Non-linear Identification Applied to Broadband Turbomachinery Noise

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Coherence based source analysis techniques can be used to identify the contribution of broadband noise sources in the exhaust of a gas turbine and hence enable the design of noise reduction devices. However, when the broadband noise source propagates in a non-linear fashion the identified contribution using ordinary coherence methods will be inaccurate. In this paper, an analysis technique to enable the contribution of linear and non-linear mechanisms to the propagated sound to be identified is reported. An experimental rig to study the propagation of noise through a rotor/stator set-up using a vane-axial fan mounted in a duct so that non-linear interactions between a sound source and the fan could be investigated is described. The technique which is used to identify non-linear noise contributions generated by the interaction of the rotor and propagated narrowband noise is reported. The analysis techniques enabled non-linear interactions to be identified and linear contributions to be determined.

I. Introduction

The reduction of the principal sources of aero-engine noise; the jet and the tonal contributions from the fan, compressor and turbine, has resulted in a new noise floor being reached. This noise floor will limit the benefits to be gained by further reducing these dominant components, unless the noise sources which set this threshold are in turn reduced. Of these, band-limited combustion noise and the broadband core noise sources of turbomachinery are significant contributors. The current trend towards high-bypass engines (which tend to reduce jet noise) and low Nox combustors (which may modify the noise characteristics) will result in broadband core noise becoming a more significant source.

Coherence-based noise source identification techniques can be used to identify the contribution of combustion noise to near and far field acoustic measurements of aero-engines. Karchmer and Reshotko1,2 and Reshotko and Karchmer3 used the ordinary coherence function between internal measurements and farfield microphones and derived the core noise at farfield locations by calculating the coherent output power (COP): a technique reported initially by Halvorsen and Bendat4. Karchmer5 also used the conditioned coherency function to determine where the source region for core noise was located. Extraneous noise contamination at an internal microphone location can result in the derived core noise at the farfield location being significantly lower than the true value. For such situations, Shivashankara6,7 used Chung’s8 flow noise rejection technique, to identify the internal core noise contribution to farfield noise measurements. Hsu and Ahuja9 extended Chung’s technique to develop a partial-coherence based technique, that uses five microphones, to extract ejection internal mixing noise from farfield signatures which were assumed to contain the ejection mixing noise, the externally generated mixing noise, and also another correlated mixing noise presumably from the ejection inlet. Wherever there is more than one source, all of these approaches necessitate the location of at least one sensor near one of the sources, e.g. the core noise source, in order to measure that source in isolation. Where there is only one source in the presence of extraneous noise, it has been shown when using Chung’s technique, that no direct measure of the source is necessary. Minami and Ahuja10 discuss a

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technique where only farfield measurements are needed to separate any number of correlated sources from extraneous noise, which due to its distributed nature, could be jet noise for example. Previously published work in this area from the 1970’s and 1980’s has been revisited in more recent years by Hsu and Ahuja. In Bennett and Fitzpatrick, techniques which can be used to identify the contribution of combustion noise to near and far-field acoustic measurements of aero-engines have been evaluated.

The coherence based source analysis techniques above can be used to identify the contribution of combustion noise in the exhaust of a jet engine and hence enable the design of noise reduction devices. However, when the combustion noise propagates in a non-linear fashion the identified contribution using ordinary coherence methods will be inaccurate. In the paper by Bennett and Fitzpatrick, an analysis technique to enable the contribution of linear and non-linear mechanisms to the propagated sound to be identified was reported. The technique was then applied to data from a small scale rig and to data from full scale turbo-fan engine tests. In this paper the techniques developed by Bennett and Fitzpatrick using tonal interactions are extended to examine bandlimited noise. In addition, the quadratic interaction model assumed in the previous paper is enhanced.

II. Non-linear Analysis

Acoustic interaction between rotors is a common observation in turbomachinery noise measurements and has been discussed analytically by Cumpsty, Holste & Neise, Enghardt et al. and numerically by Nallasamy. Energy at two different frequencies may interact to induce energy at a third. In these situations, the upstream energy source is a rotor-stator pair whose excited spinning modes impinge upon a second rotor found downstream. These interactions manifest themselves as sum and difference frequencies. However, the case where noise, which originates from an alternative noise source to the upstream rotor/stator pair, interacts with a downstream rotor-stator pair, is a relatively unexplored area. In Bennett & Fitzpatrick it was shown, using an experimental rig, how it is also possible for a tone generated, not from an additional upstream rotor/stator pair, but instead from an upstream speaker, to interact with a downstream rotor/stator pair to produce interaction frequencies. In addition, analysis of data acquired from full scale aero-engine tests within a European test campaign (Silencer) demonstrated that noise generated from the combustor interacted with both the high pressure and low pressure turbines to generate noise at sum and difference frequencies which were measured in the hot jet pipe of the engine. In this paper, the case where broadband or narrowband noise, such as may originate from a combustor or within the turbomachinery itself, interacts with a rotor-stator pair, to produce noise at sum and difference frequencies, is examined.

A. Nonlinear Simulations

The non-linear analysis of this paper investigates how to accommodate, in addition to propagated combustion noise and turbine noise measured at the exit plane of an aero-engine, the possibility of an interaction between the upstream combustion noise and the turbine, as outlined in figure 1. What is suggested is that the additional inputs into the system due to non-linearities could be an alternative cause for the drop in coherence with increasing engine speed and not simply the relative decrease in importance of the combustion noise compared to the other linear terms.

![Figure 1. Frequency response function between the combustion noise and the pressure measured at the exit plane when some rpm dependent non-linearity is included in the model.](image-url)

In order to investigate the influence of the non-linear interactions, a series of simulations were performed using synthetic data. A common non-linear interaction is quadratic in nature resulting in sum and difference...
frequencies as well a doubling in frequency. This can be demonstrated by observing the following two
trigonometric identities.

\[ [A \cos(\omega t)]^2 = \frac{1}{2} A^2 [1 + \cos(2\omega t)] \] (1)

\[ [A \cos(\omega_1 t) + B \cos(\omega_2 t)]^2 = \frac{1}{2} A^2 [1 + \cos(2\omega_1 t)] + \frac{1}{2} B^2 [1 + \cos(2\omega_2 t)] + AB \cos(\omega_1 + \omega_2) t + AB \cos(\omega_1 - \omega_2) t \] (2)

The doubling of frequency arises from self interaction, whereas the sum and difference frequencies come
about from combination interactions.

For the basic simulation discussed here, and illustrated in figure 2, synthetic data was generated in Matlab
using filtered statistically independent random data signals. Tones are used in the simulation as they more
readily demonstrate the phenomena. To be seen in figure 2 (A) is an auto-spectrum of a single tone at
1500Hz (\( G_{\text{comb}} \)), assumed to originate from the combustor can, and a second tone at 2500Hz, assumed to
be generated by the turbine, (\( G_{\text{turb}} \)). The linear superposition of these tones is shown in figure 2 (B). This
would be indicative of the auto-spectrum which would be expected to be measured at the exit plane in the
absence of nonlinear interaction. Figure 2 (C) shows the self and combination interactions, (\( G_{\text{comb}} + G_{\text{turb}} \))^2,
which would occur between these linear tones in the presence of a quadratic nonlinearity. Figure 2 (D) shows
the exit plane measurement, in black, being the summation of the linear and non-linear contributions when
nonlinear interaction was present. Clearly an ordinary coherence measurement between a sensor located
near the combustor can measuring only the combustion noise and a sensor located at the exit plane, would
be unable to detect the contribution of the combustor noise to the exit plane measurement at the nonlinear
interaction frequencies.

B. Nonlinear Identification Techniques

For ideal test situations an upstream sensor measurement will be able to isolate the broadband noise source.
Figure 3 shows the incident pressure situation in an aeroengine where a measure of combustion noise, for
example, is attainable upstream of a turbine and where the downstream measurement contains information
coherent with the turbine noise, the combustion noise and the non-linear interactions if present. In real
situations, however, such as the full scale engine tests discussed in Bennett and Fitzpatrick\(^ {12} \) and in the
experimental tests presented in this paper, turbine noise and nonlinear interactions will also propagate
upstream. The result of this is that both upstream and downstream measurements will contain information
coherent with each of the noise sources listed in figure 3(b).

As such, figure 4 is more representative of our situation, where both the upstream measurement \( x(t) \) and
the downstream measurement \( y(t) \) contain both the linear and nonlinear contributions. The challenge, thus,
is to identify the presence of nonlinear interactions, such as those illustrated in figure 2 (D), and furthermore
to separate these nonlinear contributions from the total exit plane measurement with the test situation given
in figure 4.

The technique developed in Bennett and Fitzpatrick\(^ {12} \) to facilitate this was to define a “non-linear”
coherence as

\[ \text{Nonlinear Coherence} = \gamma_{(x^2,y)}^2 \] (3)

which is simply the ordinary coherence between the square of the upstream measurement with the down-
stream measurement. The rational behind this is illustrated in an expansion of the square of the upstream
measurement, \( x(t) \) \(^ \# \);

\[ x = C + T + (C + T)^2 \] (5)

given in the following equation;

\(^ \# \)The dependance on t has been dropped for reasons of clarity
Figure 2. Auto spectra, Simulations with single fan tone, 10% Noise.

Figure 3. Incident pressure models accommodating a quadratic non-linear term.

\[(C + T) + (C + T)^2 = C^2 + 2CF + T^2 + 6C^2T + 6CF^2 + 4C^3T + 6C^2T^2 + 4CF^3 + 2C^3 + 2T^3 + C^4 + T^4 \]  

By squaring the upstream measurement the nonlinear contribution is maintained (underlined) whereas neither of the two linear components, C nor T explicitly remain in the expansion. Therefore, a coherence measure between \(x^2(t)\) and \(y(t)\) will identify the nonlinear components within the downstream measurement.

In order to isolate the linear contribution (in the presence of non-linear interactions), conditional spectral analysis techniques such as those discussed in Bendat and Piersol\(^{17}\) and employed by Esmonde et al\(^{18}\) may be used. Pertinent to this problem are results where it is calculated that if two arbitrary signals, \(i\) and \(j\),
are composed of at least two components each, where \( r \) is one of them, then the cross-spectrum between \( i \) and \( j \) with the linear effects of \( r \) removed can be expressed as

\[
G_{ij} = G_{ij} - \frac{G_{ir}G_{rj}}{G_{rr}}
\]  

(7)

It can be seen from this equation that the part correlated with \( r \) must then be

\[
G_{ij} = \frac{G_{ir}G_{rj}}{G_{rr}}
\]  

(8)

For \( i = j \), the autospectrum of either \( i \) or \( j \) with the linear part of \( r \) removed can be written as

\[
G_{ii} = G_{ii} - \frac{G_{ir}G_{ri}}{G_{rr}}
\]  

(9)

with the correlated part given by

\[
G_{ii} = \frac{|G_{ri}|^2}{G_{rr}}
\]  

(10)

The partial coherence function between \( i \) and \( j \) with the linear effects of \( r \) removed, as derived in Bendat and Piersol, \cite{Bendat} may now be defined as the ordinary coherence function between the conditioned spectra;

\[
\gamma_{ij}^2 = \frac{|G_{ij}|^2}{G_{ii}G_{jj}}
\]  

(11)

Applying this to our system, with the “nonlinear” coherence defined as above, a multiple input/single output model can be constructed as given in figure 5. Using this model, the non-linear contribution can be conditioned from the upstream measurement \( x(t) \), to leave the “residual” or partial coherence, viz. the part coherent with the linear components of \( y(t) \). This linear coherence for this two input/single output model is given by

\[
\text{Linear Coherence} = \gamma_{(x,y)\cdot x^2}^2
\]  

(12)

This technique was used with success in Bennett and Fitzpatrick \cite{Bennett} as previously discussed. The premise for this technique is that the \( x^2(t) \) term as expanded in Eqt. (6) is coherent only with the nonlinear contributions of the downstream measurement \( y(t) \). Applying this technique to the simulated data of section A, we see in figure 6 (A) how the ordinary coherence function fails to separate the linear from the non-linear terms but how Eqt. (3) applied to this data, in figure 6 (B), amplifies the relative importance of the nonlinear terms. The ideal objective of this technique is to be able to obtain nonlinear and linear coherences such as the theoretical coherences given in figures 6 (C) and 6 (D). Whilst the non-linear coherence presented in 6 (B) has suppressed the influence of the linear contributions, it is clear that for this simulation set-up, their contribution is still not insignificant. In this paper the technique is enhanced to improve the definition of the non-linear coherence.

![Figure 4](image1.png)  

**Figure 4.** Inputs into upstream and downstream measurements can be modelled as having linear and non-linear parts.

![Figure 5](image2.png)  

**Figure 5.** Input/output model for non-linear decomposition

A further examination of the expansion of Eqt. (6), shows that whilst the linear terms \( C \) and \( T \) do not appear explicitly, certain terms in the expansion are partially correlated with them. The first column of Table 1 highlights, in grey, these terms. An enhanced formulation of the nonlinear coherence would be, therefore, to condition these terms from \( x^2(t) \). From analysis of the \( x^3(t) \) expansion, as presented in the second column of Table 1, it can be seen that multiples of the same correlated terms appear. Therefore,
to condition $x^3(t)$ from $x^2(t)$ is to remove these partially coherent terms. However, the expansion of $x^3(t)$ also contains further terms not contained in the $x^2(t)$ expansion, and therefore, additional useful information would also be removed. A more optimal approach can be found by conditioning the $x^4(t)$, (column 3 of Table 1) from $x^3(t)$ term first and then to condition this residual from $x^2(t)$. Conditional Spectral Analysis is well suited to such treatment of inputs and figure 7 (A) presents the new multiple input/single output model for the nonlinear coherence. To remove this new nonlinear residual from the $x(t)$ term input is therefore to obtain the linear coherence. The model to obtain the linear coherence is given in figure 7 (B).

Results using these new formulations of the nonlinear and linear coherences are shown in figure 8. By conditioning the $x^2(t)$ term with only the $x^3(t)$ we see in figure 8 (A) that the contributions of the linear terms have been reduced, and indeed this is an improvement of the result using just the $x^2(t)$ term as per figure 6 (B). However, figure 8 (C) shows how the influence of the linear terms can be entirely removed by first conditioning the $x^4(t)$ term. Notice that the value of the coherence at the frequencies of the non-linear terms reduces with each conditioning. In parallel, the linear coherence for each permutation is shown in figures 8 (B) and (D) and is seen to be close to the ideal situation in both cases. Given these new advances, the nonlinear and linear coherences are redefined as

\begin{align}
\text{Enhanced Nonlinear Coherence} &= \gamma^2_{(x^2,y)} x^3 \cdot x^4 \\
\text{Enhanced Linear Coherence} &= \gamma^2_{(x,y)} x^2 \cdot x^3 \cdot x^4
\end{align}

and are shown schematically in figure 7.

**Figure 6.** Coherence, Simulations with single fan tone, 10% Noise.
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Table 1. \( x(t) \) term expansions
Figure 7. Conditional Spectral Analysis technique schematics for nonlinear and linear partial coherence models.

Figure 8. Coherence, Simulations with single fan tone, 10% Noise. Enhanced nonlinear and linear coherences applied.
III. Experimental Results

A. Experimental Setup

An experimental rig was designed and built to gain a fundamental physical understanding of the convection of noise through a rotor/stator set up, and is shown schematically in Fig. 9. A speaker represents the source noise which is directed down a brass tube of 3mm wall thickness with an internal diameter of 0.051m. This end of the tube is open and allows air to be sucked down the pipe by a vane-axial fan situated at a minimum of 1.2m from the entrance, according to the test set-up. This vane-axial fan which has a single 8 blade rotor stage downstream of a single 5 vane stator stage represents a simplified turbine of the turbofan engine. The tube ends with an open anechoic termination designed to reduce flow expansion/separation noise as well as reflections. A number of microphones were located upstream and downstream of the fan, at various axial positions, such that they were mounted flush with the inside of the pipe.

![Figure 9. Schematic of experimental set up.](image)

The data was acquired using a National Instruments 48 channel, 24 bit data acquisition system. Each channel was simultaneously sampled and automatically low pass filtered to avoid aliasing. The acquired data was stored on the PC, ready for post processing.

B. Narrowband Interaction

An analysis was performed on the experimental rig to detect the presence of non-linearities. In order to investigate the hypothesis that upstream broadband noise might interact with a rotor/stator pair to produce acoustic energy at sum and difference frequencies band limited noise was radiated from the speaker. Figure 10 shows the sound pressure level at a location downstream of the vane-axial fan using a microphone flush mounted with the inside of the duct. Three test configurations are shown. The first power spectral density (PSD) in red shows the energy measured by the microphone when band limited noise of 10.5 – 11kHz is emitted from the speaker. The plot in green shows the PSD when the speaker is turned off and the vane-axial fan is turned on. The fan has a high rotational speed of 16500rpm at the nominal max design voltage of 26VDC. As the fan has 8 blades this would result in a nominal blade pass frequency (BPF) of 2200Hz. In this test the rpm is lower with the BPF occurring at approximately 1600Hz a peak at which can be seen in the figure, as are its harmonics, nBPF, four of which are visible and are indicated with black dashed lines. The third test configuration in this figure is for the case where both the vane-axial fan and speaker operate simultaneously. It is clear, from observation of the blue PSD, that in addition to the 500Hz band of energy emitted from the speaker, bands of noise are frequency scattered to either side in accordance with ±BPF. This result is highly significant as noise is generated in frequency ranges which cannot be attributed to the simple superposition of the noise sources.

To demonstrate the effect of fan speed and associated nBPF dependency of the frequency scattering, a series of tests were carried out where the narrowband noise source remained constant with a reducing fan speed. Figure 11 shows a waterfall plot of PSD’s for the same microphone location but where in each successive test the fan speed is decreased. Two principle observations may be made from this plot. The first is that with decreasing nBPF the sum and difference frequency bands group closer to the speaker source.
band as to be expected. The second is that as a side effect of decreasing fan speed, the background flow noise decreases and additional scattered frequency ranges are revealed.

This latter point is further examined in figure 12 where the lower noise floor is more clearly seen. Of particular interest in this plot is how the interaction frequency magnitudes can remain significantly high even when the $BPF \text{ } magnitude$ has decreased substantially. The consequence of this is that nonlinear interaction noise can be a significant contributor to the overall sound pressure and may even greater than the “linear” noise sources.

![Figure 10. Auto-spectrum showing non-linear interaction between bandlimited noise at 10.5-11kHz and the fan.](image)

C. Non-linear Identification

The nonlinear identification techniques of section II are applied here to the experimental data. As discussed, often in real experimental tests, data acquired from sensors contain information from a number of different sources. In such cases, alternatives to the ordinary coherence function need to be applied. In figure 13 (A) and (B), a test set-up is such that microphones located both upstream and downstream of the vane-axial fan contain the vane-axial fan (or “turbine”) noise, the speaker (or “combustor”) noise and the nonlinear interactions. From observation of figure 13 (C), the ordinary coherence function between the upstream and downstream microphones reveals little other than that the coherence is high between the two locations for each of the sources. However, if the enhanced nonlinear coherence of Eqt. (13) is employed, then the coherence indicates both that nonlinear interaction has taken place and also identifies the associated frequency ranges.

The usefulness of this techniques as an identification tool is demonstrated in figure 14, where a waterfall plot of a new set of data is presented. In this series of tests, the vane-axial fan speed remains constant, and instead, the center frequency at which the bandlimited noise is emitted is incrementally increased. Some evidence of the presence of the nonlinear interactions is evident from the PSD’s, however, as previously stated, in full scale turbomachinery tests where there are many rotor/stator stages, such manual diagnosis
Figure 11. Waterfall plot of auto-spectrum showing non-linear interaction between bandlimited noise and the fan for a number of fan speeds.

is unreasonable. The enhanced nonlinear coherence has again been applied to a selection of the PSD’s of figure 14, and the results are presented in figure 15. Once again, the ability of the technique to identify the nonlinear interactions, when present, is displayed. The first plot is a situation where there is in fact no non-linear interaction, and for this result the coherence is low at all frequencies.

For all tests carried out on this particular experimental rig, nonlinear interaction has never been observed below a frequency of approximately $7k\, Hz$, or when the speaker source frequency is below this critical frequency. In the first plot of figures 14 and 15, the 500 Hz bandlimited source with a center frequency of 6250 results in no nonlinear interaction. In the work of Bennett the possibility that it is the modal content of the nonlinear interactions that determines its subsequent propagation down the duct was explored. It may also be possible that the diameter length scale, whose wavelength corresponds to the critical $\approx 7k\, Hz$ cut-off frequency, may be the cause. Both of these hypotheses will be further explored within the FP7 European Project TEENI on an experimental rig of DLR, one of the consortium partners. It is believed that the larger diameter of the rig will result in nonlinear interactions occurring at lower frequency ranges such as those in which direct and indirect combustion noise propagates.
Figure 12. Auto-spectrum showing non-linear interaction between bandlimited noise and the fan at high and low fan speeds.

IV. Conclusions

In this paper, the ability for coherence based noise source identification techniques to identify core noise in aero-engines was discussed. An experimental rig was designed and built to gain a fundamental physical understanding of the propagation of noise through a rotor/stator set-up. Experiments performed on the rig allowed it to be shown experimentally that acoustic energy in a duct at a certain frequency may interact with rotor/stator noise at a different frequency to scatter energy to a third frequency which is a sum of the two. The case where broad band or narrow band noise, such as may originate from a combustor, as opposed to an upstream rotor, interacts with a rotor-stator pair, (e.g. turbine noise), producing noise at sum and difference frequencies was explored in this paper. An experimental technique was developed which enables the non-linear interaction between the propagated sound source with the vane-axial fan to be detected and identified when present. The technique was extended to allow the linear and non-linear acoustic contributions to be separated.

The capacity to identify non-linear interaction is important as

- Energy in certain frequency ranges will not be the result of linear superposition of known noise sources.
- Energy in certain frequency ranges will change when sound sources producing noise at different frequencies are altered. This makes liner design difficult.
- Reducing a sound source will reduce noise in additional frequency ranges to the ones associated with the sound source.
- Addressing the non-linear interaction mechanism could be more effective in reducing noise than trying to reduce the resulting noise with a liner, for example.

V. Acknowledgements

This work was partly supported by the Seventh Framework Programme TEENI project which is funded under EU Commission grant agreement 212367
Figure 13. Auto spectra, Non-linear Coherence experimental data
Figure 14. Waterfall plot of auto-spectrum showing non-linear interaction between bandlimited noise and the fan for a range bandlimited frequencies.

Figure 15. Waterfall plot - Nonlinear coherence applied.
References