Tailoring highly conductive graphene nanoribbons from small polycyclic aromatic hydrocarbons: a computational study

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Abstract
Pyrene, the smallest two-dimensional mesh of aromatic rings, with various terminal thiol substitutions, has been considered as a potential molecular interconnect. Charge transport through two terminal devices has been modeled using density functional theory (with and without self interaction correction) and the non-equilibrium Green's function method. A tetra-substituted pyrene, with dual thiol terminal groups at opposite ends, has been identified as an excellent candidate, owing to its high conductance, virtually independent of bias voltage. The two possible extensions of its motif generate two series of graphene nanoribbons, with zigzag and armchair edges and with semimetallic and semiconducting electron band structure, respectively. The effects related to the wire length and the bias voltage on the charge transport have been investigated for both sets. The conductance of the nanoribbons with a zigzag edge does not show either length or voltage dependence, owing to an almost perfect electron transmission with a continuum of conducting channels. In contrast, for the armchair nanoribbons a slow exponential attenuation of the conductance with the length has been found, due to their semiconducting nature.

1. Introduction
In the search for suitable interconnects for nanodevices and molecular circuitry, since the first successful isolation of graphene in the laboratory [1], an interest has arisen in the meshes of this material [2]. Their organic analogs, polycyclic aromatic hydrocarbons (PAHs) have attracted particular attention because of the possibility to synthesize high molecular weight hexagonal carbon meshes [3]. Despite the high expectations of favorable charge transport through PAH wires, recent theoretical investigations have generally predicted a rather poor conductance and demonstrated an ineffective use of the conjugated carbon backbone [4–7]. An optimal class of molecular interconnects is expected to provide a high and consistent level of conductance for a length range of tens of nanometers and over a sizable bias region. In contrast, a strong localization regime is typically predicted for the transport even for the short PAHs [4–7]. Recently multiple chemical anchoring groups have been proposed for a more efficient coupling across the entire junction [8]. This simple idea has not only resulted in a dramatically enhanced electronic transport, but also in a much improved mechanical and thermal stability, which is also necessary for usable circuit operation.

The smallest PAH with a 2D hexagonal mesh is pyrene, with four benzene rings in the plane. Previous theoretical
investigations have unanimously predicted a low conductance for pyrène [4, 5, 7] and an even worse charge transport by its oligomers [6], due to the nonresonant tunneling mechanism and strong localization regime. Here we report computational results on the conductance through pyrène in various orientations with respect to the transport axis and terminal surfaces and with variable number and position of thiol head groups. After the identification of a highly conductive pyrène derivative two series of extended graphene nanoribbons were considered on the basis of this isomer. Both series display a high conductance. Whereas one set demonstrates an exponential attenuation of conductance with nanoribbon length, the other series exhibits a length and bias-independent conductance. Hence, the latter set shows very desirable transport properties as potential interconnects in molecular circuits.

2. Methods

The geometries of all the junctions considered here have been fully optimized, via the action of the conjugate gradient procedure, until the forces were smaller 10 meV Å⁻¹. The optimizations were performed using density functional theory (DFT) as implemented in the SIESTA program [9]. The LDA functional [10] was used in both the DFT and transport calculations.

A junction of Au(001) terminated leads has been utilized to model the two terminal device. The Au(001) surface was described by a square superstructure of eight gold atoms per layer. The optimized geometries obtained from the SIESTA computations, as well as all the relevant computational parameters, were subsequently employed in electron transport calculations. The latter were conducted using the non-equilibrium Green’s function (NEGF) Landauer approach [11] as implemented in the SMEAGOL package [12–14], which is interfaced to SIESTA. Self interaction correction (SIC) has been applied in combination with the LDA to the scattering region of the junction to partly rectify the artifacts arising from the band misalignment between the wire and terminals [15–18]. In the present work this has been done by utilizing the atomic self interaction correction (ASIC) [19, 20]. A value of 1.0 was used for the scaling parameter α, amounting to the full ASIC.

3. Results and discussion

In addition to the conventional 1,6-pyrene diethiol (1,6-PDT), with thiol groups on the long axis, two other para isomers of PDT have been considered, 2,7- and 3,8-PDT and a meta-substituted 2,8-PDT. In addition, a pyrène molecule with dual anchoring thiol groups has also been considered as a potential wire. This leads to two additional possibilities: pyrène-1,2,6,7-tetraethyl (PTT) and 2,3,7,8-PTT. Other combinations, such as 1,3,6,8-PTT, are not considered because the additional separation between the thiols would make double attachment to the terminals impossible, while 3,4,8,9-PTT has been treated elsewhere [21] very recently.

Based on previously published results, thiols bind to the low index gold surface most favorably via the hollow and bridge sites [22, 23]. Accordingly, two junction conformations have been considered for the 1,6-PDT wire: adsorbed on hollow and bridge sites, both in the upright orientation. Clearly, the other three PDT isomers cannot be adsorbed in the upright orientation and the same goes for the two PTT wires. Instead, these were initially positioned in the junction with the S atoms above either a hollow or a bridge site, with the pyrène plane perpendicular to the terminal surfaces. The fully optimized geometries of the six junctions are illustrated in figure 1.

The corresponding I–V characteristics and zero-bias transmission spectra are shown in figure 2. The relatively low conductances calculated for the four PDT junctions are in agreement with the previously predicted transport properties of pyrène and its oligomers between gold electrodes [4–7]. The associated transmission spectra display familiar features: a broad peak below the Fermi energy and another peak above, well separated by a sizable gap. The two peaks representing the most important occupied and unoccupied electron transmission channels are characteristic for aromatic wires (see, e.g., figure 5 in [24]), and they typically originate from the frontier molecular orbital, highest occupied (HOMO) and lowest unoccupied (LUMO), levels. In the case of the 1,6-PDT junctions, however, the symmetry prevents these from establishing an effective coupling with the electrodes. The most relevant frontier MOs with an out-of-plane π character, from the third highest occupied (HOMO−2) to the third lowest unoccupied (LUMO + 2), are illustrated in figure S1 in the supplementary data (available at stacks.iop.org/JPhysCM/25/275301/mmedia). Both the HOMO and LUMO are antisymmetric with respect to the mirror plane π, perpendicular to the molecular plane. Consequently, their orbital weights on the central column of atoms are zero. Hence, the single thiol groups, also situated on the axis, can at best provide a weak, through space, coupling of these MOs to the contacts. Thus, these two most important MOs do not make a substantial contribution to the transmission. In contrast, the second HOMO (HOMO−1), which is nearly degenerate with the HOMO, and the second LUMO (LUMO+1), are both symmetric, they exhibit an excellent conjugation across the whole backbone and provide the dominant contribution to the conductance of 1,6-PDT. Other frontier MOs suffer from either a poor conjugation on the C backbone (e.g. HOMO−2), or zero orbital weights on terminal thiols, or both (e.g. LUMO+2). The 2,7-PDT isomer exhibits a much better conjugation for all the frontier MOs, in particular the HOMO and LUMO, as shown in figure S2 (available at stacks.iop.org/JPhysCM/25/275301/mmedia). The MO densities of 3,8-PDT, shown in figure S3 (available at stacks.iop.org/JPhysCM/25/275301/mmedia), generally display very similar characteristics to

1 See supplementary data (available at stacks.iop.org/JPhysCM/25/275301/mmedia) at URL http://iopscience.iop.org for the plots of the orbital density of the frontier MOs of 1,6-PDT, 2,7-PDT, 3,8-PDT, 2,8-PDT, 1,2,5,7-PTT and 2,3,7,8-PTT. The electronic states in the ~1.5 to 2.0 eV interval for the 2,3,7,8-PTT junction, whose energies are labeled with blue triangles in the bottom panel of figure 2 are also shown therein.
Figure 1. The optimized geometries of the PDT and PTT derivatives between the Au(001) terminals.

Table 1. Calculated HOMO and LUMO energy levels and the energy gap between them for the five pyrene derivatives, given in eV.

<table>
<thead>
<tr>
<th></th>
<th>1,6-PDT</th>
<th>2,7-PDT</th>
<th>3,8-PDT</th>
<th>2,8-PDT</th>
<th>1,2,6,7-PTT</th>
<th>2,3,7,8-PTT</th>
</tr>
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<tbody>
<tr>
<td>HOMO</td>
<td>-5.388</td>
<td>-3.087</td>
<td>-5.287</td>
<td>-5.063</td>
<td>-5.127</td>
<td>-4.701</td>
</tr>
<tr>
<td>Gap</td>
<td>2.319</td>
<td>2.095</td>
<td>2.255</td>
<td>2.071</td>
<td>2.069</td>
<td>1.833</td>
</tr>
</tbody>
</table>

...those of 2,7-PDT. Consequently, their transmission spectra in figure 2 show the same features, although with more subdued amplitudes in the case of 3,8-PDT. The first occupied peak below the Fermi level is particularly attenuated for 3,8-PDT, which is the consequence of the 0.2 eV lower HOMO energy than that of 2,7-PDT, given in table 1. The predicted transport properties and frontier MO density and energy levels of the meta 2,8-PDT isomer bear even more resemblance to those of 2,7-PDT (MO densities are shown in figure S4 available at stacks.iop.org/PhysCM/29/275301/mmedia). In general, it is evident that all four PDT isomers exhibit similar conductance channels and, unsurprisingly, similar current magnitudes are predicted in the low bias regime.

Combining the individual benefits of 1,6-PDT and 2,7-PDT, as in the case of 1,2,6,7-PTT, yields somewhat improved characteristics, in particular for the HOMO, which exhibits a high orbital density on all the terminal thiols, shown in figure S3 (available at stacks.iop.org/PhysCM/29/275301/mmedia). As a consequence, the occupied peak just below the Fermi level in the 1,2,6,7-PTT transmission...
Figure 2. Upper panel: current versus bias voltage for the six pyrene junctions as calculated from the LDA (ASIC uncorrected). Lower panels: the zero-voltage transmission probability across these junctions. The blue triangles in the bottom panel indicate the Γ point energies of the electronic states that give rise to the transmission continua. The energy is given relative to the Fermi level.

For the other pyrene derivatives. Contrary to the spectra of the other four derivatives, the transmission coefficient of the 2,3,7,8-PTT, in the bottom panel of figure 2, displays qualitatively very different characteristics. The conductance gap, prominent in all the other spectra, has completely disappeared and so have the distinct peaks. In contrast, this spectrum exhibits a flat continuum of highly conducting channels in the relevant energy interval of ±1 eV from the charge neutrality point. Consequently, the associated I-V characteristics demonstrates a very high conductance, nearly independent of the bias voltage. The transport properties of 2,3,7,8-PTT suggests that this junction utilizes numerous electronic states whose energies are close to the Fermi level. Given the flat transmission spectrum in this energy range, it is not possible to single out particularly prominent states that give rise to highly conductive transport channels. Instead, one can identify the important MOs by considering orbital density distribution (at the zone center) of the electronic states whose energy is near the Fermi level and with a strong orbital conjugation across the entire junction, i.e., the gold electrodes, the thiol head groups, and the carbon backbone. This analysis reveals about a dozen of relevant electronic states in the ±1 eV interval, most of which have an out-of-plane π character. The Γ-point energies of the electronic states that give rise to the conducting channels are indicated by blue triangles in the bottom panel of figure 2. The corresponding orbital plots of these are shown in figure S7 (available at stacks.iop.org/JPhysCM/25/275301/mmedia). The large number of these states, with strong coupling between gold and PTT, manifested by the high degree of dispersion away from the zone center, give rise to the continuous flat transmission spectrum.

The potential of pyrene for the high, bias-independent conductance has, until the present work, remained elusive [4–7]. The significance of the present findings is to show how even the smallest PAH with a two-dimensional hexagonal mesh, pyrene, still inherits the highly desirable charge transport properties of graphene. A further consideration of the structural relationship between pyrene and extended graphene meshes provides probably the clearest explanation of the remarkably good conductance of 2,3,7,8-PTT. The 2,3,7,8-PTT motif can be extended into two series of graphene nanoribbons (GNRs). The first way generates a class of zigzag GNRs conventionally labeled 3-zGNR [25], while the alternative produces an armchair, 6-aGNR, series. Both 3-zGNR and 6-aGNR are illustrated in figure 3. In line with previous predictions from both tight binding [2, 25] and first principles [26, 27] calculations, the computed band structure in figure 3 indicates that the 3-zGNR is a quasi semimetal with a near zero band gap, while the 6-aGNR is a semiconductor with a sizable direct band gap. However, for finite length nanoribbons both series will exhibit substantial HOMO-LUMO gaps, as shown in figure 4. Hence, it is interesting to evaluate the conductance of both the series as a function of length. The results may also provide useful information on what series would be more suitable as molecular interconnects in nanosize devices.

The I-V characteristics and zero-bias transmission coefficients for wires from the 3-zGNR class with four (4R),
eight (8R), twelve (12R), sixteen (16R) and twenty (20R) rings are shown in figure 5. Several favorable observations can be made. Firstly, very high current levels are predicted for all the wires, with no visible variation with the length. Secondly, all the $I-V$ characteristics are linear, resulting in a high conductance which is independent of either length or bias voltage across the series. Hence, the contacts are providing the key contribution to the total resistance. The transmission spectra for 4R and 8R exhibit a continuum of channels with high transmission probabilities over a large energy range. In contrast, for the longer members, 12–20R, the spectra show an increasingly rich peak structure, reflecting the importance of the delocalized out-of-plane $\pi$ electronic states for the long range transport. The bottom panel in figure 5 demonstrates a high degree of correlation between the projected density of states (PDOS, out-of-plane contribution) on two representative C atoms, situated along the nanoribbon edge and in the central row, and the transmission spectrum. The two sharp peaks in the 12–20R spectra, on each side of the Fermi energy, arise from the HOMO and LUMO and make the key contribution to the low bias conductance. Finally, the inclusion of the ASIC results in a slight reduction of the conductance for all wires. Qualitatively though, the ASIC corrected results are in excellent agreement with their uncorrected counterparts.

The $I-V$ characteristics and zero-bias transmission coefficients for wires from the 6-aGNR class with four (4R), eight (8R), twelve (12R), sixteen (16R) and twenty (20R) rings are shown in figure 6. In contrast to their 3-aGNR counterparts, an attenuation of the current with length is evident across the entire bias range. An inspection of the low bias conductance, shown in figure 7, reveals an exponential dependence on nanoribbon length. From a least squares fitting procedure a rather low attenuation factor $\beta$ of 0.125 Å$^{-1}$ is obtained for this series. As expected, the application of the ASIC produces an increasingly wider energy gap between the occupied and unoccupied channels in the transmission spectra. As a consequence, the relatively high uncorrected conductance of the shorter members 4–12R is substantially reduced. For 16R and 20R, which show sizable gaps even...
in the uncorrected spectra, the effects of the ASIC appear marginal.

Most commonly the conjugated aromatic wires exhibit an exponential decay, \( \exp(-\beta L) \), of the conductance with molecule length (\( L \)) [6, 28-30], which is consistent with the nonresonant tunneling mechanism or superexchange [31]. This behavior, predicted for 6-aGNRs in the present work, can be understood in terms of Simmons’ model [28, 31]. In the molecular junctions for which the frontier MO energy levels remain sufficiently separated from the Fermi energy the factor \( \beta \) itself will not exhibit a large variation with length. This is exactly the case with the HOMO and LUMO levels of the 6-aGNRs series, as shown in figure 4. In contrast, as the same plot shows, the variation of these levels with molecule length for 3-zGNRs is too rapid to make a common factor \( \beta \) possible for this series. Hence, this simple relation no longer applies. Instead, the detrimental effects of nanoribbon length are fully compensated by the narrowing energy gap between the Fermi and frontier MO levels. Furthermore, as the spectrum in the bottom panel of figure 5 shows, for 20R (and, presumably, longer members beyond 20R) the low bias charge flow is practically resonant. The two peaks nearly coinciding with the Fermi level represent the highly conducting graphene electronic states with linear dispersion. Hence, the length independent trend is expected to continue for even longer members of this series. A similar length independent conductance, which is a signature of ballistic transport, has been observed in carbon nanotubes [32, 33].

4. Conclusions

The conductance of pyrene in various orientations with respect to the gold electrodes has been modeled using the NEGF approach combined with DFT calculations. The 2,3,7,8-tiolated form of pyrene has been found to have excellent charge transport properties, manifested by the high conductance virtually independent of bias voltage. Thus, it has been shown that the smallest of the 2D PAHs has the potential, previously overlooked, for use as a molecular wire. Based on the 2,3,7,8-PIT motif two series of short GNRs, 3-zGNR with zigzag and 6-aGNR with armchair edges, have been inspected as nanocircuit interconnects. The 3-zGNR set exhibits a conductance practically independent of the nanoribbon length and the bias voltage, making it an almost ideal wire. The semiconducting nature of the 6-aGNRs, combined with the nonresonant tunneling mechanism of charge transport, causes an exponential attenuation of conductance with the length.

The present findings indicate the importance of the multiple terminal groups for an optimal use of available electron transport channels and multiple conjugated pathways across the junction. The ballistic nature of charge transport through the 3-zGNRs shows that the contact points with gold are the principal source of resistance. The proposed dual terminal points not only substantially reduce the resistance, but in addition, provide a much more effective coupling to the gold electrodes and open up the multiple pathways of charge flow across the entire junction. Our results demonstrate
that with these PAHs and short GNRs can realize their full potential for charge transport applications.

Acknowledgments

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