Restructuring of emergent grain boundaries at free surfaces – an interplay between core stabilization and elastic stress generation

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Abstract
Scanning tunneling microscopy and calculations are used to study the structure and relaxation of grain boundaries at the surface of planar nanocrystalline copper (111) films and bicrystals. We show that the strong energetic preference for boundary cores to lie along close-packed planes introduces a restructuring that rotates adjoining grains and generates elastic stresses in the triple junction region. The interplay of this stress field and the core stabilization determines the length scale of the restructuring and controls the shape and magnitude of the displacement field around the triple junction. Depending on the in-plane angle, restructured boundaries can extend to depths of ~15 nm with the associated elastic stress fields extending to even greater depths. These results point to a new mechanism of boundary relaxation at surfaces that is expected to be important in grain coalescence, film stress evolution and the properties of nanoscale materials.

Main

Introduction
Grain boundaries (GBs) impact a wide range of properties – electrical transport in nanoscale materials ¹, intergranular corrosion and catalysis at surface ²-⁵, stress evolution in thin films ⁶,⁷, and the mechanical strength of polycrystalline materials ⁸ – all critical to materials and device technologies ⁹-¹². The ever-increasing demand for innovation has heightened the need for an improved understanding of GBs and their impact on performance ¹³-¹⁵. However, little is known about the atomic-scale behavior of emergent grain boundaries (eGBs) at the surfaces of macroscopic materials. These studies are particularly challenging due to surface corrosion phenomena and the potential of capping layers used in TEM to suppress the intrinsic behavior of eGBs. Thus, it is challenging for TEM to detect atomic relaxation along the axis of eGBs or the natural shape of the triple junction (TJ) so that the eGB behavior and their associated surface and size effects have largely gone unstudied experimentally ¹⁶,¹⁷. Alternatively, the structure of eGBs is known to control dynamical thermal grooving at high temperatures ¹⁸-²⁰, but is poorly understood at lower temperatures where structure and stress play important roles.
Here we studied the structure of eGBs on surfaces of copper (111) nanocrystalline films and bicrystals, using of UHV cryogenic STM together with numerical calculations. The picometer resolution of STM allows a precise mapping of the atomic structure of eGBs and the displacement field of the free surface at the TJ. We identify the existence of a restructuring phenomenon that is driven by an energetic preference for boundary cores to lie along close-packed planes (CPPs) that involves the rotation of adjoining grains and the generation of elastic stresses in the TJ region. The interplay of the core stabilization and this stress field determines the length scale of the restructured boundary and controls the shape and magnitude of the displacement field around the TJ.

**Atomic & nanoscale structures and geometrical analysis**

We begin by considering the atomic structure of an eGB on a 50 nm thick nanocrystalline copper (111) film. Details of the sample, preparation and STM measurement are provided in the Supplementary Material (SM). Figure 1a shows the perspective view of the TJ, where the boundary meets the surface. The grains on either side of the boundary are about 20 nm wide and TJ is located in a local groove. Fig. 1b shows an atomic resolution image of this boundary. Both sides are clearly (111) surfaces as expected and eGB cores show dislocation-like features similar to the emergent LAGB previously reported. Although the atomic planes are curved or rotated downwards into the GB plane, there is no evidence of step formation, consistent with a free surface that is able to respond to the presence of a stress field in the subsurface region. The absence of surface steps confirms that the groove is not related to the Mullins’ thermal-grooving phenomenon and Wulff construction.

The misorientation or in-plane angle $\theta$ measured in Fig. 1b between the [110] directions of the two adjoining grains is $\sim 25^\circ$. In the half period of the boundary, the Burgers circuit in green shows that there is a $\vec{B}/2 = [110]$ closure failure along half of the period vector $\vec{b}/2 = 5/4\, [\overline{1}\overline{1}\overline{2}] + 2/4\, [1\overline{1}0]$, one with a spacing $3/4\, [\overline{1}\overline{1}\overline{2}] + 1/4\, [1\overline{1}0]$ and another with a spacing $2/4\, [\overline{1}\overline{1}\overline{2}] + 1/4\, [1\overline{1}0]$. When inserted into Frank’s formula,

$$\sin(\theta/2) = B/2p$$

we find $\theta = 26.01^\circ$, which agrees well with our measurement of $\sim 25^\circ$. Hence, we will refer to this boundary as eGB26. Using the surface basis of $1/4\, [\overline{1}\overline{1}\overline{2}]$ and $1/4\, [1\overline{1}0]$, the period vector can be rewritten as $[10,4]$ in surface notation, which decomposes into $[10,4]=[3,1]+[2,1]+[3,1]+[2,1]$ or $[3,2,3,2]$ for short.

The nature of the restructured boundary is evident from an analysis of the displacement field around the TJ. The groove width and minimum depth measured across the local maxima along the TJ are $\sim 3$ nm and $\sim 65$ pm, respectively (Fig 1c) and groove volume is $\sim 16$ atoms per period. Away from the boundary on either side of the groove the grains recover and return towards the planar orientation. The local angle within the groove is $0.15$ rad or $\sim 8.6^\circ$, meaning that the atomic planes on either side of the boundary are rotated $4.3^\circ$ away from the film normal. The global angle beyond the TJ groove is $\sim 0.7^\circ$. Previously we showed that adjoining grains at low angle boundaries in nanocrystalline copper (111) films exhibit an out-of-plane rotation angle $\varphi$ that scales with the in-plane misorientation angle $\theta$:

$$\tan \left(\varphi/2\right) = 1/2\sqrt{2} \cdot \sin(\theta/2)$$

The driving force for out-of-plane rotation is the energy anisotropy of the dislocation line that favors a [112] tilt axis that stabilizes the GB cores by enabling them to lie long [111] planes. For eGB26, the predicted rotation angle $\varphi/2$ on each side of the boundary is $\sim 4.5^\circ$ and very close to the local $4.3^\circ$ groove angle measured in Fig. 1c, d. From the boundary geometry perspective, a finite local groove angle implies that close to the surface the local tilt axis is shifted away from [111] towards [112], whereas the constant near-zero angle ($\sim 0.7^\circ$) further away from the boundary implies that deep into the film the tilt
axis returns to [111]. Different tilt axis have different symmetry, which indicates a phase-like restructuring around the TJ. We tested the generality of these results by mapping the TJ displacement field for a wide range of GB angles and found excellent agreement between the local groove angle and that predicted by the $(\theta/2, \varphi/2)$ scaling (see Fig. 1d). As expected, a finite positive (negative) global angle results in a smaller (larger) local angle compared to that predicted by geometry. Collectively, these results point to a strong preference for GB cores to lie along [111] planes regardless of the GB misorientation angle (see below).

**Bicrystal & surface effect**

To further confirm the generality of these results and that the shift of the tilt axis towards [112] is a property of eGBs in copper [111] materials, we employed STM to analyze the structure of the single boundary in an engineered macroscopic bicrystal. The bicrystal was 2 mm thick and 8 mm diameter and comprised of two Cu (111) single crystals that have been oriented and fused to form a GB 26.01° boundary (MaTeck Material). The preparation of the bicrystal for STM analysis is described in SM.

Figure 2a shows the presence of the single boundary and the arrangement of surface steps on either side of this boundary. A close-up view image is shown in Fig. 2b, which was recorded at a location >10 nm from the nearest step. Figure 2b inset shows an atomic resolution image of the adjoining crystals of the bicrystal that confirms the (111) surface periodicity and that the in-plane angle is indeed 26.01 degrees. Importantly we note the period vector of the boundary decomposes into [3,2,3,2], identical to the decomposition observed in nanocrystalline film in Fig. 1b. The displacement field across the bicrystal boundary is shown in Fig. 2c. The TJ exists within a groove formed between the adjoining crystals. Topographic-sections across the groove recorded under different bias conditions (see Fig. SM-1) show evidence of an electronic effect at larger positive bias (also seen in nanocrystalline films), the width and depth of the groove is essentially identical to that recorded for the nanocrystalline film. The local angle is 5.1° while far from the groove the global angle is $\sim -0.5°$. The existence of near identical eGBs at the surfaces of 50 nm thick nanocrystalline films and macroscopic bicrystals demonstrates that the restructured eGB26 is not influenced by the limited grain size (~50 nm) in the film and that the length scale of restructured boundary is much smaller than this grain size.

**Bulk GB energy calculation**

STM provides a direct measurement of TJ structure and the displacement normal to the surface. To understand the boundary restructuring and associated subsurface deformation fields, we rely on numerical calculations. Since for LAGBs the shift of the tilt axis towards [112] leads to a reduction of the boundary energy $^{21}$, we calculated the corresponding driving force for a wide range of in-plane angles, i.e., the energy difference $\Delta \gamma$ between a bulk GB with a tilt axis [111] and its corresponding bulk boundary with the tilt axis shifted toward [112], shown schematically as black and red in Fig. SM-2, respectively (GB geometrical specifications in SM). Classical molecular statics (MS) calculation results in Fig. 3a show that for all in-plane angles $\theta$, the [112] tilt boundary is always lower in energy. For each in-plane angle, the boundary energy decreases smoothly as the tilt axis shifts across the range of possible tilt axes between [111] and [112], revealing the absence of a thermodynamic barrier to grain rotation. For copper, the values of $\Delta \gamma$ range from 70 mJ m$^{-2}$ to 300 mJ m$^{-2}$ depending on the misorientation angle $\theta$ and in all instances $\Delta \gamma$ is a significant fraction of the original boundary energy. For GB 26.01°, $\Delta \gamma = 112 \text{ mJ/m}^2$, or $\sim 14\%$ of the GB 26.01° energy of 833mJ/m$^2$ (see Fig. SM-3).

**eGB calculation**
To see if the reduction in the bulk GB energy results in GB restructuring at the surface, we perform all-atom MS and molecular dynamics (MD) simulations of the symmetric tilt eGB26 in an \( H \geq 50 \) nm thick [111] copper film (SM and Tab. SM-1). While we observe a narrower and shallower groove compared to experiment (depth <10 pm and full width at half maximum (FWHM) <1 nm) at a [3,2,3,2] decomposed surface TJ, the structural transition of the boundary is absent (Figure SM-4). The change in energy of the TJ in the eGB26 is negligible (Supplementary Note and Fig. SM-7). Alternatively, mechanical reorientation of the rotated eGB[112]26 onto a (111) substrate preserves the [112] misorientation axis and the TJ structure (see Fig. SM-6). While the eGB energy now increases due to the (elastic) stresses associated with the reorientation, the surface profiles show increasing agreement with the experimental profiles (Fig. 1c & 2c) as the thickness of the reoriented eGB[112]26 is decreased to below 10 nm (Fig. SM-8). This is suggestive of partial rotation of the top layer and is consistent with a simple dimensional analysis: for a reoriented film of total height \( H \), the elastic energy cost scales as volume (\( \sim H^2 \)) while the GB energy reduction is proportional to its area (\( \sim H \Delta y \)).

We study the stability of the partially rotated eGB system using a modified computational framework eGB system summarized in Fig. 3b (see SM). The rotation is now limited to a top layer of varying thickness \( h \) and consisting of a V-shaped notch with an included angle \( \phi \). Commensurability between the rotated and reference (unrotated) regions of the film is ensured by shear-stitching the notch along the boundary normal, resulting in a valley at the eGB. Analogously, shear-packing of the cutout wedge at the eGBs leads to ridges at the GBs that bound the cell edges. The shear stitching/packing scheme is equivalent to the rotation of the top layer to eliminate the notch/wedge and mate it with the rest of the crystal, as summarized in Fig. SM-9.

eGB subsurface structure

Figure 4a shows the atomic-scale TJ structure following an equilibrium MS simulation of a \( h = 1.25 \) nm [6 (111) layers] thick rotated layer within an \( H = 50 \) nm thick film. The corrugation along the groove is evident from the surface profiles extracted at local maxima and minima, labelled X1 and X2 respectively. The corresponding line profiles plotted in Fig. 4b reveal groove depths of \( D1 \approx 100 \) pm and \( D2 \approx 40 \) pm respectively, and a surface width (FWHM \( \sim 1.5 \) nm) that is at least 50% larger compared to the unrotated eGB and similar to experimental FWHM of 1.3 nm. The local angle at the minima is \( \sim \phi \) and the global angle asymptotes to zero over a \( \sim 10 \) nm width centered at the eGB (Fig. 4b). The periodic TJ structure shows the emergence of dislocation-like features with a decomposition consistent with experiments (top, Fig. 4c). Subsurface characterization reveals coexistence of the two distinct GB structures with a transition at approximately the prescribed layer thickness \( h \) (bottom, Fig. 4c). This restructured eGB is stable to preparing temperatures (\( \sim 800 \)K). Varying \( h \) at fixed film thickness (\( H = 50 \) nm) leads to similar groove profiles, albeit with differing TJ widths (Fig. SM-10). The energy of each of these partially rotated eGBs is lower than that of the rotated and reoriented film, indicating that the equilibrium top layer thickness is less than 50 nm, consistent with the size independent local groove angles observed in the experiments.

eGB energetics: driving force for eGB restructuring and its stability

We analyze the stability of the partially rotated eGB system using a combination of scaling analyses and continuum computations. For a (111) copper film with surface energy \( \gamma_s \), the driving force for rotation (per film width) to form a valley is (Supplementary Note)

\[
\Delta U_F = [\gamma_{[112]}/\cos(\phi/2) - \gamma_{[111]}]h - [2\gamma_s \cdot \tan(\phi/2)]h
\]
where the first term is the contribution from the reduction in the GB area and the second term is the surface area eliminated by shear-stitching the notch \( l \). The elastic deformation energy scales quadratically with the notch height \( h \) and shear strain \( \varphi \). Detailed finite element method (FEM) computations of a shear-stitched surface notch (see SM) reveal a top layer under tension (Fig. SM-11) and a net elastic energy of the form

\[
\Delta U_e = f(h/H) C(v) \ G (\varphi h)^2
\]

where \( G \) is the shear modulus, \( C \) is a material constant set by the Poisson’s ratio \( v \), and the function \( f \) is the correction due to the finite thickness of the film parametrized by the ratio \( h/H \) (Fig. SM-12 and Supplementary Note).

Figure 4d shows the layer thickness dependence of these energetic contributions for the eGB26 system with film thickness \( H = 50 \) nm. The relevant interfacial and bulk parameters for pure copper are listed in Tab. SM-3-5. The elastic energy curve is plotted as a range based on anisotropy in the elastic parameters of pure copper (\( G, v \)) along and normal to the film, including the average over all orientations in a randomly textured polycrystal. Minimization of the total energy \( \Delta U_F + \Delta U_e \) yields an equilibrium top layer thickness \( h^* = 1.01 \) nm, or approximately five \( \{111\} \) layers, and a net energy change \( \Delta U^* = -0.1547 \) nJ/m. The minimum corresponds to elastic parameters along the GB normal and is close to that based on a polycrystalline average (\( h^* = 1.00 \) nm), see Tab. SM-5.

The continuum analysis is performed for a single crystal, and therefore ignores higher order corrections, if any, due to stress accommodation at the GB. Surface stresses and stress-dependent GB energies can drive additional changes. We capture these corrections using all-atom computations with rotated layer thickness in the range \( 0 \leq h \leq 2 \) nm, or \( 0 - 9 \{111\} \) layers. The variation in the total energy of the eGB system, also plotted in Fig. 4b for comparison, is similar to the continuum predictions with a slight shift in the minimum to \( h^* = 1.25 \) nm. The energy change \( \Delta U^* = -0.0954 \) nJ/m is smaller, likely due to the discrete nature of the \( \{111\} \) layers and stress-dependent bulk and interfacial parameters that are naturally incorporated in the atomistic model. This interplay is evident in the atomic stress distribution in Fig. 4c that exhibits a tensile to compressive stresses at the line defect that separates the two co-existing GBs, consistent with the elastic healing of a V-shaped notch (Fig. SM-11), and is distinct from the intrinsic stresses associated with each GB.

**eGB generalization to LAGB (energetics and subsurface structure)**

We test the generality of the energetic interplay at eGBs by performing a similar analysis for a valley formed at the eGB3.89 system (Fig. 5). A prescribed out-of-plane rotation of \( \varphi = 1.375^\circ \) corresponds to the \([111] \to [112]\) shift of the misorientation axis (Tab. SM-1). The GB and surface contributions to the driving force together with FEM-based bulk elastic energy are plotted in Fig. 5a. The surface contribution for the LAGB is smaller, as expected. The net energy exhibits a minimum at \( h^* \equiv 13 \) nm (Tab. SM-5) with negligible size effects at larger film thicknesses in the range \( H = 50 - 100 \) nm. MS computations of the eGB3.89 system around this minimum mimic the trends observed in the continuum computations, with an equilibrium rotated layer thickness that is shifted to \( h^* = 14.4 \) nm. The energy change of eGB3.89 system \( \Delta U^* = -0.51 \) nJ/m is again smaller than the continuum computations \( \Delta U^* = -0.67 \) nJ/m.

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1 Both contributions are dependent on the out-of-plane rotation \( \varphi \), and therefore the misorientation angle \( \theta \) \((\tan \varphi/2 \propto \sin \theta/2)\). For LAGBs, the driving force approaches \( \Delta \varphi \) and the surface contribution becomes increasingly important for HAGBs.
The surface profile shows corrugation with $D_1 \approx 110$ pm and $D_2 \sim 40$ pm, similar to the STM profiles in NC films with small deviations $\sim 7.5$ nm away from TJ (Fig. 5b). The corrugation $\sim 70$ pm is indicative of dissociated partial dislocations. The surface TJ exhibits a 1/2 [9817] period vector and the SF ribbon planes lie on the CPP, consistent with [112] tilt axis. The elastic stresses due to the reorientation increase the width of the SF ribbons at the surface (Fig. SM-13), suggestive of a GB contribution to the stress accommodation. Both experimental and atomistic peak ($X_2$) profiles reveal additional reconstructions at the SF edges at the surface that subvert the complete formation of the local groove. Figure 5c-d show the subsurface structure of the LAGB and stress distribution around the eGB. We see a sharp transition between the two co-existing GB structure, stabilized by a diffuse (compressive) stress, and the transition from tensile to compression stresses occurs well away from the line defect separating the two GB structures. The overall interplay between geometry and mechanics is similar to the observations for eGB26. The excellent agreement between atomistics and continuum computations for both eGBs indicates that higher order effects have a minimal effect on the energetics that sets the thickness of the rotated layer.

**Concluding remarks**

In this paper we demonstrated the existence of a natural driving force that restructures GBs at surfaces. This phenomenon will be particularly important whenever there is an interplay between GB energy, structure and stress. For example, tensile or compressive stresses generated in films at different growth stage$^{24,25}$ will modulate the intrinsic stress of eGBs, decreasing (increasing) the length scale at valley-shaped (ridge-shaped) boundaries, respectively. It will also impact material properties controlled by GBs, particularly in ultrathin films with thicknesses approaching the length scale of the restructured boundary and stress fields. In this instance, the film is comprised of a network of restructured boundaries and the surface effect described here becomes a size effect. Since [112] lies within a CPP, any boundary with this tilt axis can be considered to be a folded CPP. Given that electronic transport in copper occurs predominantly along CPPs$^{11,26,27}$ these [112] boundaries should exhibit reduced levels of boundary scattering. To realise these benefits it is necessary to develop processes that enable the deposition of materials with thermodynamically-relaxed [112] tilt boundaries.

J.J.B and X.Z. acknowledge support from Science Foundation Ireland grants (12/RC/2278 and 16/IA/4462) and early discussions with David Srolovitz, Adrian Sutton and Jian Han, and thank Peter Gleeson and John J. Plombon from Intel Corporation for the PVD samples. H.W. and M.W. acknowledge support from the National Natural Science Foundation of China (Grant No. 12172347) and the Fundamental Research Funds for the Central Universities (Grant No. WK2480000006).
Figure 1 Grain boundary structures at atomic resolution and nanoscale.

(a) Perspective view of GB 26.01°. (b) Atomic resolution mapping of GB 26.01°. The red lines show the vectors in both half crystals. The green path shows a Burgers circuit with a closure failure of a content two times nearest-neighbor distance. (c) STM topography of GB 26.01°. (d) Data points of white and green lines in (c). The black line is a local fit of the green points and the red line is the first derivative of the black line. Tuning parameters for (c) are I = 20 pA and U = -500 mV. Tuning parameters for (b) are I = 30 pA and U = 5 mV. (d) The local and global out-of-plane angles as a function of in-plane angles for LAGBs and HAGBs. Note that GB [111] 18.74° shows a range of the out-of-plane displacement angles at different sites.
Figure 2 Grain boundary structure at surface in bicrystal.

(a) STM topography image shows a straight line, where GB 26.01° emerges at the bicrystal (BC) surface. (b) STM image of eGB26 at the surface. Inset, shows atomic resolution of the TJ region and confirms the [3,2,3,2] decomposition. (c) Topographic profile of the TJ groove recorded along the cross section in (b) together with the profile of the TJ groove at the nanocrystalline (NC) surface. Tunneling parameters for (a) are I = 20 pA and U = 2 V, for (b) inset are I = 20 pA and U = 20 mV, for (b) are I = 20 pA and U = -200 mV.

Figure 3 GB energy and eGB calculation.

(a) In-plane angle dependent GB energy as the composite axis shift from [111] to [112] through out-of-plane rotation. (b) Computational scheme used to study the partial rotation of a top layer of thickness $h$ (shaded green) within a film of thickness $H \gg h$. Solid lines indicate GBs separated by the grain size $L$. Red and blue lines correspond to the unrotated and rotated GBs, respectively. The location of the valleys and ridges are as indicated.
Figure 4 Structure, morphology, and mechanics of the eGB26 system.

(a) Atomic-scale configuration of an equilibrated eGB composed of the $\theta = 26.01^\circ$ HAGB with a rotated layer thickness of 1.25 nm, or 6 \{111\} layers in a $H = 50$ thick \{111\} copper film. Atoms are coloured based on their depth coordinate. (b) Line profiles along troughs (blue, $X_1$) and peaks (red, $X_2$) within the undulating surface TJ, as indicated in (a). The solid green line is the slope of the $X_1$ profile. (c, top) Magnified view of the surface TJ. The dashed green lines connecting close-packed directions across the eGB serve as guides for the planar decomposition of the indicated periodicity vector. Atoms are coloured based on the potential energy (c, bottom). Side view showing the through thickness GB structure within the rotated and reference layer. The defect atoms are identified and coloured based on the central symmetry parameter. (d) The GB, surface and elastic energy contributions to the total energy of the eGB for varying rotated layer thicknesses. The elastic energy cost is plotted as a range based on continuum (FEM) computations; see text for details. Green spheres are results of MS simulations. The minima corresponding to the continuum and atomistic plots are indicated. (e) Through-thickness stress distribution in the vicinity of the eGB. The color indicates the atomic (virial) stress.
Figure 5 Atomistic-continuum computational analyses for the eGB3.9 system.

(a) Same as in Fig. 4d, but for eGB composed of the $\theta = 3.89^\circ$ LAGB. The vertical dashed lines indicate the minima for the continuum and atomistic computations. (b) The trough (green) and peak (red) line profiles extracted via MS simulations (spheres) and STM characterization of a 50 nm thick NC copper film (solid lines). (c-d) Through thickness (c) GB structure using the central symmetry parameter and (d) stress distribution based on the atomic stress observed.
References


