Analysis of strain and intermixing in single-layer Ge/Si quantum dots using polarized Raman spectroscopy

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The built-in strain and composition of as-grown and Si-capped single layers of Ge/Si dots grown at various temperatures (460-800 °C) are studied by a comparative analysis of the Ge-Ge and Si-Ge modes in the polarized Raman spectra of the dots. A pronounced reduction of the strain and Ge content in the dots after deposition of the cap layer at low temperatures is observed, indicating that strain-induced Si diffusion from the cap layer is occurring. For large dots grown at 700-800 °C the observations are in agreement with a model of the Ge/Si dot consisting of a Si-rich boundary region and a Ge-rich core.

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I. INTRODUCTION

In recent years, a considerable amount of work has been devoted to the study of semiconductor self-assembled quantum dots (QD's) which can be successfully grown from III-V, II-VI, and Group-IV lattice-mismatched semiconductors using a Stranski-Krastanov growth technique. Ge/Si self-assembled QD's are of particular interest because of their compatibility with Si-based electronics. The growth of high-quality, Ge/Si, self-assembled QD's can be achieved by molecular beam epitaxy or chemical vapor deposition (see review in Ref. 2 and references therein).

The presence of strain and the specific chemical composition of semiconductor quantum dots has an enormous influence on their optical and electrical properties. Intense and, in some cases, anisotropic strain is essential for the growth of self-assembled and strain-induced quantum dots. 1,3 Strain results in a reconstruction of the electronic and vibrational structure of the quantum dots comparable to that induced by the quantum confinement effect. The interdiffusion of atoms surrounding the dot into the crystal lattice of the dot, the intermixing effect, is a crucial step in the formation of the nanostructure. This intermixing effect influences the shape and depth of the potential wells for electronic excitations, the elastic coefficients of the materials, and therefore their phonon spectra. Because of the small size of the dots, the change in composition caused by intermixing may be very large. As an example, the Si content in germanium dots embedded in a Si structure can increase by up to 70% as a result of intermixing.⁴ This raises the possibility of utilizing strain and composition effects in order to manipulate quantum dot parameters or to synthezise novel quantum dot structures. This has already been done for III-V quantum dots grown by droplet epitaxy.⁵ Knowledge of these parameters is of crucial importance for future optoelectronic applications of quantum dot nanostructures.

Ge/Si quantum dot heterostructures are of special interest for the study of intermixing and strain effects. Indeed, in many cases in these heterostructures, the quantum dot material is a binary alloy $Ge_xSi_{(1-x)}$ with 0 < x < 1. Strain is also unavoidable due to the large Ge-Si lattice mismatch. Despite its great importance, a comprehensive understanding of the combined effects of strain and intermixing in Ge-Si dots has yet to be realized. The details of the intermixing process in Ge/Si dots remain unclear. A random distribution of Si atoms in Ge dots has been predicted theoretically in Ref. 6. On the other hand, a highly anisotropic lateral Ge profile was found by a selective etching technique in uncapped Ge/Si pyramids and explained by a model of intermixing caused by surface diffusion.⁷ X-ray diffraction (XRD) data on buried⁸ and uncapped9 Ge/Si dots, selective etching of stacked dot layers, 10 and micro-Raman data on Ge/Si dots 4 and thinlayer heterostructures exhibit significant z anisotropy of the Ge content due to intermixing. Overgrowth of dots by a Si layer is usually required in these structures. This overgrowth generates additional intermixing and relaxation in the dots. For this reason the effect of the overgrowth parameters on the strain and Ge composition profile in single layer Ge/Si dots has been studied by XRD (Refs. 8 and 11) and photoluminescence (Ref. 12) techniques.

Raman spectroscopy, a rapid, sensitive, contactless, and nondestructive analytical method, is widely used for the characterization of Ge/Si nanostructures. Indeed, the position, intensity, and width of Raman lines due to the local Ge-Ge, Ge-Si, and Si-Si modes of the Ge/Si alloy enable one to obtain information on the composition, strain, and confinement within the Ge-Si nanostructures.3,4,13-15 However, there is difficulty regarding the analysis of Raman spectra of Ge/Si dots grown on Si substrates due to overlapping of the Ge-Si and Ge-Ge modes of Ge/Si with the twophonon spectrum [transverse acoustical (TA) modes] of the Si substrate, or spacers, at \sim 435 and \sim 302 cm⁻¹ (see discussion in Refs. 16-18). Since the two-phonon spectrum of Si is strongly polarized, ¹⁹ a suggestion has been made to take polarized Raman measurements of Ge/Si nanostructures in a configuration which allows suppression of the contribution of the silicon acoustic phonons to the Raman spectra in the region \sim 200–460 cm⁻¹ (Refs. 17 and 19–21). This approach has recently been successfully applied for studying strain and composition in a Ge/Si multilayer dot heterostructure with a Ge content of up to 70% (Ref. 4).

Analysis of Raman spectra is simplified for dots with a relatively low Si content, 19 because the Raman cross section of Ge is 1000 times greater that that of Si. Also, it is easier to take these measurements from multilayer dot structures, 4,20,22 where the signal from a large number of dots is analyzed. Considerable experimental difficulties arise when attempting to take measurements from a single Ge/Si dot layer with a large Si content whose Raman spectra are dominated by the two-phonon peaks of the silicon substrate. Nevertheless, these measurements are of great importance because the Raman spectra of multilayer structures provide stress values and intermixing averaged over a number of dot layers due to the relatively large penetration depth of the probe beam into the sample.⁴ However, to the best of our knowledge, Raman studies have not been performed to date in order to determine the composition profile and the strain state inside single-layer Si/Ge dots with a large Si content.

This paper reports polarized micro-Raman studies of the strain and atomic intermixing effect in single-layer Ge/Si dots grown on Si (001) surfaces at a variety of temperatures for both as-grown dot layers and dot layers under a Si cap layer.

II. EXPERIMENT

Ge dots were grown using an ultrahigh-vacuum chemical vapor deposition (UHV CVD) system. Pure SiH_4 and hydrogen-diluted (10%) GeH_4 were used as gas sources. Transmission electron microscopy (TEM) measurements were performed on sample cross sections using a 400-kV microscope. Details of the experimental setup and the growth conditions have been reported elsewhere.²³

A set of samples, grown at various temperatures, each consisting of a single-dot layer, was fabricated as follows. The temperature of the Ge layer growth was varied from 460 to 800 °C. At each of these temperatures a pair of

samples, one with and one without a Si cap layer, was grown. The Ge dots were capped by Si at the same deposition temperature that was used for Ge growth. The size and shape of the as-grown samples were characterized by cross-sectional high-resolution TEM and atomic force microscopy (AFM) techniques. Depending on the growth temperature, the Ge dots formed have different shapes, sizes, and areal density. The hut- and pyramid-shaped Ge/Si dots prepared were found to be highly oriented along the crystallographic axes of the Si substrate.²⁴ The growth conditions and properties of these samples are summarized in Table I. Typical AFM images of samples studied are shown in Figs. 1(a)–1(c).

Raman spectra were registered in backscattering geometry using a RENISHAW 1000 micro-Raman system equipped with a Leica microscope. To prevent sample heating the power density was kept below $10^5~\rm W/cm^2$. Measurements were performed at room temperature with the 514.5-nm line from an argon ion laser. A spot size of about 1 μ m was used throughout the study. An 1800-lines/mm grating was used for all measurements, corresponding to a spectral resolution of \sim 2 cm⁻¹ per 3 pixels.

Polarized Raman measurements were performed in backscattering geometry with a polarization configuration chosen according to the Raman selection rules to allow the signals from the Ge dot layer to be distinguished from those from the Si substrate. The sample position, crystallographic axes of the Si wafer, and polarizations of the incident and scattered light are shown in Fig. 1(d). Note that strain-induced LO-TO frequency splitting of the Ge-Ge mode, which is often utilized for strain measurements in Ge/Si QD's, 19,20,22 cannot be used for single-dot layers. Therefore, Raman spectra were obtained in VH or [001(100, 010)00-1] (Porto's notation) configurations [Fig. 1(d)], where scattering by the 2TA Si mode (peak at $\sim 302 \text{ cm}^{-1}$) is forbidden but scattering by the LO-like Si and Ge modes is allowed. All spectra were registered using the same accumulation time of 60 s. Forty accumulations were taken for each Raman spectrum measurement. In order to define the position of the phonon lines with a higher accuracy, the Raman bands were fitted with a Voigt function where the Gaussian contribution is a combination of the apparatus function and inhomogeneous broadening of the Raman lines because of the nonuniform dot composition.

III. RESULTS AND DISCUSSION

A set of representative Raman spectra (thick lines) measured in VH geometry in the region 250–500 cm⁻¹ is presented in Fig. 2(a) for samples grown at a temperature of 460 °C (1, as-grown; 2, with 20-nm Si cap layer) and 550 °C (3, with 20-nm Si cap layer). Raman spectra of the corresponding Si substrates, as reference spectra, obtained under the same conditions are also presented for comparison in Fig. 2(a) as thin lines. Prominent differences are clearly discernible between the sample and reference spectra in the region of interest. Although the 2TA band is observed at \sim 300 cm⁻¹ in both the sample spectra and the reference ones in the VH geometry, the Ge-Ge peak with an intensity suffi-

Growth temperature (°C)	Si cap thickness (nm)	Dots: base/height (nm)	Shape of dots	Areal density (μm ⁻²)	Ge content <i>x</i>	Strain ε
800	0	220/21	Pyramids	2.3	0.36±0.04	-0.012±0.003
		270/40	Domes			
800	70	220/21	Pyramids	2.3	0.34 ± 0.05	-0.011 ± 0.003
		270/40	Domes			
700	0	100/12	Pyramids	10	0.34 ± 0.05	-0.014 ± 0.003
		110/22	Domes			
700	60	100/12	Pyramids	10	0.32 ± 0.05	-0.013 ± 0.003
		110/22	Domes			
600	0	100/15	Domes	14	0.40 ± 0.04	-0.018 ± 0.002
600	46	100/15	Domes	14	0.34 ± 0.04	-0.014 ± 0.002
550	0	95/14	Domes	30	0.52 ± 0.04	-0.022 ± 0.002
550	22	95/14	Domes	30	0.40 ± 0.04	-0.017 ± 0.002
525	0	50/5	Hut clusters	150	0.65 ± 0.07	-0.025 ± 0.003
525	20	50/5	Hut clusters	150	0.47 ± 0.04	-0.018 ± 0.002
460	0	48/5	Hut clusters	100	0.85 ± 0.10	-0.028 ± 0.004
460	20	48/5	Hut clusters	100	0.50 ± 0.04	-0.020 ± 0.002

TABLE I. Growth conditions and parameters of samples with a single layer of Ge/Si dots.

cient for analysis appears as a low-energy shoulder of the Si 2TA peak in the sample spectrum. Importantly, the high degree of orientation of the hut- and pyramid-shaped Ge dots on the Si substrate in the samples studied²⁴ results in the highest value of intensity in the LO-phonon-like Ge-Ge peak in the VH polarization configuration.

The characteristic Raman spectrum of the Ge/Si dots (I_D) was obtained by taking the difference between the Raman spectra of the sample (I_S) and the reference Si wafer (I_{Si}) measured in the VH geometry:

$$I_D = I_S - FI_{Si}$$
,

where F is a scaling factor, obtained by taking the ratio of the LO-phonon bands of the Si substrate at 520 cm⁻¹ in the Raman spectrum of the sample and the reference Si wafer, $F = (I_S/I_{Si})_{520}$. Using this approach, the contribution of the Si substrate to the Raman spectrum of the sample can be taken into account.⁴ The contribution of the Ge wetting layer to the spectra is expected to be negligible.^{4,19}

In order to compare the intensities of the Raman signals from different samples, the spectra were normalized to the intensity of the Si substrate peak at 520 cm⁻¹ and the total volume of the dots illuminated by the incident light. A representative set of dot Raman spectra obtained in this way is shown in Fig. 2(b) for samples grown at different temperatures. Results are shown for both as-grown samples (thin line) and samples capped by a Si layer (thick line). Three features at frequencies of ~300, ~420, and ~450 cm⁻¹ are seen in the Raman spectra [Fig. 2(b)]. Assignment of these bands is well established: ^{13,25} the first and second peaks belong to the Ge-Ge and Si-Ge modes, respectively, while the third feature at 440–470 cm⁻¹ is attributed to unresolved lines of localized Si-Si vibrations in the neighborhood of

different numbers of Ge atoms. As can be seen from Fig. 2(b), the Raman spectra differ from each other depending on the temperature of the dot layer growth and whether a Si cap layer is present. The intensities of the Ge-Ge and Si-Ge bands in the Raman spectra of samples containing a single layer of dots were sufficient for analysis with $\sim 5\%$ uncertainty in the integrated intensities. The intensities of the Si-Ge band for the dot layers grown at 460 and 525 °C with-

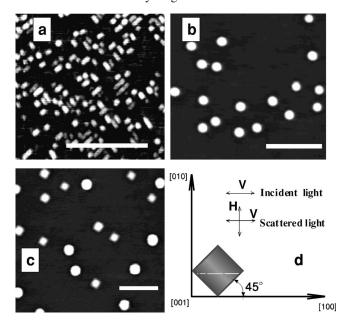


FIG. 1. AFM image of Ge/Si(001) dots grown at different temperatures: (a) 525 °C, (b) 600 °C, and (c) 800 °C; scale bars of 0.25, 0.5, and 1.0 μ m, respectively, are shown. (d) Schematic of electric vector orientation in incident and scattered channels during polarized Raman measurements.

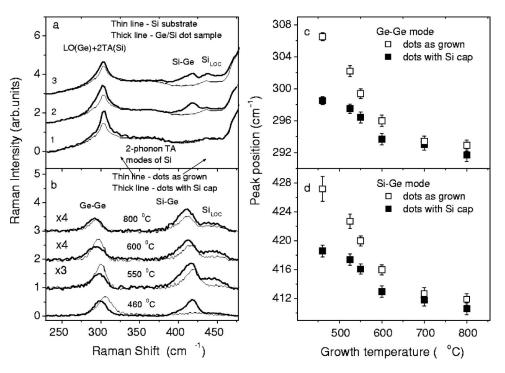


FIG. 2. (a) Raman spectra collected in VH polarization of Si substrate (thin line) and samples grown at 460 °C (1, without Si cap layer, and 2, with 20-nm Si cap layer), and (3) at 550 °C with 20-nm Si cap layer. (b) Differential Raman spectra for single-layer Ge/Si dots grown at different temperatures with (thick line) and without (thin line) a Si cap layer. The dependence of the peak position of (c) Ge-Ge and (d) Si-Ge phonon modes vs growth temperature for as-grown (□) and coated with Si cap layer (■) Ge/Si dots.

out a silicon cap layer were measured with uncertainties of 10% and 8%, respectively. However, due to the very large intensity of the Si substrate LO-phonon line at 520 cm⁻¹ in the spectra of the samples, we were not able to reliably distinguish the Si-Si line originating from the Ge/Si dots which is usually utilized for analysis of the strain and composition within the dots. ^{19,22,25,26} Therefore, for heterostructures with a single layer of Ge/Si dots we are restricted to examination of the positions and the integrated intensities of the Ge-Ge and Si-Ge Raman bands only.

The Raman spectra of the uncapped QD layers grown at 460 °C [see Fig. 2(b)] and 525 °C show a very weak Si-Ge peak and strong Ge-Ge peak located at ~307-303 cm⁻¹. This demonstrates that the Ge-Ge-mode frequencies exceed that for bulk Ge [300.8 cm⁻¹ (Ref. 27)], indicating the presence of compressive strain inside the dots and a high Ge content within the dots. The intensities of the Ge-Ge peaks in the spectra of the other samples are comparable with those of the Si-Ge peaks, suggesting a Ge content of 40%-60% in the Ge/Si dots. ^{19,22,26,28} Figures 2(c) and 2(d) present the temperature dependences of the Si-Ge and Ge-Ge peak positions for Si/Ge dots, for both as-grown and Si capped layers.

The ratio of the integrated intensities of the Ge-Ge and Si-Ge Raman peaks, $I_{\text{Ge-Ge}}/I_{\text{Si-Ge}}=Bx/2(1-x)$, can be used for determining the Ge content in Ge/Si alloys and nanostructures. Here x is the Ge content and B is a constant depending on the experimental conditions. The validity of this equation was initially checked for polarized Raman measurements in our experimental setup for a number of thin SiGe layers with known Ge content, situated between Si epitaxial layers. In this way, we determined a coefficient B of 1.5 for our experiments. The values of x for the dots studied are listed in Table I and shown in Fig. 3(a) for both as-grown and Si-capped dot layers. The errors are calculated using the standard deviations of the values for the integrated intensities of the Ge-Ge and Si-Ge modes.

In general, a shift in the Ge-Ge peak within the Ge/Si dots from the Ge bulk value can be attributed to (1) a confinement effect, (2) an intermixing effect, and (3) stress within the dots. Confinement tends to shift the Ge-Ge phonon peak downwards as the size of the dots reduces below 2–3 nm (Refs. 29 and 30). In this study, the size of the Ge/Si dots is too large to expect a substantial confinement effect. Normally, intermixing decreases the Ge phonon frequency when compared with that for bulk germanium, while

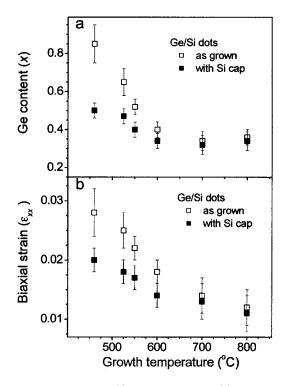


FIG. 3. Dependence of (a) Ge content x and (b) biaxial strain ε on growth temperature for Ge/Si dots.

compressive biaxial stress results in an upward frequency shift of the Ge-Ge and Si-Ge modes relative to those in a relaxed SiGe alloy. The Raman peak positions in Ge/Si dot systems are determined by the interplay between these two effects.

To a first-order approximation, we will only consider the biaxial strain in a Si/Ge layer structure, since the height-to-base ratio is small for all dots studied. The biaxial strain in the dot can be found from the Ge-Ge and Si-Ge peak positions using a model of biaxial strain in the (001) plane and the cusplike behavior of the Si-Ge mode in relaxed Ge/Si alloys. ^{19,25,26} In order to extract information on stress and intermixing in the Ge/Si dots from the shift of the Ge-Ge and Si-Ge Raman bands, we utilize an approach developed in Refs. 19 and 26. Based on the x values obtained from the ratio of the integrated intensities of the Ge-Ge and Si-Ge peaks, the value of the strain can be estimated by using empirical expressions both for Si-Ge ($\omega_{\text{Si-Ge}}$) and Ge-Ge ($\omega_{\text{Ge-Ge}}$) peak positions. These expressions, viz.,

$$\omega_{\text{Si-Ge}} \text{ (cm}^{-1}) = 400.5 + 14.2x - 575\varepsilon_{xx},$$

$$\omega_{\text{Ge-Ge}} \text{ (cm}^{-1}\text{)} = 282.5 + 16x - 384\varepsilon_{xx},$$

were obtained and verified for Ge_xSi_{1-x} alloys with a Ge content of x < 0.5 (Ref. 26). Here ε_{xx} is the biaxial strain in the (001) plane, which is directly related to the biaxial stress σ . The arithmetic average values of ε_{xx} calculated separately from the ω_{Si-Ge} and ω_{Ge-Ge} data for dots with $x \le 0.5$ are listed in Table I and shown in Fig. 3(b) as a function of the growth temperature for both as-grown and Si-capped dot layers. For the uncapped samples grown at 460, 525, and 550 °C, where x > 0.5, the ε_{xx} values were calculated by using the dependence of ω_{Ge-Ge} on strain, given by

$$\omega_{\text{Ge-Ge}} \text{ (cm}^{-1}) = \omega_{\text{Ge-Ge}}^0 + b_{\text{Ge-Ge}} \varepsilon_{xx},$$

where $\omega_{\text{Ge-Ge}}^0$, the frequency of the Ge-Ge mode in unstrained Si/Ge alloys, is taken from Ref. 25 and $b_{\text{Ge-Ge}}$ is the phonon strain-shift coefficient of $-400~\text{cm}^{-1}$ (Ref. 19). As shown in Ref. 19, this expression describes well the biaxial strain in Ge/Si dots with a high Ge content. The biaxial strain thus calculated is also presented in Table I, and shown in Fig. 3(b) versus growth temperature. Allowing for errors, the ratio of the strain and Ge content values for our samples is close to -0.042, characteristic of pseudomorphic, biaxially strained SiGe layers on a Si substrate.

For a single layer of dots, intermixing may occur at the dot/substrate interface for as-grown dots and additionally at the interface between the dots and cap layer for samples capped by silicon. Intermixing may be caused by thermoinduced atomic diffusion and also by the strain field distributed over the dot surface. The uncapped dots grown at the relatively low temperatures of 460 and 525 °C possess a Ge content x of 0.85 and 0.65 and compressive strains of -0.028 and -0.025, respectively. These hut-shaped dots have similar sizes, and the reduction of x and ε_{xx} is most likely to have resulted from temperature-induced intermixing and strain relaxation at the dot/substrate interface during dot growth.

Surprisingly, deposition of a 20-nm Si cap layer results in a dramatic reduction of the Ge content in these samples to 0.5 and 0.47 coupled with an elastic strain relaxation to -0.02 and -0.018. This suggests that the migration process of Si atoms from the cap layer into the dots becomes more efficient than migration from the Si substrate. However, given that intermixing governed by the surface interdiffusion would be expected to be proportional to the Ge-Si interface area, the increasing Si content, especially in the sample grown at 460 °C, cannot be explained by a simple increase of the Ge-Si interface surface due to capping. We believe that, for relatively small dots, strain-induced Si diffusion from the cap layer contributes significantly to a reduction of the Ge content and strain relaxation in the capped dots. This is supported by the fact that, in the region 460–600 °C, the uncapped dots demonstrate stronger dependences of x and ε_{xx} on temperature than the dots capped by the silicon layer (Fig. 3).

In general, the Ge content and strain gradually reduce as the growth temperature increases. Simultaneously the differential in the Ge content as well as in the strain value between as-grown and capped dots decreases and becomes negligible at 700 and 800 °C, indicating a reduction of the cap layer contribution to intermixing and strain relaxation at these temperatures. The behavior of the temperature dependences of intermixing for as-grown and capped dots derived from our Raman data agrees qualitatively with data obtained in photoluminescence experiments for analogous single-layer Ge/Si dots,¹² where the increased contribution of Si intermixing during capping with a reduction of the capping temperature has been observed. The XRD investigations of the Ge content for SiGe domelike dots layer grown at 630 °C and capped by a Si layer at capping temperatures of 460, 540, and 630 °C (Ref. 11) showed that the influence of the cap layer on the composition and strain within the dots reduces with a reduction of the capping temperature. However, this finding does not contradict our observation and can be explained by the fact that free-standing dots grown at 630 °C have already intermixed and relaxed substantially.

It should be noted that at 800 °C both as-grown and capped dots show an upward trend in Ge content although the strain continues to decrease. This is most likely because the size of the dots grown at 800 °C is much larger than the sizes of the dots grown at lower temperatures (see Table I). In addition, it is believed that intermixing mainly occurs at the boundary regions of the large dots; i.e., the dots consist of a Ge-rich core and a Si-rich shell generating a gradient in the Si concentration. Although the diffusion coefficient increases rapidly at growth temperatures from 700 to 800 °C (Ref. 20), the anticipated increase in dot size would be expected to lead to a relative increase in the contribution from the Ge-rich core to the Raman signal, as compared with that from the Si-rich shell. The existence of a nonuniform composition is supported by the fact that the peak width of the Ge-Ge mode of about 20-22 cm⁻¹ was found for the Ge/Si dot studied. This is broader than that of $\sim 15 \text{ cm}^{-1}$ reported for Si/Ge superlatices and SiGe alloys.31

IV. CONCLUSION

In conclusion, we have demonstrated that polarized micro-Raman spectroscopy can be used for the study of the

evolution of composition and biaxial strain even in single layers of Ge/Si dots. The dependences of these parameters on the dot growth temperature for both as-grown layers and layers covered by a thin Si cap layer are presented. We found that the temperature dependences of the Si capping effect on the biaxial strain and intermixing in single layers of Ge/Si dots grown on Si (001) surfaces correspond qualitatively to those determined in XRD and photoluminescence experiments performed on analogous Ge/Si structures. 11,12 The Ge content and biaxial strain dependences on the growth temperature in capped and uncapped Ge/Si dot single layers also qualitatively agree with those obtained by Raman spectroscopy of Ge/Si dot superlattices. 19,22 It has been found that, at low temperatures, the deposition of the Si cap layer strongly affects intermixing which causes elastic strain relaxation within the dot. It appears likely that this is due to straininduced interdiffusion of the silicon atoms into dots. The Raman data obtained for large dots formed at high growth temperatures agree with a model of Ge/Si dots consisting of a Si-rich boundary region and a Ge-rich core. These conclusions, however, are based on indirect evidence since only average Ge content and strain but not their detailed profile within the dots can be obtained by micro-Raman spectroscopy, which possesses a low spatial resolution relative to the dot sizes investigated. However, this limitation could be overcome by using tip-enhanced Raman spectroscopy, ³² a very promising technique for the investigation of the intermixing and strain profiles within Ge/Si dots with nanoscale spatial resolution.

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