Optical and magnetic-circular-dichroism—optically-detected-magnetic-resonance study of the Co\textsuperscript{2+} ion in LiGa\textsubscript{2}O\textsubscript{4}

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Optical and magnetic-circular-dichroism—optically-detected-magnetic-resonance studies have been carried out on Co-doped LiGa\textsubscript{2}O\textsubscript{4}. The Co ions are found to be predominantly in the 2+ charge state and to substitute for tetrahedrally coordinated Ga\textsuperscript{3+} in the LiGa\textsubscript{2}O\textsubscript{4} lattice, in sites which are shown to have C\textsubscript{3} point-group symmetry. The strong absorption bands from the ground state \textit{A}\textsubscript{1}(\textit{F}) to the excited states \textit{E}\textsubscript{1}(\textit{P}) and \textit{E}\textsubscript{1}(\textit{F}) are each split by the low-symmetry C\textsubscript{3} field. A combination of the low-symmetry field and spin-orbit coupling is responsible for the ground-state splitting of 19.5±0.5 cm\textsuperscript{-1} observed by fluorescence line narrowing. Strong broadband luminescence is observed from the \textit{E}\textsubscript{1}(\textit{P}) level to three lower levels, \textit{A}\textsubscript{1}(\textit{F}), \textit{E}\textsubscript{2}(\textit{F}), and \textit{E}\textsubscript{1}(\textit{F}), with a lifetime that is constant at 200 ns from 10 K up to room temperature. The optically-detected magnetic-resonance studies show that the Co\textsuperscript{2+} ions are in sites which have axial symmetry along (111)-type axes of the unit cell, indicative of the C\textsubscript{3} symmetry present in these substitutional sites. We give a detailed crystal-field model for the Co\textsuperscript{2+} ion in the C\textsubscript{3} site in LiGa\textsubscript{2}O\textsubscript{4} and deduce the crystal-field parameters from our experimental data.

I. INTRODUCTION AND BACKGROUND

When cobalt (Co) is added as a dopant to wide band-gap oxide materials, they acquire a characteristic color due to electronic transitions on the Co ions in the visible region of the spectrum. The cobalt ions are generally found in the 2+ and 3+ charge states in these oxide hosts. In 1961, Pappalardo, Wood, and Linares\textsuperscript{1} carried out a study of the spectroscopic properties of cobalt in a number of oxide crystals. They investigated cobalt doping of MgO and ZnO, which offer full octahedral and tetrahedral symmetry for the dopant Co ions, respectively. These are therefore ideal test systems to establish the spectroscopic properties of dopant Co ions in oxide materials. The simplicity of the observed spectra allowed Pappalardo \textit{et al.}\textsuperscript{1} to perform a detailed crystal-field analysis of the spectra. These researchers also carried out investigations of cobalt-doped spinel (MgAl\textsubscript{2}O\textsubscript{4}) and YAG (Y\textsubscript{3}Al\textsubscript{5}O\textsubscript{12}), each of which offer both tetrahedral and octahedral environments for the dopant Co ions. On the basis of the work in MgO:Co\textsuperscript{2+} and ZnO:Co\textsuperscript{2+}, they found that their spinel and YAG samples were dominated by Co\textsuperscript{2+} spectra and that, given a choice, the Co\textsuperscript{3+} ions greatly preferred tetrahedral to octahedral coordination in these materials. A subsequent study of Co absorption spectra in garnet hosts was carried out by Wood and Remeika\textsuperscript{2} in 1967. The observed spectra were ascribed to Co\textsuperscript{2+} and Co\textsuperscript{3+} ions, mainly in distorted tetrahedral environments. The tetrahedral Co\textsuperscript{3+} spectrum observed in the garnet material YAG is dominated by a broad double-peak band centered near 9000 cm\textsuperscript{-1}. On the other hand, the tetrahedral Co\textsuperscript{2+} spectrum in YAG shows three absorption regions. The strongest absorption occurs in the visible peaking near 16 000 cm\textsuperscript{-1}, giving the YAG:Co samples a characteristic blue color, and two absorption bands occur in the near infrared, peaking at 7100 and 4700 cm\textsuperscript{-1}.

The material LiGa\textsubscript{2}O\textsubscript{4} crystallizes with the spinel (MgAl\textsubscript{2}O\textsubscript{4}) structure, which is adopted by a large number of compounds whose general formula is \textit{XY\textsubscript{2}}O\textsubscript{4}. In general, two types of spinel are distinguished: "normal" and "inverse," and the cube in Fig. 1 represents the unit cell of normal spinel. For convenience, the cell is divided into octants, and the arrangements of ions in two of the octants are shown. These arrangements are repeated in alternate octants. The octahedral and tetrahedral sites may be distinguished in this figure. Whereas in normal spinel the octahedral and tetrahedral sites are occupied by trivalent and divalent ions, respectively, in inverse spinel one-half of the trivalent ions occupy tetrahedral sites while the other half, together with the divalent ions, occupy octahedral sites, and the structure can be represented by the formula \textit{Y}(\textit{XY})\textsubscript{2}O\textsubscript{4}.

The LiGa\textsubscript{2}O\textsubscript{4} arrangement is a variation of the inverse
spinel structure and contains 4 formula units in the cubic cell shown in Fig. 1. The monovalent Li\(^+\) ions and three-fifths of the Ga\(^{3+}\) ions are distributed among the octahedral sites in an ordered manner so that each row of octahedral ions in a \(<110>\) type direction contains a lithium ion in every fourth position. This distribution of Li ions results in the arrangement shown in Fig. 2 for the second-nearest-neighbor shell of cations about a gallium ion in the tetrahedrally coordinated site. The nearest-neighbor oxygen ions are not shown. The Li ions are arranged symmetrically about the \(<111>\) direction of the cell. This arrangement of the Li ions means that the site symmetry for the tetrahedrally coordinated Ga\(^{3+}\) ions is reduced from \(T_d\) to \(C_3\), and, as we will see later, the Co\(^{2+}\) ions substitute for Ga\(^{3+}\) at these sites in LiGa\(_2\)O\(_8\). There are four possible inequivalent Co\(^{2+}\) sites in the unit cell, with \(C_3\) axes along \(\langle 111\rangle\) type directions. The crystal structure of LiGa\(_2\)O\(_8\) has been described in detail by Gorter.\(^4\)

In the past, extensive optical spectroscopic studies have been carried out on Cr\(^{3+}\), Mn\(^{4+}\), Fe\(^{3+}\), and Ni\(^{2+}\) ions in LiGa\(_2\)O\(_8\).\(^5\)\(^-\)\(^9\) In this study we have combined optical and magnetic-circular-dichroism–optically-detected-magnetic-resonance (MCD-ODMR) spectroscopies to obtain a detailed account of the electronic structure and environment of the Co\(^{2+}\) ion in LiGa\(_2\)O\(_8\). The experimental results are consistent with the \(C_3\) site symmetry expected for substitutional Co\(^{2+}\) in the tetrahedrally coordinated sites in this material. A crystal-field model is developed for the Co\(^{2+}\) ion in LiGa\(_2\)O\(_8\), and values for the crystal-field parameters are derived from the data.

II. EXPERIMENTAL DETAILS

The luminescence and excitation measurements were carried out in an Air-Products flow cryostat with temperatures in the range 10–300 K. An Aviv spectrophotometer was used for the absorption experiments along with a cold-finger cryostat with liquid-N\(_2\) cooling. For the luminescence work, an Ar\(^+\) laser with 100-mW power at 514.5 nm was employed. The excitation spectra were recorded using a cw dye laser with DCM or RG6 as the active dye medium. Both photomultipliers (with S20 and GaAs photocathodes) and a liquid-N\(_2\)-cooled Ge detector were used to monitor the light signals.

The MCD and ODMR experiments are illustrated in Fig. 3. In this illustrative example, the ground and excitation...
ed states are spin doublets, and these are each split into
two by the magnetic field. The two circularly polarized
absorption transitions, $\sigma_L$ and $\sigma_R$, are shown. These are
transitions in which the light travels along the direction of
the magnetic field. The oscillator strength of the two transitions
are equal, but the absorption strength will depend
on the populations in the ground-state sublevels. In
this case, where there is a greater population in the lower
level, in accordance with the Boltzmann formula, then
$\sigma_L$ will be greater than $\sigma_R$ and the MCD signal, which is
proportional to $\sigma_L - \sigma_R$, will be nonzero.

If now the sample is irradiated with microwave power
at a frequency corresponding to the Zeeman splitting of
the ground state, this will tend to equalize the populations
in the two levels and there will be a decrease in the
MCD signal. Thus, the ground-state resonance condition
shows up as a change in the optical signal and this consti-
tutes the optically-detected-magnetic-resonance signal.

The MCD-ODMR experiments were carried out at
1.6 K in an Oxford Instruments SM-3 superconducting
magnet cryostat. The sample was mounted at the center
of a 35-GHz TE_{011} microwave cavity having optical ac-
cess. A Hinds SM-3 quartz modulator produced alternating
left and right circularly polarized light at 50.3 kHz.
The MCD signals were detected using both Si and Ge
detectors combined with standard lock-in techniques.
For the ODMR experiments, ~50 mW of microwave
power was introduced into the cavity. For the case in
which the absorption coefficients $\sigma_L$ and $\sigma_R$ are small,
the MCD signal is given by

$$MCD = (\sigma_L - \sigma_R) \propto (I_L - I_R),$$

where $I_L$ and $I_R$ are the transmitted intensities for left
and right circularly polarized light.

The samples of LiGa$_5$O$_8$ used in this study were grown
by the flux method, and the dopant cobalt ions exhibit
two zones of concentration in the material: a deep blue
core and an outer pale blue region. Electron microprobe
measurements of the cobalt concentration in one sample
gave 0.5% in the core and 0.12% in the pale area. All
measurements were carried out on samples cut from the
lightly doped region. For the magnetic resonance experi-
ments a small sample (dimensions 1 mm x 1 mm x 1.5
mm) was cut so that it could be positioned in the
microwave cavity with the magnetic field in the (01\overline{1}) plane.

III. EXPERIMENTAL RESULTS

The LiGa$_5$O$_8$:Co$^{2+}$ system shows two regions of strong
absorption, and their spectra recorded at 85 K are shown
in Fig. 4. These spectra show a very strong similarity to
those of Co$^{2+}$ ions in tetrahedrally coordinated environ-
ments in Y$_3$Al$_5$O$_{12}$ and ZnAl$_2$O$_4$. A Tanabe-Sugano
energy level diagram for the lowest energy levels of a $d^7$
ion in a tetrahedral crystal field is also given in Fig. 4,
and we assign the visible absorption band to the $^4A_2(4F) \rightarrow ^4T_1(4P)$ transition and the infrared band to
the $^4A_2(4F) \rightarrow ^4T_1(4F)$ transition. A third absorption
transition due to the $^4A_2(4F) \rightarrow ^4T_2(4F)$ transition, ex-
pected to lie in the region of 4000 cm$^{-1}$, could not be
detected even in samples with nominal Co concentration
of 1%. The weak band in Fig. 4 with a zero-phonon line
at 13 580 cm$^{-1}$ is tentatively assigned to Co$^{3+}$ in the
tetrahedral coordinatorate site in LiGa$_5$O$_8$ by comparison
with previous studies of Co-doped Y$_3$Al$_5$O$_{12}$.

On inspection of Fig. 4 we see that both absorption
bands are split; the band in the visible has two broad
components at 15 400 and 16 600 cm$^{-1}$, while the band in

![FIG. 4. The absorption spectrum of LiGa$_5$O$_8$:Co$^{2+}$ recorded at 85 K showing the $^4A_2(4F) \rightarrow ^4T_1(4P)$ and the $^4A_2(4F) \rightarrow ^4T_1(4F)$ transitions. The inset shows a Tanabe-Sugano energy-level scheme for Co$^{2+}$ in LiGa$_5$O$_8$. The absorption transitions are indicated on the energy-level scheme.](image)
the near infrared has two broad components at 7210 and 6300 cm$^{-1}$. A similar splitting was observed by Wood and Remeika in the corresponding Co$^{2+}$ spectra in YAl$_3$O$_{12}$.

Using Ar$^+$ laser excitation at 514.5 nm, three luminescence transitions are observed and the complete luminescence spectrum at 20 K and room temperature are shown in Fig. 5. This spectrum was recorded using a Ge detector and is not corrected for the system response. We note that, as the Ge detector has a poor response in the visible, the first luminescence transition in the red is much stronger than the other two. The zero-phonon line of the first luminescence transition at 15 157 cm$^{-1}$ recorded at 15 K coincides with the first sharp peak of the visible absorption band in Fig. 4. All three luminescence bands of Fig. 5 are found to have the same excitation spectrum [recorded at 15 K and shown in Fig. 6(a)] and the same lifetime. Therefore, these are assigned to transitions originating on the same $^4T_1(4P)$ level. The red luminescence is the $^4T_1(4P)$ $\rightarrow$ $^4A_2(4F)$ transition (see the energy-level diagram in Fig. 4) while the two near-infrared luminescence transitions in Fig. 5 are assigned to the

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The sharp dip in the MCD signal at 566 nm is ascribed to a Fano antiresonance effect.
FIG. 8. (a) The \( ^4A_2(^4F) \rightarrow ^4T_1(^4F) \) absorption transition recorded at 85 K. (b) The wavelength dependence of the MCD signal for the \( ^4A_2(^4F) \rightarrow ^4T_1(^4F) \) transition recorded at 1.6 K.

FIG. 9. The magnetic-field dependence of the MCD signal along the (a) [100], (b) [111], and (c) [011] directions recorded at the arrowed wavelength position (1400 nm) in Fig. 8. For comparison, the scaling of the y axis for the three signals is the same. The dips and peaks in the spectra are due to ODMR transitions. Note the “positive” ODMR transition for the [111]-oriented spectrum.

\[ ^4T_1(^4P) \rightarrow ^4T_2(^4F) \] and \[ ^4T_1(^4P) \rightarrow ^4T_1(^4F) \] transitions, respectively. The lifetime of all the luminescence bands at 10 K was found to be 200±20 ns. This lifetime is constant up to room temperature within experimental error.

The red luminescence transition, recorded in greater detail at 15 K, is shown in Fig. 6(b) along with the luminescence excitation spectrum in Fig. 6(a). The two spectra in Fig. 6 are clearly mirror images of one another except for the features marked x, y, and z in the excitation spectrum. The frequencies (with respect to the zero-phonon line at 15157 cm\(^{-1}\)) of all the fine-structure features in the spectra of Fig. 6 are given in Table I. The extra fine-structure lines in the excitation spectrum are at 46, 63, and 277 cm\(^{-1}\) from the zero-phonon line position.

In Figs. 7 and 8 we present the MCD spectra recorded at \( B = 1.64 \) T and \( T = 1.6 \) K for the LiGa\(_2\)O\(_4\):Co\(^{2+}\) system along with the corresponding absorption transitions at \( T = 85 \) K. The MCD spectra have not been corrected for the system response. The MCD band in Fig. 8(b) contains a great wealth of fine structure at this temperature, even more than is evident at 85 K in the absorption spectrum in Fig. 8(a). In the MCD spectrum of Fig. 7(b) there is a rather interesting feature at 566 nm. It is seen to be a “dip” in the MCD signal at this point. This feature is also observed as a dip in absorption strength in the absorption spectrum of Fig. 7(a).

The magnetic field variation of the MCD signal taken at \( \lambda = 1400 \) nm along the [100], [111], and [011] directions is shown in Fig. 9. We note that the intensity of the MCD signal is not isotropic, as it would be if the Co\(^{2+}\) ion was at a site of full \( T_d \) symmetry. We find instead that it shows a maximum along the [111] direction [Fig.
suggesting an axis of symmetry along this direction. In this figure we also show the ODMR transitions, identified as peaks and dips in the MCD signals. It is interesting to note that the high-field ODMR transition along [111] shows an increase in the strength of the MCD band.

The angular variation of the $\text{Co}^{2+} \text{ ODMR transitions}$ with the magnetic field $B$ in the (011) plane is shown in Fig. 10. The solid points are due to ODMR transitions which show an increase in the total MCD signal (positive ODMR), and the open points are due to transitions which show a decrease in the MCD signal (negative ODMR). The “positive” ODMR signal is strongest along [111] and weakens quickly as the crystal is rotated towards either the [100] or [011] direction. The splitting of the ODMR lines near [100] is due to a small misalignment ($\sim 2^\circ$) of the LiGa$_2$O$_4$:Co$^{2+}$ crystal; the small size of the sample makes alignment difficult.

IV. CRYSTAL-FIELD MODEL

In this section we describe our crystal-field model for the $\text{Co}^{2+}$ center in LiGa$_2$O$_4$. This model includes a full treatment of the $C_3$ crystal field which acts upon the $\text{Co}^{2+}$ ion. We start with the electron-electron interaction, and then include the crystal-field interaction. Lastly, we consider the spin-orbit interaction, which gives rise to a splitting of the ground state. This leads to an expression for the fine-structure parameter $D$ for the ground state.

A. Electron-electron interaction

The $\text{Co}^{2+}$ impurity in LiGa$_2$O$_4$ has the $d^7$ configuration, which we treat as a three-hole configuration. In accordance with Hund’s rule, the ground-state term is a $^4F$ term. There is a second spin quadruplet, a $^4P$ term. In the case of a free $\text{Co}^{2+}$ ion, the $^4P$ term is the first excited term, lying approximately 15 500 cm$^{-1}$ above the ground term. The $^4P$-$^4F$ splitting is reduced for the case of the $\text{Co}^{2+}$ impurity in crystals, as a result of the greater extent of the wave functions when the ion is in a crystalline environment. We denote the $^4P$-$^4F$ splitting, which can be expressed in terms of the Racah parameter $B$, by the single parameter $\Delta$.

B. Crystal-field interaction

1. $T_d$ component

We decompose the crystal-field potential into two components, which we treat separately. The first component is a field of $T_d$ symmetry, resulting primarily from the first shell of neighbors that consists of four oxygen ions in tetrahedral coordination with the $\text{Co}^{2+}$ as shown in Fig. 1. In addition, the third shell of neighbors consists of four gallium ions also in tetrahedral coordination about the $\text{Co}^{2+}$ ion. These gallium ions are located in the corners of the left-hand octant in Fig. 1. The tetrahedral crystal field splits the one-hole $d$ states so that the $t_{2g}$ symmetry holes are lower in energy than the $e$-symmetry holes by an amount $10Dq$. The partial removal of the fivefold degeneracy of the $d$ states splits the $^4F$ term into three manifolds: $^4A_2$, $^4T_2$, and $^4T_1(4P)$. The $^4P$ term spans the manifold $^4T_1(4P)$. These splittings are shown in Fig. 11, which indicates schematically the effect of various perturbations on the $\text{Co}^{2+}$ ion in LiGa$_2$O$_4$. The many-hole ($M = \frac{3}{2}$) states for these manifolds are given by

$$^4A_2 = (\xi, \eta, \zeta),$$

$$^4T_2 = (\epsilon, \eta, \zeta),$$

$$^4T_{14}(4P) = 1/\sqrt{5}[2(\xi, \eta, \theta) + 2(\xi, \eta, \epsilon)],$$

$$^4T_{12}(4P) = 1/\sqrt{5}[2(\xi, \eta, \theta) - (\zeta, \zeta, \epsilon)],$$

(2)

where $(X_1, X_2, X_3)$ denotes the Slater determinant of the orbitals $X_1$, $X_2$, and $X_3$. In addition, the tetradedral crystal field gives rise to a mixing between the $^4T_1(4F)$ and $^4T_1(4P)$ manifolds, resulting in the repulsion of these levels, as shown in the middle of Fig. 11.

2. $C_3$ component

The second component of the crystal-field potential is a component of $C_3$ symmetry. The second shell of neighbors around the $\text{Co}^{2+}$ impurity consists of nine gallium ions and three lithium ions arranged as shown in Fig. 2. If all the ions in the second shell were identical, i.e., gallium ions in this case, then the site symmetry would be $T_d$. It is the three lithium ions that are responsible for lowering the symmetry to $C_3$. Contrary to a note by Macfarlane, there is a distinction between $C_3$ and $C_{3v}$ potentials, though, like the $C_{3v}$ potentials, the $C_3$ potential splits each orbital triplet into an orbital singlet and an orbital doublet. We consider an expansion of the potential in terms of spherical harmonics. The linear combination of $L = 4$ spherical harmonics (neglecting the $M = 0$ har-
monic) which describes a $C_{3v}$ potential is $(Y_{43} - Y_{4-3})$, which is proportional to $\cos(3\phi)$, where $\phi$ is measured about the three-fold axis with $\phi = 0$ defining one of the three reflection planes. Reflections through these planes change $\phi$, but not $\cos(3\phi)$. In lowering the symmetry to $C_3$, an additional term must be added to the potential and this term does not remain unchanged with reflections through these three planes but retains the three-fold rational symmetry. The linear combination $(Y_{43} + Y_{4-3})$, which is proportional to $\sin(3\phi)$, is such a term. This additional term is the distinction between the $C_{3v}$ and the $C_3$ potentials.\(^{14}\)

We write the one-electron $C_3$ potential within $d$ states in terms of operators which span irreducible representations of the $T_d$ point group. We find

$$V_{C_3} = \alpha A_1 + V(T_{2g} + T_{2\eta} + T_{2\xi}) + W(T_{1x} + T_{1y} + T_{1z})$$

$$(3)$$

where $\alpha$, $V$, and $W$ are constants. Analytic expressions for these constants can be derived, for example, by assuming a point-ion model. However, we proceed by treating these as parameters. We note that it is the last term in Eq. (3) which distinguishes this potential from one of $C_{3v}$ symmetry. We define the following reduced matrix elements for $i,j = \xi, \eta, \zeta$ and $k = \theta, \epsilon$:

$$\langle t_{2i} | V_{C_3} | t_{2j} \rangle = \alpha_t$$

$$\langle e_k | V_{C_3} | e_k \rangle = \alpha_e$$

$$\langle t_{2i} | V_{C_3} | e_k \rangle = u / \sqrt{3} \delta_{ij} \quad (i \neq j)$$

$$\langle t_{2\xi} | V_{C_3} | e_\theta \rangle = \sqrt{2/3} v'$$

$$\langle t_{2\xi} | V_{C_3} | e_\epsilon \rangle = \sqrt{2/3} w$$

$$\langle t_{2\xi} | V_{C_3} | e_\eta \rangle = \sqrt{2/3} w'$$

$$\langle t_{2\xi} | V_{C_3} | e_\zeta \rangle = \sqrt{2/3} w''$$

$$\langle t_{2\xi} | V_{C_3} | e_\theta \rangle = \sqrt{2/3} v'$$

$$\langle t_{2\xi} | V_{C_3} | e_\epsilon \rangle = \sqrt{2/3} w'$$

$$\langle t_{2\xi} | V_{C_3} | e_\eta \rangle = \sqrt{2/3} w''$$

$$(4)$$

The parameters $\alpha_t$ and $\alpha_e$ give a contribution, in addition to that of the tetrahedral component of the crystal field, to the splitting of the $t_{2g}$ and $e$ holes. We therefore incorporate this additional contribution into the parameter $10Dq$. The parameters $v$ and $v'$, which result from the $T_{2g} + T_{2\eta} + T_{2\xi}$ operator, are defined following Macfarlane.\(^{15}\) The parameter $w$ results from the $T_{3x} + T_{1y} + T_{1z}$ operator, and so does not appear as a parameter for a $C_{3v}$ potential. Using these parameters and Eq. (3) in conjunction with the Wigner-Eckart theorem, we have exactly prescribed the one-hole matrix elements of a $C_3$ potential within a basis of $d$ holes. The nature of this potential is better understood if we make a change of basis for the $t_{2g}$ states that reflects the axial nature (111-type directions) of the $C_3$ potential. Consider the basis set defined by

$$t_{2g} = 1/\sqrt{3}(t_{2\xi} + t_{2\eta} + t_{2\xi})$$

$$t_{2i} = 1/\sqrt{6}(2t_{2\xi} - t_{2\eta} - t_{2\eta})$$

$$t_{2e} = 1/\sqrt{2}(t_{2\xi} - t_{2\eta})$$

In the basis set of $d$ states ($t_{2g}$, $t_{2i}$, $t_{2e}$, $e_i$, $e_e$), the one-hole matrix elements of the $C_3$ potential are

$$\begin{bmatrix}
2\nu / 3 & 0 & 0 & 0 & 0 \\
0 & -\nu / 3 & 0 & v' & w \\
0 & 0 & -\nu / 3 & -w & v' \\
0 & v' & -w & 0 & 0 \\
0 & w & v' & 0 & 0
\end{bmatrix}$$

$$\mathcal{H}_{C_3} =$$

$$(6)$$

From Eq. (6), we readily see the difference in how the $C_{3v}$ and $C_3$ potentials act within $d$ states. The parameter $v'$ mixes the $t_{2i}, t_{2e}$ states with $e_{\theta e}$ states in one sense, while the parameter $w$ mixes these states in the opposite sense.

The matrix elements of the $C_3$ potential taken between the many-hole states of the four manifolds prescribed in Eq. (2) are readily determined from the one-hole matrix elements given in the previous paragraph. This results in a $10 \times 10$ matrix. This matrix can be reduced in to a $4 \times 4$ block and a $6 \times 6$ block through a change of basis for the orbital-triplet manifolds like that given in Eq. (5). Within the basis set $\{^4A_2, ^4T_{1e}(^4F), ^4T_{2g}, ^4T_{1g}(^4P)\}$, the many-hole matrix elements of the full crystal-field interaction and the electron-electron interaction are

$$\begin{bmatrix}
-6G & I & -2J & 2I \\
I & 3G + 2L & -4K & -2G + 2N \\
-2J & -4K & -G + 2H & 2K \\
2I & -2G + 2N & 2K & F + 2M
\end{bmatrix}$$

$$\mathcal{H} =$$

$$(7)$$

Within the basis set $\{^4T_{1e}(^4F), ^4T_{1e}(^4F), ^4T_{2g}, ^4T_{1e}(^4P), ^4T_{1e}(^4P)\}$, the many-hole matrix elements of the crystal-field and electron-electron interaction are

$$\begin{bmatrix}
3G - L & 0 & 2K & -P & -2G - N & -J \\
0 & 3G - L & P & 2K & J & -2G - N \\
2K & P & -G - H & 0 & -K & -Q \\
-P & 2K & 0 & -G - H & Q & -K \\
-2G - N & J & -K & Q & F - M & 0 \\
-J & -2G - N & -Q & -K & 0 & F - M
\end{bmatrix}$$

$$\mathcal{H} =$$

$$(8)$$
The variables \( F, G, H, \ldots, Q \) given above are defined by
\[
F = \Delta, \quad L = 1/5(3v/2 + 2\sqrt{2}v'),
\]
\[
G = 2Dq, \quad M = 1/5(v - 2\sqrt{2}v'),
\]
\[
H = v/6, \quad N = 1/5(-v/3 + 3\sqrt{2}v'/2),
\]
\[
I = \sqrt{2}5v', \quad P = 1/\sqrt{3}(\sqrt{3}v/2 + \sqrt{2}v'),
\]
\[
J = w/\sqrt{2}, \quad Q = 1/\sqrt{3}(-v + v'/\sqrt{2}),
\]
\[
K = w/\sqrt{10}.
\]

From Eqs. (7) and (8), we can show that, as required by symmetry, the \( C_3 \) potential splits the orbital triplets into an orbital singlet and an orbital doublet, as shown in Fig. 11, and we can also show how the differences between the \( C_3 \) and \( C_{3v} \) potentials affect the mixing of the orbital triplets. Diagonalizing the matrices in Eqs. (7) and (8) yields the many-hole energy levels and eigenstates for the Co\(^{2+}\) impurity in the site of \( C_3 \) symmetry.

C. Spin-orbit interaction

The spin-orbit interaction has the effect of splitting in first order each of the orbital doublets into four Kramers doublets. (Note that \( S = \frac{3}{2} \).) In addition, the spin-orbit interaction in second order splits the orbital singlets into two Kramers doublets. We concentrate on the splitting of the \( ^4A_2 \) ground manifold.

The spin-orbit interaction mixes the \( ^4A_2 \) ground manifold with the \( ^4T_2 \) manifold. The many-hole matrix elements of the orbital angular momentum \( L \) taken between the states of these two manifolds is characterized by
\[
\langle T_2^i | L_2 | A_2 \rangle = 2i, \quad i = \sqrt{-1}.
\]

This matrix element is unchanged if we transform to the basis set for the \( ^4T_2 \) manifold defined by Eq. (5) and perform a similar transformation on the orbital momentum operators. For example, we define \( L'_2 \), by
\[
L'_2 = 1/\sqrt{3}(L_x + L_y + L_z),
\]
which yields
\[
\langle T_2^i | L'_2 | A_2 \rangle = 2i
\]
and similarly for \( T_2^0 \) and \( T_2^e \) with \( L'_2 \) and \( L'_y \), respectively.

We neglect for the moment the mixing of the \( ^4T_2 \) manifold with the other orbital-triplet manifolds, but consider only the splitting, due to the \( C_3 \) symmetry field, of this manifold into an orbital doublet, at an energy \( E_D \) above the \( ^4A_2 \) manifold, and an orbital singlet, at an energy \( E_S \) above the \( ^4A_2 \) manifold. The spin-orbit interaction between the \( ^4T_2 \) and \( ^4A_2 \) manifolds splits the \( ^4A_2 \) manifold into two Kramers doublets. One doublet is comprised of the \( M_s = \pm \frac{1}{2} \) states, the second of the \( M_s = \pm \frac{3}{2} \) states. The second-order energies of these two doublets are given by
\[
E(\pm \frac{1}{2}) = -3\lambda^2(3/E_S + 2/E_D),
\]
\[
E(\pm \frac{3}{2}) = -\lambda^2(1/E_S + 14/E_D),
\]
where \( \lambda \) is the many-electron spin-orbit parameter. For the free Co\(^{2+}\) ion, \( \lambda \) is approximately \(-180 \, \text{cm}^{-1}\). For the ion in a crystalline environment, \( \lambda \) is somewhat reduced (typically to 0.8 of the free-ion value) from this value.

The ground-state fine-structure parameter denoted \( D \) is a measure of the splitting between the two Kramers doublets within the ground \( ^4A_2 \) manifold. We now include the mixing of the \( ^4T_2 \) manifold with the other orbital-triplet manifolds. We define the fraction of the \( ^4T_2 \) wave function within the \( i \)th \((i = 1, 2, 3)\) orbital doublet to be \( \beta_i \), and the fraction of the \( ^4T_2 \) wave function in the \( i \)th orbital singlet (neglecting the \( ^4A_2 \)) to be \( \alpha_i \). We find then that \( D \) is given by
\[
D = \frac{1}{2}\left[ E(\pm \frac{1}{2}) - E(\pm \frac{1}{2}) \right] = 4\lambda^2 \left[ \sum_{i=1}^{3} \beta_i / E_D - \sum_{i=1}^{3} \alpha_i / E_S \right].
\]

Since the fine-structure splitting is large compared with the Zeeman splitting as measured here by ODMR, we can treat the two Kramers doublets resulting from the \( ^4A_2 \) manifold independently, with each doublet being described by an effective spin \( S' = \frac{1}{2} \). The effective-spin Hamiltonian for each of the doublets is
\[
\mathcal{H}_{\text{eff}} = \mu_B \mathbf{B} \cdot \mathbf{S}'
\]
The \( g \) tensor has two independent components: \( g_1 \) (along the three-fold axis) and \( g_2 \) (perpendicular to the three-fold axis). In first order, the \( g \) values in the \( \pm \frac{1}{2} \) manifold are \( g_1 = 3g_e \) (\( g_e = 2.0023 \)) and \( g_2 = 0 \). The \( g \) values in first order in the \( \pm \frac{3}{2} \) manifold are \( g_1 = g_e \) and \( g_2 = 2g_e \).

Departures of the experimental \( g \) values from these theoretical values within the \( M_s = \pm \frac{1}{2} \) manifold are explained using the usual second-order corrections involving the spin-orbit interaction and the orbital Zeeman interaction. As with the fine-structure splitting, the mixing with excited states involves the states of the \( ^4T_2 \) manifold. We find that
\[
g_\parallel = g_e - 8\lambda \sum_{i=1}^{3} \alpha_i / E_S,
\]
\[
g_\perp = 2 \left[ g_e - 8\lambda \sum_{i=1}^{3} \beta_i / E_D \right].
\]
The results in Eq. (16) have a similar form to those in Eq. (14). Indeed, we can relate the \( g \) values to the fine-structure parameter by
\[
g_\parallel / 2 - g_\perp = -2D / \lambda.
\]

V. ANALYSIS OF RESULTS AND DISCUSSION

We now proceed with the analysis of our experimental data in light of the theory developed in the previous section and of the assignments made for the observed optical transitions in Sec. III. We noted that both absorption transitions in Fig. 4 show a splitting into two bands; this splitting is due to the \( C_3 \) crystal field present at the Co\(^{2+}\)
site. The additional band with a peak at 18,200 cm\(^{-1}\) in Fig. 4 is most likely due to higher-lying levels arising from the \(^2G\) free-ion level as shown in the energy-lying diagram in Fig. 4.\(^{17}\) Values for \(\Delta\) and 10\(Dq\) can be estimated by fitting the average energies of the \(^4A_2(^4F) \rightarrow ^4T_1(^4P)\) and \(^4A_2(^4F) \rightarrow ^4T_1(^4F)\) transition. The experimental positions we choose for the fitting are at 6300, 7210 cm\(^{-1}\) for the \(^4A_2(^4F) \rightarrow ^4T_1(^4P)\) transition and 15400, 16600 cm\(^{-1}\) for the \(^4A_2(^4F) \rightarrow ^4T_1(^4P)\) transition. Choosing these positions is somewhat difficult due to the presence of much vibrational structure in these spectra. Values for \(v, v', w\) are then chosen and the matrices in Eqs. (7) and (8) are diagonalized iteratively until a good fit to the experimental positions is found. The following values are found from our analysis:

\[
\Delta = +10781 \text{ cm}^{-1}, \quad v = +1362 \text{ cm}^{-1}, \\
10Dq = +3770 \text{ cm}^{-1}, \quad v' = -10 \text{ cm}^{-1}, \\
w = \pm 20 \text{ cm}^{-1}.
\]

These values give an excellent fit to the experimental positions. Hund's rule requires that the ground state be the \(^4F\) term; so we require \(\Delta\) to be positive. The strong tetrahedral component of the crystal field, coming primarily from the four nearest-neighbor oxygen ions, determines the sign of 10\(Dq\). These oxygen ions are negatively charged. The lobes of the \(t_{2g}\)-symmetry hole orbitals are closer to the oxygen ions than the lobes of the \(e\)-symmetry hole orbitals. Hence, the \(t_{2g}\)-symmetry holes are lower in energy than the \(e\)-symmetry holes, making 10\(Dq\) positive. Setting the signs of these parameters we find that the signs of \(v\) and \(v'\) are determined to be positive and negative, respectively. The fit to the data is insensitive to the sign of \(w\). This fitting procedure suggests that, for each orbital triplet, the doublet is shifted down in energy and the singlet shifted up in energy by the \(C_3\) crystal field.

The positive sign of \(v\) is physically reasonable. In an ionic model, the gallium ions possess a \(+3e\) charge and the lithium ions a \(+1e\) charge. Hence, the perturbation potential resulting from the lithium ions is that of three negatively charged ions in a \(C_3\) symmetry configuration. The lobes of the \(t_{2g}\) hole orbital lie in a plane perpendicular to the \(C_3\) symmetry axis and the lobes of the \(t_{2g}\) and \(t_{2e}\) hole orbitals, are therefore closer to the lithium ions. Hence, these latter two orbitals have a lower energy than the \(t_{2g}\) orbital. Equation (6) therefore implies that \(v\) is positive.

The signs of \(v'\) and \(w\) are much harder to explain in physical terms. We note, however, that, in the point-ion model for this defect, \(v'\) is predicted to have a sign opposite to that of \(v\), and \(w\) is predicted to have the same sign as \(v\). We recall that the sign of \(w\) is not determined in our fit. In any event, both \(v'\) and \(w\) are found to be small in our case.

An interesting feature of this \(Co^{2+}\) system is the sharp dip observed at 566 nm in the absorption spectrum in Fig. 7(a) and in the MCD signal of Fig. 7(b). We believe that the dip is due to Fano antiresonance effect such as has been observed in \(K_{MgF_2}:V^{2+}\) and in \(Cr^{3+}\) doped glasses.\(^{18,19}\) Consulting the Tanabe-Sugano diagram for a \(d^2\) ion in tetrahedral symmetry,\(^{17}\) we find that there are a number of levels originating on the free-ion \(^2G\) level which are expected to lie in this general spectral region. We are unable to make any definitive electronic assignment for the antiresonance feature.

The width of the zero-phonon 15,157 cm\(^{-1}\) line of the \(^4T_1(^4P)\) level in luminescence is 24 cm\(^{-1}\) (full width at half maximum) at 15 K. A series of nonresonant fluorescence line narrowing (FLN) experiments were performed in order to investigate structure hidden within this large inhomogeneous profile. The detailed results of this investigation have been published elsewhere.\(^{20}\) From these FLN measurements, the ground-state splitting due to a combination of the \(C_3\) crystal field and spin-orbit coupling is 19.5 cm\(^{-1}\), from which we obtain \(D = 9.75\) cm\(^{-1}\).

The optical spectra in Figs. 4–8 show a considerable number of sharp-line features. As indicated above, each of the crystal-field levels is further split by spin-orbit coupling, the doublet into four components and the singlet into two components. As a result the \(^4A_2(^4F) \rightarrow ^4T_1(^4P)\) absorption spectrum in Fig. 4 should contain six electronic components among a large number of vibrational side bands. It is difficult to identify transitions to these electronic levels in the absorption spectra shown in Fig. 4 which were taken at 85 K. However, in the excitation spectrum of the \(^4T_1(^4P) \rightarrow ^4A_2(^4F)\) luminescence transition shown in Fig. 6(a), recorded at 15 K under much higher resolution, the features labeled \(x, y, z\) are clearly electronic as they are not observed in the corresponding luminescence spectrum. We tentatively identify the line at 15,157 cm\(^{-1}\) and the features at 46, 63, and 277 cm\(^{-1}\) above 15,157 cm\(^{-1}\) as the spin-orbit split components of the orbital doublet level coming from \(^4T_1(^4P)\). The possible presence of levels arising from the \(^2G\) free-ion level in this spectral region is a complicating factor making our identification rather tentative. The \(^4A_2(^4F) \rightarrow ^4T_1(^4F)\) transition in Figs. 4 and 8 is particularly rich in spectral features making identification of the six expected electronic components very difficult. Nevertheless, we can reasonably assign the lines at 6060 and 7140 cm\(^{-1}\) to electronic transitions.

The very fast radiative decay time of the luminescence transitions at low temperature indicates that these transitions have a strong electric dipole character and, consequently, have a large oscillator strength. This comes about because, in the tetrahedral site (in which the site symmetry is \(C_3\)), in \(LiGa_2O\(_3\)) the odd-parity crystal field mixes the 3d states of \(Co^{2+}\) with higher-energy states of opposite parity, and this mixing is responsible for the electric-dipole character of this transition. The lack of discernible change in the lifetime up to room temperature indicates the absence of a competing nonradiative decay process for this level and strongly suggests that the luminescence process is very efficient. The room-temperature luminescence spectrum in Fig. 5 shows three broadbands which have high luminescence efficiency. In contrast to both ZnO:Co\(^{2+}\) (Ref. 21) and ZnAl\(_2\)O\(_4\):Co\(^{2+}\) (Ref. 11), the luminescence bands in Fig. 5 originate on the \(^4T_1(^4P)\) level rather than the \(^2E\) level. From the
Tanabe-Sugano diagram\textsuperscript{17} we find that luminescence transitions originating on the $^4T_1(^4P)$ are very broad due to the sensitivity of the $^4T_1(^4P)$ level to the crystal-field environment. Luminescence transitions from the $^2E$ level consist of sharp lines due to its insensitivity to the crystal field. The three luminescence transitions observed in LiGa$_2$O$_4$:Co$^{2+}$ are also spin allowed, which contributes to their large oscillator strength. The combination of broad luminescence transitions coupled with a large oscillator strength makes LiGa$_2$O$_4$:Co$^{2+}$ an ideal candidate for a tunable solid-state laser in the visible and near infrared.

The “positive” ODMR lines in Figs. 9 and 10 are an interesting feature of these samples. We would intuitively feel that the ODMR transition should equalize the populations of the ground-state levels as illustrated in Fig. 3 and thereby cause a reduction of the MCD signals in Fig. 9. Along the [100] direction the four Co$^{2+}$ sites in the unit cell all make the same angle with the applied magnetic field $B$. We therefore see only a single ODMR transition as in Fig. 9(a). When the applied magnetic field is along the [111] direction, the four $\langle 111 \rangle$-type centers are no longer equivalent; the center aligned along the magnetic field is distinguished from the other three. In this case we expect to see two ODMR transitions as observed in Fig. 9(b). The low-field ODMR transition shows a reduction in the MCD signal as expected. On the other hand, the high-field ODMR transition appears to show an increase in the total MCD signal. The total MCD signal observed is a combination of the parallel MCD signal and the MCD signals from the other three centers. The MCD signal for the parallel center must therefore be opposite in sign to that from the other centers. For the example shown in Fig. 3, this would mean that the Zeeman splitting of the ground or excited states for the parallel center is opposite to that for the other three centers. We find that, as the magnetic field is rotated away from the [111] direction, the intensity of the “positive” ODMR lines weakens (Fig. 10) and eventually the ODMR lines become negative. This result is a further demonstration that the site occupied by the Co$^{2+}$ ion has an axis of symmetry along $\langle 111 \rangle$-type directions. Along the [111] direction the coupling between the Kramers doublets participating in the MCD signal with all the other Kramers doublets within the $d^7$ shell is at a minimum. Rotating the magnetic field $B$ away from $\langle 111 \rangle$ results in an admixture into the ground and excited states which eventually leads to a reversal of the Zeeman splitting as the magnetic field approaches the [100] and [011] directions (Fig. 10). This effect was also observed by Ahlers et al.\textsuperscript{22} for the $^{2}D_{5/2}(1)$ center in KCl. While this give a qualitative explanation for the observed effect, the microscopic origin for this reversal of the Zeeman splitting has not been determined.

The ODMR line positions in Fig. 10 can be fitted to the spin Hamiltonian in Eq. (15) with the two independent $g$ values, $g_x = 2.215$, $g_z = 4.628$. The fit to the experimental data is shown as the solid lines in Fig. 10. These $g$ values indicate that the observed ODMR transitions are within the $\pm \frac{1}{2}$ levels of the ground state and so the sign of the fine-structure parameter $D$ is positive from Eq. (14). As $g_{1/2} > g_{1}$, we are again led to the conclusion from Eq. (16) that the orbital doublets arising from the orbital triplet manifolds are lower in energy than the orbital singlets. At the low temperatures of the MCD-ODMR experiments the population of the $\pm \frac{3}{2}$ levels is very small and so no signals were observed in this doublet. From Eq. (17) we estimate the spin-orbit constant to be $\lambda = -193$ cm$^{-1}$. We can also estimate $\lambda$ from Eq. (14). In doing this we use the theoretical estimate for the positions of the $^4T_2$ doublet and singlet split levels and in this case we find $\lambda = -190$ cm$^{-1}$. Both values are quite similar but somewhat surprising as we would normally expect to see a reduction in $\lambda$ from the free-ion case.

Both the ODMR and the optical zero-phonon linewidths are quite broad. The ODMR linewidth is 20 mT and exhibits no resolved hyperfine structure associated with the $^{57}$Co nucleus (100% abundant) which has a nuclear spin of $I = \frac{3}{2}$. We noted earlier that the inhomogeneous optical zero-phonon transition linewidth is 24 cm$^{-1}$ so that the large ground-state splitting could not be resolved. The Co$^{2+}$ ion substitutes for Ga$^{3+}$ in the lattice and some charge compensation is thus required to maintain charge neutrality. Both of these broad linewidths are probably due to a distribution of positions for the charge compensating ions which would result in a distribution of strains at the sites of the substitutional Co$^{2+}$ ions in the LiGa$_2$O$_4$ lattice. At present we do not know what species is providing the charge compensation for the Co$^{2+}$. It is interesting to note that the behavior shown in Fig. 10 is consistent with the $C_3$ symmetry deduced from the crystal structure, and this would imply that either the charge compensating ion is far away from the Co$^{2+}$ ion or located along a $\langle 111 \rangle$-type direction.

VI. CONCLUSIONS

The optical spectra of Co$^{2+}$ in LiGa$_2$O$_4$ provide clear evidence that the Co$^{2+}$ ions substitute for tetrahedrally coordinated Ga$^{3+}$ ions in this lattice and therefore occupy sites of $C_3$ symmetry, as illustrated in Fig. 2. We have presented a detailed crystal-field model for the Co$^{2+}$ ion in this site, and we have deduced the crystal-field parameters. Strong luminescence with a lifetime of 200 ns is observed to three lower levels from the $^4T_1(^4P)$ level. In a previous publication this system was suggested as a possible candidate as a visible-infrared laser system.\textsuperscript{9} Further experiments to look at excited-state absorption effects would have to be undertaken to determine the potential of LiGa$_2$O$_4$:Co$^{2+}$ as a laser system. Within the accuracy of the ODMR experiment, the site symmetry of the Co$^{2+}$ ion is $C_3$, suggesting that charge compensating ions are either far removed from the Co$^{2+}$ or are along the $C_3$ axis.

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