -2/\pi$ were calculated respectively for each instantaneous result. In terms of the size distribution, those vortices were grouped into $0-2w^2$, $2w^2-6w^2$, $6w^2-10w^2$, $10w^2-14w^2$, $14w^2-18w^2$, and
FIG. 20. Examples of instantaneous vector fields from N1, with $\Gamma_1$ contour superimposed.

18$w^2$-20$w^2$. Here those large-scale eddies are subdivided into thee categories with different sizes: 0-2$w^2$ and 2$w^2$-6$w^2$ are treated as the small-size eddies; 6$w^2$-10$w^2$ and 10$w^2$-14$w^2$ are the medium-size eddies, 14$w^2$-18$w^2$, and 18$w^2$-20$w^2$ are the great-size eddies. The probability of each group is shown as a histogram in Fig. 21. Compared with other probabilities, those great-size eddies, especially 18$w^2$-20$w^2$, are much lower and cannot be clearly visualised. Therefore a zoomed sub-figure is made in each figure.

In Fig. 21, N1 is used as the baseline and is shown in all cases with a consistent legend. Fig. 21(a) describes probability variation against the rear jet velocity. It is found that when the front jet velocity reduces, the size of the large-scale vortices tends to shrink. In N3, which has the lowest $U_1$, among N1, N2, and N3, the probability mainly concentrates in the small-size and the medium-size eddies. No eddies over 10$w^2$ show up. With the increase of $U_1$ in N1 and N2, the probability of the great-size
eddy also increases. Therefore, it is concluded that a higher front jet velocity can contribute to the evolution of the large-scale eddies in the leading edge of the rear jet.

Fig. 21(b) illustrates the probability variation as a function of the space between two jets ($P$). Regardless of the value of $P$, the large-scale vortices can be observed with all different sizes. In other words, within the test range, no obvious correlation between the vortex evolution and $P$ can be found.

In Fig. 21(c), N1, N6, and N7 are compared to analyse the vortex size as a function of the crossflow velocity. Similarly, to $U_1$, the crossflow velocity is correlated with the vortex size. When the crossflow velocity increases from N7 to N1, then eventually N6, the probability of the great-size eddies reduces. For example, no great-size eddies can be detected in N7, which has the highest $U_\infty$. By contrast, the case with the highest probability of the small-size eddies is found to be N7. In terms of the medium-size eddies, this correlation between the crossflow velocity and the eddy size still
exists. To be more specific, N7 ranks between N1 and N6 for the size of $6w^2 - 10 w^2$, but becomes the lowest when the size increases to $10w^2 - 14w^2$. There is more randomness in the medium-size eddies. However, overall, the probability of the great-size eddies is the most when the crossflow is the lowest.

In summary, the histogram in Fig. 21 suggests that the size of the large-scale vortices in the leading edge of the rear jet is dependent on the shielding from the front jet. More specifically, when the front jet is faster or the crossflow is slower, an improved shielding can be given to the rear jet. As such, the evolution of the large-scale vortices can have more space to proceed, thus, more great-size eddies will occur.

IV. CONCLUSIONS

In this paper, a 2D PIV measurement of the interaction zone between two planar jets was conducted. Both mean and instantaneous flow field results were reported. Based on the data, discussions were made on the characterisation of the IZ, i.e. the two coupled recirculation structures, size, velocity and turbulence field of the IZ. Finally, an analysis of the large-scale vortices was conducted.

For the coupled recirculation structures, the formation of $R_1$ and $R_2$ was firstly discussed. Compared with SJIC, it is concluded that $R_1$ corresponds to the downstream recirculation zone of the single jet, and $R_2$ corresponds to the upstream recirculation zone of the single jet. Secondly, an analysis of $R_1$ and $R_2$ was made, from a topological perspective, on the critical points and the area. The critical points include two centre points (CP1 and CP2), one stagnation point (SP), and one reattachment point (RP). CP1 and CP2 were taken to assess the position of the recirculation structures, SP was used to be the converging point of the two jets and the height of the IZ, and RP was used to be the lower limit of the boundary between $R_1$ and $R_2$. It is found that the position of the two recirculation structures and the converging point of the two jets varies with different parameters, which, the area of $R_1$ and $R_2$ are also dependent on.

The size of the IZ was defined as the sum of $R_1$ and $R_2$, calculated for all cases in the test matrix. Within the range tested, the size was observed to increase with the front jet velocity and the space between two jets. However, it is negatively correlated with the crossflow velocity. Furthermore, some inference on the size of the IZ were made for the extreme conditions, i.e. $U_\infty \to 0\,\infty$, $U_1 \to 0\,\infty$ and $P \to 0\,\infty$, respectively. As such, a more complete variation process of the IZ size with different parameter was given.

On the velocity field and the turbulence characteristics. The shared edge between $R_1$ and $R_2$ was found to be the region with the highest speed inside the IZ. In addition, CP1, CP2 and SP were observed to be surrounded with low flow speed. LSP$_{CP1}$ is separated with other two by the shared edge. However, the separation between LSP$_{CP2}$ and LSP$_{SP}$ is ambiguous, especially when $U_1$ reduces or $U_\infty$ reduces. As for the turbulence characteristics, the contour of mean turbulence kinetic energy was shown. The contour revealed that the turbulence of the front jet leading shear layer is dependent on the crossflow, and that of the front jet trailing shear layer is dependent on the shielding from the front jet. The peak region of turbulence appears in the location where the front jet impinges the rear jet. The region with the lowest TKE is found to extend from the front slot proximity to CP1, and the area of the low-TKE region is dependent on the flow conditions.

As an instantaneous characteristic, the large-scale vortices, i.e. shear layer vortices were identified using $\Gamma_1$ value. To analyse the effects of different parameters, the probability of the SLV area in the leading edge was calculated and the histogram of the ranges different sizes was given. The conclusion was made that the shielding given by the front jet has a substantial impact on the evolution of the SLV.
