#### Accepted Manuscript

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Authors: Kevin. M. Metz, Paula E. Colavita, Kiu-Yuen Tse, Robert J. Hamers



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Please cite this article as: Kn.M. Metz, P.E. Colavita, K.-Y. Tse, R.J. Hamers, Nanotextured gold coatings on carbon nanofiber scaffolds as ultrahigh surface-area electrodes, *Journal of Power Sources* (2010), doi:10.1016/j.jpowsour.2011.09.098

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- High density edge plane containing carbon nanofibers electrodes are modified
- Electroless metal deposition is used to deposited highly textured gold coatings
- The electrochemical response of the hybrid electrodes is characterized
- The modified electrodes hold promise for varied applications in energy storage

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# Nanotextured gold coatings on carbon nanofiber scaffolds as ultrahigh surface-area electrodes

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5 Kevin. M. Metz<sup>1</sup>\*, Paula E. Colavita<sup>2</sup>, Kiu-Yuen Tse<sup>3</sup>, and Robert J. Hamers

6 Department of Chemistry, University of Wisconsin-Madison, 1101 University Ave.,
7 Madison, WI 53706, USA

8

#### 9 Keywords

- 10 Gold
- 11 Carbon
- 12 Electrodes
- 13 Nanoscale
- 14 Supercapcitor
- 15

#### 16 Abstract

17 High surface area metal electrodes are desirable for applications in energy storage 18 and energy conversion. Here, the formation and electrochemical characterization of a hybrid material made by electroless deposition of gold onto a scaffolding of vertically 19 20 aligned carbon nanofibers is described. Vertically aligned carbon nanofibers, ~80 nm in 21 diameter, provided mechanical support and electrical contact to the highly textured 22 nanoscale gold coatings. By chemically functionalizing the nanofiber surfaces and then 23 using electroless deposition methods, a highly textured metal coating was formed. The 24 electrochemical response of these "nano-on-nano" hybrid electrodes was characterized 25 using electrochemical methods. The results show that using the metallic coatings can increase the electrochemically active surface area by up to a factor of 10 compared with 26

<sup>\*</sup> Corresponding author. Tel.:1 517-629-0656; fax: 1-517-629-0264. E-mail address: kmetz@albion.edu

<sup>&</sup>lt;sup>1</sup> Present address: Department of Chemistry, Albion College, 611 E. Porter St., Albion, MI 49224, USA

<sup>&</sup>lt;sup>2</sup> Present address: School of Chemistry, Trinity College Dublin, College Green, Dublin 2, Ireland

<sup>&</sup>lt;sup>3</sup> Present address: 3M Company, Corporate Research Materials Laboratory, St Paul, MN 55144-1000, USA

- the starting carbon nanofiber scaffolds. The electrochemical response of the electrodeswas modulated by varying the deposition time of the gold.
- 29

#### 30 **1. Introduction**

31 Recently high surface area materials, such as nano-composites, have received 32 much attention as substrates for emerging energy storage and conversion technologies[1-33 3] associated with supercapacitors[4, 5], next-generation batteries[6], fuel cells [7-9], and 34 catalysis [10, 11]. Nanoscale forms of carbon, including nanotubes and nanofibers, have 35 been the focus of much research due to their excellent chemical stability and electrical 36 conductivity [2, 3]. Nanoscale forms of carbon can also be combined with polymers or 37 metals to form nano-composites [3, 7, 9, 12-16]. Such nano-composites are attractive 38 because their properties can be altered, building from the excellent performance of the 39 nanoscale carbon to create structures with tailored chemical or electrical properties [2, 3]. 40 However, fabrication of these composites can be hampered by the atomic perfection of 41 nanoscale carbon, which can create non-reactive surfaces. For example, many types of 42 nanoscale carbon need to be oxidized before metals can be deposited [13]. Often, the 43 oxidation processes used are harsh and can damage, or destroy, much of the carbon. 44 Additionally, accessibility of the full surface area can be difficult to achieve. 45 A gold-carbon nanocomposite based on vertically aligned carbon nanofibers

46 (VACNFs) [17] has previously been reported on. The fabrication method takes advantage
47 of the fact that nanofibers can be grown in a structure in which graphene sheets are nested
48 inside one another in a stacked-cup arrangement. This structure exposes large amounts of
49 edge-plane graphite along the sidewalls. Photochemical functionalization of the

50	nanofibers with a molecular layer exposing carboxylic acid groups leads to extremely
51	efficient nucleation of metals onto the nanofibers [17, 18]. The use of photochemical
52	functionalization has the advantage of being fully compatible with metal substrates and
53	causing no damage to the physical properties of the nanofibers.
54	Previous studies also showed that metal deposition on top of the molecular
55	monolayer modified VACNFS increased the active area of the electrode by a factor of ten
56	compared to the nanofiber template; creating an electrode with a 100 fold increase in
57	electrochemically accessible surface area compared to a planar electrode [17].
58	Additionally, it was demonstrated that the effective capacitance of these highly textured
59	electrodes scaled with the accessible surface area [17].
60	Here a more thorough characterization of Faradaic and non-Faradaic response of
61	these highly textured, nano-structured gold electrodes in order to understand the resulting
62	interfacial electrical response. Data that helps elucidate the mechanism of the electroless
63	plating on molecular monolayer-modified carbon surfaces is presented. Additionally, the
64	electrical response of the electrodes at the interface of aqueous solution, both in the
65	presence and absence of electron transfer reagents, is investigated. Finally, comparisons
66	are made to other types of high surface area electrodes. The results demonstrate that
67	metal-on-carbon hybrid nanostructures, which have a high surface capacitance and lower
68	contact resistance, can provide very high surface area of electrochemically accessible,
69	chemically stable materials that may be of potential utility in energy storage, e.g., as
70	electrodes in electrochemical double layer capacitors [4].

71

### 72 **2. Experimental**

#### 73 2.1 Growth of carbon nanofibers.

74 Carbon nanofibers were grown in a custom built chamber using DC plasma 75 enhanced chemical vapor deposition (DC-PECVD) [19-21]. Silicon substrates (with their 76 native oxide) were coated with 50 nm of molybdenum, 20 nm of titanium, and 20 nm 77 nickel as the top layer. Nanofibers were grown using acetylene and ammonia with flow 78 rates of 30 standard cubic centimeters per minute (sccm) and 80 sccm, respectively, at a 79 chamber pressure of 4 Torr and a DC power of 360 W. Growth times and conditions 80 determine the physical properties of the nanofibers produced. Here, all fibers were 81 grown for 15 minutes, which produces high densities of vertically aligned, cylindrical 82 nanofibers with an average diameter of 80 nm and an average length of 2  $\mu$ m.

83

#### 84 2.2 Gold deposition on carbon nanofibers.

85 To enhance nucleation of gold the nanofibers were functionalized with a 86 molecular monolayer in order to produce a high density of carboxylic acid groups along 87 the nanofiber sidewalls. This was achieved using a photochemical grafting procedure 88 developed previously [22] in which organic molecules bearing a terminal alkene group 89 (C=C) covalently grafts to the graphitic edge-planes of VACNFs when illuminated with 90 ultraviolet light at 254 nm [23]. This method has been shown to form molecular layers 91 that allow facile electron transport [24]. Here, this work is extended to metallic layers on 92 carbon nanofibers. Freshly grown VACNFs were reacted with undecylenic acid methyl 93 ester by dripping a thin film of the pure liquid reagent onto the VACNF samples, and illuminating with 254 nm light (~1 mW cm<sup>-2</sup>) for 16-18 hours in a nitrogen-purged 94 95 reaction chamber. The surface-linked ester was then converted to carboxylic acid using a

96 slurry of potassium tert-butoxide in dimethyl sulfoxide [24], producing carbon nanofibers
97 functionalized with carboxylic acid moieties. The fibers were then cleaned in 0.1 M HCl
98 and washed in a 50:50 solution of distilled water and methanol.

99 Deposition of gold onto the COOH-terminated nanofibers [17] was achieved by

sensitizing the carboxylic acid-modified fibers in a bath containing 0.026 M SnCl<sub>2</sub> and

101 0.07 M trifluoroacetic acid in a 50:50 methanol: deionized water solution; this step binds

102 tin ions to the carboxylic acid moieties on the surface [25]. The tin sensitized fibers

103 were then activated with silver by immersion in a silver bath consisting of 0.03 M

104 ammoniacal silver nitrate. This leaves atomic silver bound to the surface, via a redox

105 reaction with the tin ions. Finally the VACNF samples were placed in individual gold

baths, containing 0.127 M Na<sub>2</sub>SO<sub>3</sub>, 0.025 M NaHCO<sub>3</sub>, 0.625 M formaldehyde and 8 mM

107  $Na_3Au(SO_3)_2$  (Technic Oromerse Part B gold solution), at pH 10, and 6°C for durations

108 of 1 to 22 hours. The time in the gold bath controlled the amount of gold on the fibers109 [17].

110

111 2.3 Electrical characterization.

Electrical characterization was carried out using electrochemical impedance spectroscopy (EIS) and Cyclic Voltammetry (CV) using a three-electrode geometry. Measurements were made in aqueous solutions of KCl, KClO4, and  $Ru(NH_3)_6^{+2/+3}$ , of various concentrations. All measurements used the gold-coated carbon nanofiber sample as the working electrode. For comparison, capacitance measurements were made in aqueous solutions of KCl over planar gold and glassy carbon electrodes. The data were collected using a single junction Ag/AgCl (3M KCl) reference electrode. In all

119	measurements ohmic contact was made to the top side of the gold-coated carbon
120	nanofiber samples outside of the fluid compartment of the cell. Impedance
121	measurements were made at the open circuit potential in room temperature. Aqueous
122	solutions were purged with argon prior to use. All data shown here have been normalized
123	to the geometric area of the cells used. All measurements were performed using a 3-
124	electrode potentiostat and impedance analyzer (Solartron 1260/1287) using Zplot or
125	Corrware software (Scribner Associates, Inc).
126	
127	2.4 Fourier Transform Infrared (FTIR) Measurements.
128	The chemical functionalization and tin sensitization of the carbon nanofibers were
129	verified using infrared spectroscopy. Spectra were collected using infrared reflection
130	absorption spectroscopy (IRRAS) in a Bruker Vertex 70 FTIR spectrometer with a
131	variable angle reflection accessory (VeeMaxII, Pike). Spectra shown here were collected
132	with s-polarized light at an incidence angle of $60^{\circ}$ from the surface normal. The
133	background and sample spectra each consisted of 500 scans at 4 cm <sup>-1</sup> resolution. Spectra
134	were baseline-corrected using commercial software (Grams, Thermo Galactic).
135	
136	3. Results
137	3.1 Nanoscale morphology.
138	Figure 1 shows scanning electron microscope (SEM) images of as-grown
139	VACNFs before any modification (Figure 1A) and functionalized nanofibers after
140	immersion in the gold deposition bath for different lengths of time. It is clear from Figure

141 1A that the fibers are cylindrical, vertically aligned and packed in a high density

142	arrangement. Once functionalized and placed in a gold bath, nanoparticles of gold						
143	nucleate and grow on the carbon nanofibers. Figure 1B shows VACNFs after 3 hours in						
144	a gold bath. At this point the nanoparticles are clearly visible and in some cases have						
145	started to coalesce. After 5 hours in the gold bath the gold nanoparticles have fully						
146	coalesced, forming a textured gold sheath that completely encapsulates the carbon						
147	nanofibers. With continued time in the gold bath, the gold sheath forms a more complex						
148	texture, with spike-like features frequently extending more than 100 nm long. Figure 1C						
149	shows a gold-carbon composite after 7 hours in a gold bath, which displays this complex,						
150	highly textured gold coating. The interactions of the spike-like projections on						
151	neighboring fibers form a very complex, essentially random network in the interstitials						
152	between the fibers.						
153	Control experiments were performed on planar carbon surfaces that were						
154	functionalized with an identical monolayer. The functionalized planar surfaces showed a						
155	high density of nanocrystalline gold particles and some regions of spongy masses of gold,						
156	but did not show the complex morphology observed on the functionalized VACNFs.						
157							
158	3.2 Characterization of functionalization chemistry and impact on electroless deposition						
159	on VACNF electrodes.						
160	An important aspect of the fabrication method is the use of a molecular layer to						
161	provide carboxylic acid sites for metal binding. Infrared spectroscopy was used to						
162	characterize the chemical changes associated with the functionalization and their						
163	influence on the final structures shown in Figure 1. Figure 2 shows infrared absorption						
164	spectra of carbon nanofibers that were photochemically functionalized and de-protected						

165 to expose carboxylic acid groups before(Figure 2A) and after (Figure 2B) exposure to 166 tin. Figure 2C shows a control spectrum for a carbon nanofiber sample that was not 167 functionalized, but was exposed to the tin sensitization bath. The absorption band of atmospheric carbon dioxide near 2360 cm<sup>-1</sup> has been omitted for clarity. All spectra were 168 collected and referenced to a background spectrum collected from a freshly grown, bare 169 170 carbon nanofiber sample using a 60° incidence angle and s-polarized light. All three spectra are dominated by a large peak near 1587 cm<sup>-1</sup>; this peak appears 171 172 to originate in C=C binding vibrations of the bulk nanofibers and thus is related to the 173 nanofiber structure. Therefore examination of changes in the weaker features in the 174 spectra is needed to monitor changes in the surface chemistry. The FTIR spectrum shown in trace (A) of Figure 2 shows methylene (CH<sub>2</sub>) peaks at 2927 and 2856 cm<sup>-1</sup> and a sharp 175 peak in the C=O regions at 1715  $\text{cm}^{-1}$ [26]. 176 The importance of surface chemical termination is revealed more clearly after the 177 178 next step of functionalization, which involves binding of tin as a sensitizer to the 179 nanofibers. Tin exposure was carried out by wetting the fibers with methanol and then 180 soaking them in the tin sensitizing bath for 30 minutes. The spectrum of the "bare" 181 nanofibers that was exposed to tin shows no significant features other than the peak near 1587 cm<sup>-1</sup>, which corresponds to the bulk nanofibers. For the COOH-modified samples 182 183 (Fib. 2b), exposure to tin leads to no significant change in the C-H region, but the peak at 1715 cm<sup>-1</sup> (2A) disappears and is replaced with a new peak at 1658 cm<sup>-1</sup> (2B). This is 184 very close to the value of 1655 cm<sup>-1</sup> previously reported for the C=O antisymmetric 185 186 stretching of tin carboxylate [27].

187	The FTIR data show that (1) photochemical functionalization leads to formation
188	of stable monolayers, and (2) that immersion into the tin bath leads to clear, well-defined
189	changes in the spectra corresponding with the transition from –COOH termination to –
190	$(COO^{-})_2 Sn^{+2}$ . Finally, the fact that no significant CO features are observed on the "bare"
191	nanofibers either before (data not shown) or after tin treatment demonstrates that the bare
192	nanofibers have only small numbers of carboxylic acid groups, below the detection limit
193	of FTIR. The fact that there is no corresponding peak in the bare nanofibers spectrum
194	provides direct evidence that the molecular layer is needed to create oxidized carbon sites
195	for metal binding (vide infra).

196

#### 197 *3.3 Electrochemical impedance measurements.*

198 Electrochemical impedance spectroscopy (EIS) was used to examine how the 199 evolution in morphology from the simple cylinders to the more complex geometry visible 200 in Figure 1 alters the electrical properties of the interface. In EIS, a small modulation 201 with a root-mean-square (RMS) amplitude of ~ 10 mV is applied to the sample. The in-202 phase and out-of-phase components of the current are measured, and the impedance is 203 described by the complex quantity

204

$$Z = Z' + iZ'' \tag{1}$$

Impedance data are usually presented as plots of the magnitude (|Z|) and phase angle (θ)
of the impedance as a function of frequency. Figure 3 shows EIS on bare carbon
nanofibers and on carboxylic acid-modified nanofibers that were exposed to the gold
electroless deposition bath for 3 hours and 7 hours. These measurements were made in
0.1 M KCl solution at the open circuit potential (0.086 V, 0.023 V, and 0.044 V vs.

210 Ag/AgCl for the bare, 3 h and 7 h samples respectively). At low frequencies, all three 211 samples show nearly linear decreases in impedance, dropping over the range from 0.1 Hz 212 to 10 Hz. Figure 3A shows that increased time in the gold bath results in a lower 213 impedance at low frequency. At 0.1 Hz, the lowest frequency measured here, the absolute impedance drops from ~2600  $\Omega$  cm<sup>2</sup> for bare nanofibers, through ~820  $\Omega$  cm<sup>2</sup> 214 for nanofibers with gold deposited 3 hours to a minimum of ~400  $\Omega$  cm<sup>2</sup> for nanofibers 215 216 with 7 hours of gold deposition, representing a ratio of impedances of  $\sim 1.0 : 0.31 : 0.15$ . 217 This ratio of impedances is over the frequency range from 0.1 Hz to 10-100 Hz. At high 218 frequency, greater than 1 kHz, the area-normalized impedance of all three samples drops to a few  $\Omega$  cm<sup>2</sup>. This impedance corresponds to the uncompensated resistance of the 219 220 solution. While this uncompensated resistance should be the same for all samples, some 221 variations arise due to slight irreproducibility in the position of the reference electrode, as 222 verified by independent control experiments.

223 Figure 3B shows that increased time in the gold bath also results in a larger phase 224 angle. A phase angle of -90° corresponds to ideal capacitance, whereas a phase angle of 225 0° corresponds to pure resistance. All three samples show roughly sigmoidal shaped 226 curves as a function of frequency. Bare nanofibers and 3 hour gold-coated nanofibers 227 show a phase angle of approximately -60° at 0.1 Hz while nanofibers with 7 hours of gold 228 deposited on them show a phase angle of -74°. All three curves shift upwards, towards -229 90°, before falling to near 0° at frequencies around 1 kHz. This higher phase angle 230 observed at low frequency implies that with the addition of more gold, the fibers become 231 slightly more ideally capacitive.

232	The formation of the highly textured gold surfaces is accompanied by a change in
233	the electrode material (carbon to gold) and in the effective area in contact with the
234	electrolyte solution. In the case of carbon based electrodes, the capacitance further
235	depends on the ratio of basal-plane to edge-plane graphite present [28, 29]. To help
236	determine how each of these factors contributes to the changes in impedance, EIS
237	measurements were made on planar glassy carbon and planar gold electrodes in 0.1 M
238	KCl solutions. Glassy carbon was selected as planar comparison because it contains a
239	large amount of edge-plane graphite [30], much akin to the carbon nanofibers.
240	Figure 4 shows the impedance and phase angle vs. frequency for these samples.
241	At the lowest frequencies (0.1 Hz) the impedances for gold and glassy carbon samples
242	are both substantially larger than those observed with nanofiber samples. In both cases,
243	the total impedance drops nearly linearly from 0.1 Hz to $\sim 10^2 - 10^3$ Hz, and at higher
244	frequencies plateaus at a constant value corresponding to the uncompensated solution
245	resistance. The phase angle data, Figure 4B, again exhibit roughly sigmoidal shapes,
246	reaching phase angles of -80° at the lowest frequency, increasing very slightly toward
247	90°, and then at a frequency of $10^2$ - $10^3$ Hz dropping toward zero. Figure 4A shows that
248	the glassy carbon electrodes display approximately twice the impedance of the gold
249	sample. This difference likely arises from a combination of factors including an increased
250	density of states and higher roughness for the gold sample and indicates that the much
251	more pronounced difference observed in comparing bare VANCFs with gold-covered
252	VACNFs is primarily geometric in origin, but may have some contribution from the
253	difference in materials

254	Another possible contributor to the absolute impedance observed with the
255	addition of gold to carbon nanofibers is the high specific adsorption of chloride ions to
256	gold [31]. To help separate the effects of surface area and specific adsorption,
257	experiments were performed changing the composition and concentration of the
258	electrolyte concentration. Since potassium perchlorate (KClO <sub>4</sub> ) does not exhibit strong
259	adsorption to gold [32], data in chloride- and perchlorate-containing solutions can be
260	used to assess whether there is strong specific adsorption to the gold surfaces. Figure 5
261	shows absolute impedance and phase angle data for gold coated carbon nanofibers in 0.1
262	M KCl and 0.1 M KClO <sub>4</sub> measured at the open circuit potential. The spectra in Figure 5
263	are not significantly different from one another; this demonstrates that the impedance
264	behavior of the Au-coated fibers is not dominated by anion adsorption effects.

265

#### 266 *3.4 Charge transfer at electrodes.*

To determine how the nanotextured gold coating impacts the electron-transfer 267 properties of the sample, Faradaic processes at the surfaces using the redox couple 268  $Ru(NH_3)_6^{2+/3+}$  were examined. Previous studies have shown that  $Ru(NH_3)_6^{2+/3+}$  is an 269 270 outer-sphere system involving electron transfer that is sensitive primarily to the density of 271 states of the electrode, and relatively insensitive to surface chemical composition [33]. Figure 6 shows the magnitude and phase of the impedance measured on an electrode with 272 273 gold deposited on it for 7 hours in 0.1 M KCl, and in a solution of 0.1 M KCl with 5 mM each of  $Ru(NH_3)_6^{2+}$  and  $Ru(NH_3)_6^{3+}$ , collected at the open circuit potential. A fit to an 274 275 equivalent circuit model, is also shown. The equivalent circuit used to construct this fit is 276 shown in Figure 6C, and consists of a resistor, modeling the solution resistance, in series

with the parallel combination of a CPE and a resistor, which model the capacitance and
charge transfer at the interface. The parameters used in the modeling are presented in
table 1.

280 Figure 6A shows that above  $\sim 100$  Hz, the presence of the redox agent has no 281 significant change on the electrical response. At lower frequencies, however, the 282 magnitude of the impedance is reduced. For example at 0.1 Hz the absolute impedance decreases from ~400 to ~100  $\Omega$  cm<sup>2</sup>. The phase angle response (Figure 6B) takes on a 283 284 new shape in the presence of the redox couple, changing from the roughly sigmoidal 285 shape observed in 0.1 M KCl to a more linear response at low frequency, falling from 286 about -45° at 0.1 Hz to roughly 0° at 100 Hz. This is consistent with the fact that the 287 impedance at these frequencies is limited by the uncompensated solution resistance, which is mostly unchanged by the addition of a low concentration of redox couple to the 288 289 0.1 M KCl solution.

290 As a point of reference, Figure 7 shows impedance and phase angle data for 291 planar glassy carbon and gold electrodes in 0.1 M KCl and in 0.1 M KCl containing 5 mM each of  $Ru(NH_3)_6^{2+}$  and  $Ru(NH_3)_6^{3+}$ , measured at the OCP. Figure 7 shows that, 292 293 much akin to the behavior of the gold-modified carbon nanofibers, the addition of a redox 294 couple significantly lowers the absolute impedance and phase angle of the planar 295 electrodes at low frequency. However, the effect is much more dramatic with the planar 296 samples. For example, at 0.1 Hz the hexaamineruthenium complex causes the impedance of the glassy carbon electrode to decrease from ~173 k $\Omega$  cm<sup>2</sup> to ~150  $\Omega$  cm<sup>2</sup> and the 297 impedance of the gold electrode to drop from ~18 k $\Omega$  cm<sup>2</sup> to ~150  $\Omega$  cm<sup>2</sup>. 298

299 One of the most significant results from these studies is that while for planar 300 electrodes the redox agent reduces the impedance by a factor of more than 100, on gold-301 coated nanofibers the reduction is much smaller. This implies that the high surface area 302 of the nanofibers is not the limiting factor in the Faradaic processes. 303 To explore the kinetics under quasi-steady state conditions, Figure 8 shows cyclic 304 voltammograms of gold coated carbon nanofibers (Figure 8A) and a planar gold electrode (Figure 8B) in a solution of 5 mM each of  $Ru(NH_3)_6^{2+/3+}$  with 0.1 M KCl, at a 305 scan rate of 25 mVs<sup>-1</sup>. The shapes of the curves are different near the most positive and 306 307 most negative potentials. This shape difference arises from the capacitance charging of 308 the surface during the measurement. Figure 8B also shows a peak current nearly twice as 309 large as Figure 8A, however calculating the area from the peak current, after removing 310 the capacitive current contribution, results in the geometric area of the cell used here. 311 This indicates that the gold coated nanofibers are in a planar diffusion regime. Diffusion 312 effects may also be responsible for the increased peak separation. It is reasonable that 313 diffusion effects seem to dominate given the very complex, nearly random networks that 314 exist between the individual fibers.

315

#### 316 **4. Discussion**

317 *4.1 Materials requirements for metal-nanofiber composites.* 

Recent studies have emphasized that high surface area, well-defined porosity and high crystallinity are indispensable requirements for materials in many energy storage and conversion applications [9]. For metals, high crystallinity implies good conductivity,

and the high surface area with well-defined porosity implies a highly accessible surfacearea.

323	Previous studies on high surface area porous carbon have shown that the very
324	small pores, which lead to high surface area, are not always accessible and can have
325	difficulty supporting well defined electrical double layers [5]. Carbon nanotubes and
326	nanofibers have emerged as novel high surface-area materials of intense interest.
327	However, one problem with small-diameter (e.g., single-walled) carbon nanotubes is that
328	their atomic structure is based upon wrapping of graphene sheets in such a manner that
329	they expose almost entirely basal-plane graphite along their sidewalls.
330	In contrast, nanofibers grown by the methods used here expose large amounts of
331	edge-plane graphite. In nanocarbons, such as single walled nanotubes and nanofibers, the
332	activity is often increased by harsh oxidation procedures such as boiling in hot nitric acid,
333	which creates defects and partially oxidizes the materials [13].
334	Another approach to increasing the surface area is to use nanostructures as a
335	template for other materials, such as metals. This is particularly attractive for
336	applications such as electrocatalysis, where the high surface area and tunable chemical
337	reactivity of the metals can both be used. However, the results demonstrate that even
338	noble metals such as gold can provide significant increases in the accessible surface area
339	that could be used to practical advantage. VACNFs have been shown to increase the
340	surface area of an electrode by at least 7 times [34]. This results from the well defined
341	cylindrical geometry that VACNFs assume. Each fiber in a VACNF electrode also has
342	the added benefit of an individual contact to the underlying electrode as a result of the
343	growth mechanism. Thus VACNFs by themselves meet the requirements for materials

344 applications in energy storage and conversion, making them an ideal choice for

- 345 modifications.
- 346
- 347 *4.2 Surface modification.*

348 One key issue in forming metal nanocomposites on carbon surfaces is the 349 adhesion of the metals to the carbon surface. This is typically enhanced by oxidation of 350 the surface using strong oxidizing acids, such as HNO<sub>3</sub>. While this procedure can be 351 effective, especially for bulk high surface-area carbons, it also has a few drawbacks. 352 First, wet-chemical oxidation leads to a broad distribution of different types of oxidized 353 carbon, only some of which are effective at binding to metals. This can be problematic 354 for nanostructured carbon materials. Secondly, the harsh oxidizers are difficult to 355 integrate with many metals commonly used as electrode materials. In contrast, the FTIR 356 data show that the molecular functionalization with only carboxylic acid moieties was 357 achieved on the surface under extremely gentle conditions, using 254 nm light to trigger 358 the reaction.

359 One issue of initial concern was whether the molecules would act as insulators, 360 adding a series resistance to the nanofiber-metal interface. However, the results suggest 361 that any such resistances are negligible. These results are also consistent with previous 362 results [34-36] using several different molecules, in each case showing that although the 363 molecular densities are relatively high, the layers are sufficiently porous that good 364 electrical contact is still made between the nanofiber and the metal electrode. Thus, the 365 molecular monolayer can be used to enhance metal adhesion to the nanofibers without 366 adversely affecting the electrical properties.

367

#### 368 *4.3 Surface texture.*

369	While the use of molecular monolayers provides a high density of chelating sites
370	for metal deposition, the electroless deposition process results in a surprisingly
371	corrugated surface texture. Electroless metal deposition generally results in smooth films
372	[37]. Textured structures similar to those reported here have been reported previously
373	from electrochemical deposition onto highly-oriented pyrolitic graphite (HOPG) [38-40],
374	with dendritic gold nanoparticles nucleating at step edges of the HOPG. Steps on HOPG
375	reveal atomic structures essentially identical to those of the edge planes exposed every
376	~2-3 nm along the VACNFs.
377	In these previous studies, the highly textured geometry has been attributed to
378	anisotropic diffusion of gold on different crystal planes, which can depend strongly on
379	the types of ions in solution. Similar spike-like coatings, or dendritic coatings, can be
380	formed by electroless deposition, but usually only under fast deposition conditions. That
381	is, conditions of high pH, elevated temperatures, or large metal concentrations [41-43].
382	Under these conditions the deposition reactions are fast and diffusion limited aggregation
383	generally dominates the growth, resulting in a more fractal looking structure [42, 43].
384	The method reported here is not operating under these conditions. Similar
385	electroless gold deposition protocols used on porous polymer surfaces [25, 44, 45], as
386	well as planar polymer and glass surfaces [46] have not reported any spike-like textures
387	with their deposits. Additionally, control experiments performed in on planar glassy
388	carbon, using identical procedures as described above, did not result in any highly
389	textured deposits. While the formation of this highly textured coating remains not fully

390 understood, it appears that the highly textured coating leads to many of the observed

- 391 electrochemical properties of the electrodes.
- 392

393 *4.4 Electrochemical behavior of the textured surface.* 

394 Understanding the electrochemical behavior of gold surface is essential to 395 understanding and predicting the response of the electrodes. Electrodes of this nature 396 generally are either treated as rough electrodes and described by distributed elements 397 such as a constant phase element (CPE) [47], or they are treated as porous electrodes and 398 described with a transmission line model (TLM) [48], in which the impedance of a pore 399 is defined in terms of an infinitely long transmission line defined by the solution 400 resistivity and the impedance of the wall-electrolyte interface [48-50]. The distinction as 401 to which of these two models is most appropriate is based on the depth of the pores 402 relative to an effective penetration depth that describes how far an AC electric field 403 penetrates into the pores [48-50]. The depth of the "pores" is  $\sim 2 \mu m$ . In this size range, 404 the TLM model collapses to a rough electrode model [49] and a simple distributed 405 element, such as a constant-phase element, is a better choice than the TLM for modeling 406 the electrical properties of the system [47].

The CPE is defined via the impedance relationship  $Z_{cpe} = 1/T(i\omega)^{\phi}$ , where T and  $\phi$ are parameters. A perfect capacitor has T=C and  $\phi$ =1; deviations from these values can reflect a variety of non-ideal properties including microscopic roughness, electrical inhomogeneties at the interface, or diffusion limits to the electrode [47, 51, 52]. An electrode that shows deviations based solely on diffusion limited effects has an exponent equal to 0.5 [52]; exponents between 0.5 and 1 are often attributed to roughness effects

413 [47, 51]. It is likely that the complex shape of the electrodes leads to a combination of414 these effects.

415 Table 1 summarizes the parameters determined by fitting the data with an 416 equivalent circuit consisting of a resistor in series with the parallel combination of a CPE 417 and a resistor. It is clear from table 1 that the samples show a significant deviation from 418 ideal capacitance ( $\phi$ =1). If the electrodes were behaving as true porous systems with 419 diffusion occurring primarily between fibers down the length of the pore, one would 420 expect an exponent value of 0.5 [52]. Diffusion occurring between a rough surface and 421 the solution should result in an exponent between 0.5 and 1 [47, 51]. Thus, the exponent 422 of 0.88 obtained for the gold-coated nanofiber electrodes in 0.1 M KCl implies that the 423 microscopic surface roughness associated with the network of gold influences the 424 response of the electrodes, rather than diffusion between individual fibers in this system. 425 Table 1 also shows that when the electrolyte concentration is kept constant but a redox 426 agent is added, the charge-transfer resistance drops significantly, and the exponent value 427 changes from 0.88 to 0.59. This change in the exponential value suggests a transition 428 from complex behavior to more diffusion limited behavior in the presence of a redox 429 agent, given that exponential values of 0.5, generally indicate diffusion limited behavior. 430 Calculations of active surface area based on the measurements in the presence of 431 a redox couple show an area equivalent to the projected area of the electrode, rather than 432 the extended area of the length of the fibers enhanced by the microtextured gold coating. 433 This supports the hypothesis that diffusion occurs primarily between the nanofibers and 434 the solution, and this limits the performance of the electrode in the presence of a redox 435 couple. It should also be pointed out that the deviation from ideal capacitive behavior

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distribution observed for gold coated carbon fibers is not significantly different from the deviation observed for bare carbon nanofibers with no gold coating, in KCl solutions [53]. The similarity in exponents between "bare" and gold-coated nanofibers implies that the deviation from "ideal" behavior is associated primarily with the nanofibers and not with the smaller-scale structure of the gold. This implies that the active surface area can be increased, without significantly altering the frequency response of the electrode, by the addition of gold in the absence of charge transfer.

The very high surface area provided by gold coating leads to interesting properties that could potentially be useful for applications such as energy storage in electrochemical double-layer capacitors[1]. Assuming a series RC model, the effective capacitance of the system can be extracted from the impedance using

 $C = \frac{-1}{2\pi f Z \sin \theta}$ 

(2)

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450 The high surface area obtained after 7 hours of gold deposition, leads to an effective capacitance of  $3.25 \text{ mF cm}^{-2}$  [17]. This is a substantial increase compared to the average 451 effective capacitance of 290 mF cm<sup>-2</sup> for bare nanofibers in the same solution [17]. The 452 453 value of  $3.25 \text{ mF cm}^{-2}$  is comparable to that obtained from rough porous gold electrode 454 produced by leaching out a component from a gold alloy [54]. The short nanofibers 455 investigated here yield capacitance values that are slightly smaller than the values of  $\sim 0.5$ to 50 mF cm<sup>-2</sup> obtained from high surface-area activated carbon electrodes in aqueous 456 457 solution of KOH [5, 55]. Nonetheless, the combination of highly textured gold on top of

458 carbon nanofiber scaffolding presents a unique material that can be customized for459 different applications.

460

#### 461 **5. Conclusions**

462 A new fabrication method for producing tunable nanoscale gold-carbon 463 composite electrodes has been demonstrated. The method utilizes molecular 464 functionalization, developed for planar carbon materials, to provide a high density of 465 carboxylic acid binding sites uniformly distributed along the length of the carbon 466 nanofiber starting materials. This approach avoids strong oxidants, making this method 467 fully compatible with metal substrates. The deposition process allows for control over 468 the amount of gold added to the surface. The resulting electrodes show high accessibility 469 in aqueous solutions. This method should be extendible to different metals, allowing for 470 the creation of electrodes for use in a variety of applications including energy conversion 471 and electrocatalysis.

472 The tunable nature of the metal deposition process can lead to useful substrate 473 materials ranging from highly disperse particles of metal [18], useful in applications such 474 as fuel cells and catalysis, to the full, highly textured coatings studied here. Gold has been 475 shown to be catalytically active when present in the nanoscale [11, 56, 57]. Nanoscale 476 gold has also attracted attention recently as a catalysis substrate for fuel cells [45, 58, 59]. 477 In these applications, using a small amount of metal does not significantly alter the 478 electrical response of the underlying carbon nanofibers [18]. Thus this method could be 479 used to fabricate metal-coated carbon nanofibers with varied amounts of metal, 480 depending on the needs of the study and/or application.

481	In addition to the tunable metal coating, this approach is also flexible in terms of						
482	geometry and scale. While this approach was demonstrated here on vertically aligned						
483	carbon nanofibers grown on an electrode, free standing carbon nanofibers with high						
484	densities of edge plane carbon are commercially available. Given the availability of such						
485	materials, scaling up this approach and using varied geometries should be possible. There						
486	are several functionalization methods that can be used to add molecular monolayers to						
487	free standing carbon nanofibers[60], creating the anchoring sites for metal deposition.						
488	Coupling these methods with electroless deposition, as demonstrated here, will create a						
489	highly flexible materials platform useful in many varied applications.						
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491	Acknowledgments						
492	This work was supported in part by the National Science Foundation Grant DMR-						
493	0210806.						
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600	Figure Captions					
601	Figure 1. Scanning electron microscopy images of carbon nanofibers A) before gold					
602	bath, B) after 3 hours in a gold bath and C) after 7 hours in a gold bath.					
603						
604	Figure 2. Fourier transform infrared (FTIR) spectra of carbon nanofibers.					
605	A) functionalized with carboxylic acids					
606	B) functionalized with carboxylic acids and exposed to tin;					
607	C) control sample without functionalization but exposed to tin.					
608						
609	Figure 3. A) Absolute impedance and B) phase angle as a function of frequency,					
610	measured at the open circuit potential in 0.1 M KCl for bare carbon nanofiber					
611	(dash-dotted line), carbon nanofibers after 3 h gold deposition (dotted line) and					
612	carbon nanofibers after 7 h gold deposition (solid line).					
613						
614	Figure 4. A) Absolute impedance and B) phase angle as a function of frequency,					
615	measured at the open circuit potential in 0.1 M KCl for glassy carbon (solid) and					
616	gold (dotted) planar electrode					
617						
618	Figure 5. A) Absolute impedance and B) phase angle as a function of frequency,					
619	measured at the open circuit potential in 0.1 M KCl $(solid)$ 0.1 M KClO <sub>4</sub> (dotted)					
620	on a 7 h gold-coated carbon nanofiber electrode					
621						

622	Figure 6. A) Absolute impedance and B) phase angles response as a function of
623	frequency for a 7 h gold- coated carbon nanofiber electrode in 100 mM KCl
624	(crosses) and in 4 mM $Ru(NH_3)_6$ in 100 mM KCl (circles). The lines represent
625	fits calculated using the C) equivalent circuit model.
626	
627	Figure 7. Absolute impedance and phase angle as a function of frequency, in 0.1 M KCl
628	(crosses), and 5 mM $Ru(NH_3)_6^{2^{2/3+}}$ in 0.1 M KCl (circles) on glassy carbon (A &
629	B) and gold (C & D) planar electrodes. Line represent fits to the data calculated
630	using the equivalent circuit model in Figure 6C.
631	
632	Figure 8. Cyclic voltammograms collected in 5 mM $Ru(NH_3)_6^{24/3}$ + in 0.1 M KCl at 25
633	mV s <sup>-1</sup> over A) a planar gold electrode and B) a 7 h gold-coated carbon nanofiber
634	electrode.
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637	Table 1. Equivalent circuit model (Figure 7C.) parameters for a 7 h gold-coated carbon
638	nanofiber electrode, a planar gold electrode and a planar glassy carbon electrode
639	in 0.1 M KCl and 5 mM $Ru(NH_3)_6^{2+/3+}$ in 0.1. M KCl.
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#### NUSCRIP1 ACCEP ΕD F.

	Gold-CNF		Gold Foil		Glassy Carbon	
Model Component	KCI	Ru <sup>2+/3+</sup>	KCI	Ru <sup>2+/3+</sup>	KCI	Ru <sup>2+/3+</sup>
R <sub>s</sub> (Ohm)	11	12	35	32	34	33
R <sub>ct</sub> (Ohm)	6.9 x 10 <sup>3</sup>	8.1 x 10 <sup>2</sup>	3.5 x 10 <sup>6</sup>	1.6 x 10 <sup>11</sup>	3.3 x 10 <sup>13</sup>	1.1 x 10 <sup>11</sup>
CPE T	0.0038	0.0129	8.7 x 10 <sup>-5</sup>	0.01	4.1 x 10 <sup>-5</sup>	0.01
ΟΡΕ φ	0.88	0.59	0.92	0.50	0.88	0.50

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10<sup>-1</sup>

10<sup>0</sup>

10<sup>1</sup> 10<sup>2</sup> Frequency (Hz) 10<sup>3</sup>

10<sup>4</sup>











